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# Digital Computer Program for Error Analysis of Inertial Navigation Systems

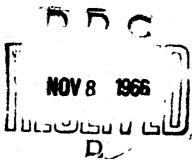
AUGUST 1966

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Prepared for COMMANDER SPACE SYSTEMS DIVISION
AIR FORCE SYSTEMS COMMAND
LOS ANGILES AIR FORCE STATION
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### DIGITAL COMPUTER PROGRAM FOR ERROR ANALYSIS OF INERTIAL NAVIGATION SYSTEMS

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COMMANDER SPACE SYSTEMS DIVISION AIR FORCE SYSTEMS COMMAND LOS ANGELES AIR FORCE STATION Los Angeles, California

#### FOREWORD

This report is published by the Aerospace Corporation, El Segundo, California, under Air Force Contract No. AF 04(695)-669.

The requirements for a generalised digital computer program for the error analysis of inertial guidance systems applicable to space missions was established in December 1963. Although under continuing development, the program has been used for system design and analysis studies since June 1964.

This report contains the first complete description of the program and replaces the partial and proliminary ones that have been issued. Its information should be sufficient for most users of the program. This program replaces the one described by R. A. Moore and D. F. Meronek in "A Digital Computer Program for a Generalised Inertial Guidance System Error Analysis" (Reference 1) used previously at Aerospace Corporation. It provides the basic tool for future inertial navigation system error analyses. It was submitted on 24 August 1966 to Captain Ronald J. Starbuck. SSTRT, for review and approval.

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Captain Ronald J. Starbuck

Project Officer

Space Systems Division
Air Force System Command

#### **ABSTRACT**

The theory and assumptions used in developing equations for the error analysis of a general class of inertial navigation systems are described. The computer program developed for their solution is described from a user's point of view. Its application includes the synthesis and/or analysis of inertial navigation systems used in ballistic missile or terrestrial space missions. The program is designed to allow studies of both pure inertial and aided inertial navigation systems, the latter being the process of updating navigation data via data from external sensors.

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#### SECTION 1

#### INTRODUCTION

This report describes, from a user's point of view, a computer program developed for the error analysis of a general class of inertial navigation systems. It is generally understood that these systems will be used in connection with either ballistic missile or space mission applications.

Section 2 describes the classes of inertial navigation systems considered, develops the equations necessary to perform an error analysis, enumerates the assumptions made in their derivations, and describes the methods and equations used for data presentation. The equations in Section 2 form the bases for the computer program, which was developed to solve them.

Section 3 deals with the operational aspects of using the computer program to perform error analyses. The input data requirements and procedures are discussed and the resulting output data and formats described. The logical order of the computations resulted in the development of two independent programs: The first, called ERAN, solves the equations presented in Section 2.3; the second, called QUTP, solves those presented in Section 2.4. These were programmed for the IBM 7090/7094 to be run under the control of the IBM Basic Monitor (IBSYS) Programming System with the assumption that core is set to zero before loading of the programs. There is a certain amount of intentional redundancy in the material presented in Sections 2 and 3. This was done so that once one is familiar with the material presented in Section 2, it will only be necessary to refer to Section 3 for program operations.

Section 4 presents three sample test cases illustrating the input data procedures and the formats of output data, and demonstrating some of the flexibility and capabilities of the program.

Appendices A through C present material augmenting the main body of the report. Appendix A consists of Standard Input Data Forms, Appendix B contains ERAN and OUTP Input Data for Sample Cases, and Appendix C gives the Output Listings for Sample Cases.

Appendix D is devoted to the subject of updating or correcting navigation data through the use of external data sources utilizing various sensor configurations. Algorithms are derived for three possible schemes of data processing. Although equations have not been programmed, the logical structure of the computer program is designed so that this feature can be incorporated without major revisions.

In Appendix E the method is discussed of treating the effects of aerodynamic drag in orbit when the accelerometers are disconnected from the navigation computer.

Appendix F contains all the figures called out in the report and Appendix G the program definitions and constants.

#### **SECTION 2**

#### **EQUATION DEVELOPMENT**

#### 2. 1 INTRODUCTION

This section defines the classes of inertial navigation systems considered and develops the equations necessary to perform an error analysis of a given configuration.

Section 2.3 relates the derivation of the differential equations of navigation error to a broad class of system errors. The solution of these equations results in the linear transformations (sensitivities) of navigator errors into errors of navigation data. The classes of errors include those of sensor anomalies, initial conditions, terminal control, and, for certain operational procedures, the effect of orbital drag uncertainties.

Section 2.4 describes the equations used for processing these sensitivities into individual navigation vector errors for each error source, and those which statistically sum all vector errors presented as a covariance matrix. Various coordinate systems and processing methods are described for data presentation.

#### 2. 2 NAVIGATION SYSTEM CONFIGURATIONS

The inertial navigation system configurations considered are schematically presented in Figure 1. The equations developed for error analysis are applicable to torqued or inertially oriented gimballed-platform systems, and to a certain class of strapped-down systems. The essential sensors used by the navigation system are three accelerometers, which sense the magnitude of the applied external accelerations, and three gyros, \* which sense angular dynamics so that the direction of the applied acceleration can be derived. The constraints of accelerometer mounting are such that the three sensing (input) axes cannot be coplanar, but can be nonorthogonal. Gyros are assumed to be mounted in a triad so that their sensing (input) axes are orthogonal. The method of deriving accelerometer orientation from gyro signals is assumed to be one of the following three:

- Gimballed Platforms. In this configuration the most conventional - the platform is initially aligned to some auxiliary references. For initial alignment on the ground, the gravity vector, which is sensed by pendulums or the accelerometers, is used for vertical reference; azimuth is referenced to either optical sensors or a gyro compass. For in-orbit alignment, stellar or horizon sensors are used. The gyros measure any deviation of the platform from the initial alignment and their signals are used to torque the platform in such a way that they become null, thus maintaining the initial reference. In some cases, the platform is torqued either to reduce the total gimbal-angle travel, or to maintain prelaunch (earth) rates. To achieve this, the gyros are torqued at prescribed rates, which the platform follows. In this case, the accelerometer transformation matrix is a function of time and computed from the commanded rates. Mathematically, this is identical to configuration (b).
- b. Strapped-down/Caged Gyros. In this configuration, the platform is mounted directly (possibly by a shock mount) to the airframe. The gyros sense angular deviations from the initial reference, but are torqued to null their

<sup>\*</sup>Two single-degree-of-freedom gyros can be oriented to represent one two-degree-of-freedom gyro.

signals. These torquing signals are a measure of the rate-of-change of the platform orientation and are used to compute the transformation matrix required for the accelerometers. The algorithm used is based on the matrix differential equation of direction cosines.

Strapped-down/Free Gyros. Until the advent of the electrostatic gyro (ESG), lighweight wide-angle free gyros were not sufficiently accurate to be considered for this application. Free (two-degree-of-freedom) gyros are used in platform configurations but are restricted to small-angle deviations. With its high degree of accuracy, the ESG acts as a potential attitude reference sensor. In this configuration, the angles the gyro case (thus, the accelerometer) makes with respect to the spin axis of the gyro are read out and used to compute the transformation matrix.

The sensor data is processed by a computer to derive position and velocity data. It is assumed that the navigation system computer has perfect algorithms for gravity, and that its word length and integration schemes are such as to produce negligible errors. Most accelerometer outputs are in the form of pulse rates proportional to acceleration, thus there are additional complications in deriving inertial velocity when the platform is not inertially oriented. The algorithms used in these cases become the subject of a separate analysis, which requires detailed knowledge of the hardware characteristics. In general, a special-purpose computer (e.g., a Digital Differential Analyzer) would be required to buffer the processing of accelerometer and gyro data into a suitable form for processing by a general-purpose computer. Generally, this form is sensed velocity data, which is then corrected for the effects of gravity from which the trajectory position and velocity data are determined. In this analysis it is assumed that the error in these computations is small enough to be negligible, or convertible to equivalent sensor errors; therefore, the errors in indicated position and velocity are functions of sensor anomalies only.

Provisions are included for analyses of aided inertial navigation systems in which external sensors are used for measuring position, velocity, and/or

platform orientation. The measurements are processed by various techniques and applied as corrections to the navigation system data. These corrections are discussed in Appendix D under Resets. The computer program in its present form does not include the coding of these equations.

#### 2.3 ERROR SENSITIVITY EQUATION DEVELOPMENT

#### 2.3.1 Coordinate Systems and Transformation Matrices

The basic coordinate system used for computing navigation errors is an earth-centered inertial (ECI) system, in which the Z axis is along the earth's polar axis, and the X and Y axes lie in the earth's equatorial plane, forming a right-hand orthogonal axis system. Generally, the convention is that the X axis passes through the Greenwich meridian at time zero.

The notation used for coordinate transformation matrices is the symbol M with two-lettered subscripts to identify the respective coordinate systems; e.g.,  $M_{EK}$  identifies the transformation matrix, which is used to transform vectors to the ECI coordinate system from the K coordinate system. Conversely,  $M_{KE}$  transforms vectors to the K system from the ECI system. The necessary coordinate systems and the transformation matrices are described in the following paragraphs.

#### 2.3.1.1 Platform Coordinate System

The platform axes are designated  $P_1$ ,  $P_2$ , and  $P_3$  and form a right-hand orthogonal coordinate system. The initial transformation matrix is developed by considering the platform axes to be initially aligned with the ECI axes and by applying ordered rotations of  $\phi_P$  about  $P_3$ , a negative  $\lambda_P$  about  $P_2$ , and a negative  $\psi_P$  about  $P_1$ . Thus, the matrix that transforms vectors in ECI coordinates to vectors in platform coordinates is

$$\mathbf{M_{PE}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\psi_{\mathbf{P}} & -S\psi_{\mathbf{P}} \\ 0 & S\psi_{\mathbf{P}} & C\psi_{\mathbf{P}} \end{bmatrix} \begin{bmatrix} C\lambda_{\mathbf{P}} & 0 & S\lambda_{\mathbf{P}} \\ 0 & 1 & 0 \\ -S\lambda_{\mathbf{P}} & 0 & C\lambda_{\mathbf{P}} \end{bmatrix} \begin{bmatrix} C\phi_{\mathbf{P}} & S\phi_{\mathbf{P}} & 0 \\ -S\phi_{\mathbf{P}} & C\phi_{\mathbf{P}} & 0 \\ 0 & 0 & 1 \end{bmatrix} (t = t_{o})$$

Figure 2 illustrates the usual initial platform orientation, where  $\phi_P$  is the longitude,  $\lambda_P$  is the geocentric latitude (positive North latitude), and  $\psi_P$  is the asimuth (positive is conventional asimuth from North).

Since platform coordinates are orthogonal

$$M_{\mathbf{EP}} = M_{\mathbf{PE}}^{\mathbf{T}}$$

where T denotes the transpose. M<sub>PE</sub> can be a function of time (for strapped-down or torqued platforms) and its calculation is discussed in Section 2.3.2.

#### 2.3.1.2 Gyro Coordinate System

It is necessary to assign a coordinate system to each gyro so that the gyro errors can be determined. The gyro axes for each component are right-hand orthogonals and designated  $G_{i1}$ ,  $G_{i2}$ , and  $G_{i3}$  (i = number 1, 2, or 3 gyro), where  $G_{i1}$  is the sensing (input) axis of the i<sup>th</sup> gyro. It is assumed that  $G_{11}$ ,  $G_{21}$ , and  $G_{31}$  also form a right-hand orthogonal axis system.

As a result of this assumption, the development of the gyro coordinate systems is simplified. Since, for any one configuration, the gyro axes are assumed to be fixed with respect to the platform axes, the gyro coordinate systems are developed with respect to the platform coordinate system. Figure 3 illustrates the initial gyro alignments with respect to the platform axes. The method of specifying gyro orientations is by specification of an axis (1, 2, or 3) and an argument (angles) of successive rotations. Each rotation operates on the gyros as a triad; i.e., all three gyros are being rotated and thus are maintaining their axis crientation with respect to each other during the rotations. The axis of rotation referred to above is that of the number one gyro. Thus, the matrix that transforms vectors in platform coordinates to gyro coordinates (gyro input axes) is

$$M_{GP} = T_{ij} \cdot \cdot \cdot \cdot \cdot T_{i2}T_{i1}$$

where

i = the axis of rotation (i = 1, 2, or 3)

 $j = the j^{th}$  rotation (j = 1, 2, ... up to 5)

and

$$T_{1j} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\theta_j & S\theta_j \\ 0 & -S\theta_j & C\theta_j \end{bmatrix}$$

transformation for a rotation about G<sub>11</sub> axis

$$T_{2j} = \begin{bmatrix} C\theta_j & 0 & -S\theta_j \\ 0 & 1 & 0 \\ S\theta_j & 0 & C\theta_j \end{bmatrix}$$

transformation for a rotation about G<sub>12</sub> axis

$$T_{3j} = \begin{bmatrix} C\theta_j & S\theta_j & 0 \\ -S\theta_j & C\theta_j & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

transformation for a rotation about G<sub>13</sub> axis

where  $\theta_i$  is the angle of the j<sup>th</sup> rotation and a positive angle is in the sense of a right-hand rotation. Upon completion of this set of rotations, there remains an additional degree of rotational freedom of each gyro about its input axis. By considering this degree of freedom, the vector components along the other two axes of the gyro (axes 2 and 3) are determined, utilizing the matrices

$$M_{G2} = \begin{bmatrix} 0 & C\psi_1 & S\psi_1 \\ S\psi_2 & 0 & C\psi_2 \\ C\psi_3 & S\psi_3 & 0 \end{bmatrix}$$
 transforms a vector in gyro coordinates to vector components along the 2 axis of each gyro

$$\mathbf{M}_{G3} = \begin{bmatrix} 0 & -S\psi_1 & C\psi_1 \\ C\psi_2 & 0 & -S\psi_2 \\ -S\psi_3 & C\psi_3 & 0 \end{bmatrix}$$
 transforms a vector in gyro coordinates to vector components along the 3 axis of each component

where  $\psi_i$  is the angle of rotation for the i<sup>th</sup> gyro and a positive angle is in the mense of a right-hand rotation.

It is convenient to describe the gyro axes in the model of a single-degree-offreedom gyro, where the  $G_{i,1}$  is the input reference axis,  $G_{i,2}$  is the output axis, and  $G_{i3}$  is the spin reference axis. Then a rotation of  $\psi_i$  = 90 deg of ith gyro will provide an orientation of two gyros with orthogonal input axes and parallel spin axes, a model of a two-degree-of-freedom gyro. Since the gyro (input axes) coordinate system is orthogonal, the following transformations are derived

$$M_{PG} = M_{GP}^{T}$$

$$M_{GE} = M_{GP}M_{PE}$$

$$M_{EG} = [M_{GP}^{M}_{PE}]^{T} = M_{EP}^{M}_{PG}$$

#### 2.3.1.3 Accelerometer Coordinate System

The following two options are used for specifying the alignment of accelerometers.

#### FIRST OPTION

First is the specification of an orthogonal triad and the method of specification is identical with that described for the gyro components; that is, an axis and argument of successive rotations are specified to align the accelerometer

input axes. Then an additional degree of freedom about each accelerometer's input axis is specified by an angle  $\beta_i$ . The accelerometer axes for each component are right-hand orthogonal and are designated A; 1, A; 2, and A; (i = number 1, 2, or 3 accelerometer), where  $A_{i,1}$  is considered the input axis. Figure 4 illustrates the initial orientation of the accelerometer axes with respect to the platform axes. The following matrices apply for accelerometers when this option is used.

$$M_{AP} = T_{ij} \dots T_{i1}$$
 (j = 1, 2, . . . up to 5)

$$\mathbf{M}_{A2} = \begin{bmatrix} 0 & C\beta_1 & S\beta_1 \\ C\beta_2 & 0 & -S\beta_2 \\ C\beta_3 & S\beta_3 & 0 \end{bmatrix} \quad \begin{array}{c} \text{transforms a vector in} \\ \text{accelerometer coordinates} \\ \text{to vector components along} \\ \text{the 2 axes of each accelerometer} \end{array}$$

$$M_{A3} = \begin{bmatrix} 0 & -S\beta_1 & C\beta_1 \\ C\beta_1 & 0 & -S\beta_2 \\ -S\beta_3 & C\beta_3 & 0 \end{bmatrix}$$
 transforms a vector in accelerometer coordinates to vector components along the 3 axes of each accelerometer

$$M_{PA} = M_{AP}^{T}$$

$$M_{AE} = M_{AP}M_{PE}$$

$$M_{EA} = [M_{AP}M_{PE}]^T = M_{EP}M_{PA}$$

#### SECOND OPTION

The second option allows for a nonorthogonal accelerometer configuration. Here the method of specification is the same (i.e., specification of an axis and an argument); however, each accelerometer is specified independently. The initial orientation of each accelerometer is the same with the accelerometer's input Axis  $A_{il}$  aligned with  $P_1$ ,  $A_{i2}$  with  $P_2$ , and  $A_{i3}$  with  $P_3$ . Therefore, a matrix is developed for each accelerometer k, as follows:

$$M_{APk} = T_{ijk} \cdot ... T_{i2k} T_{i1k} (k = 1, 2, and 3)$$

From these three matrices, the matrices MAP, MA2, and MA3 are formed as

$$M_{AP} = \begin{bmatrix} M_{11} \\ M_{12} \\ M_{13} \end{bmatrix}$$

$$\mathbf{M}_{\mathbf{A}2} = \begin{bmatrix} \mathbf{M}_{21} \\ \mathbf{M}_{22} \\ \mathbf{M}_{23} \end{bmatrix} \mathbf{M}_{\mathbf{P}\mathbf{A}}$$

$$M_{A3} = \begin{bmatrix} M_{31} \\ M_{32} \\ M_{33} \end{bmatrix} M_{PA}$$

where  $M_{ik}$  is the i<sup>th</sup> row of  $M_{APk}$  (k = 1, 2, 3)

Since for this option the accelerometers are nonorthogonal,  $M_{\hbox{\it pA}}$  is developed from the inverse rather than the transpose, and the following relationships result

$$M_{PA} = M_{AP}^{-1}$$

$$M_{AE} = M_{AP}M_{PE}$$

$$M_{EA} = [M_{AP}M_{PE}]^{-1} = M_{EP}M_{PA}$$

#### 2.3.1.4 Initial Condition Coordinate System

These coordinate systems are used to transform errors specified in a convenient coordinate system into errors in ECI coordinates. The initial platform errors are specified in the platform coordinate system and transformed into ECI coordinates by  $M_{EP}$ . Two options are provided for specifying initial position and velocity errors. In the first, the errors are assumed to be referenced to platform axes; thus  $M_{EP}$  is used. In the second, the errors are assumed to be referenced to the geocentric vertical and directed in azimuth by a specified angle  $(\psi_{I})$  (see Figure 5). The transformation matrices for position and velocity errors are then

#### OPTION 1

$$M_{EI} = M_{EP}$$

OPTION 2

$$\mathbf{M}_{E,I} = \begin{bmatrix} \mathbf{C} \mathbf{Ø} & -\mathbf{S} \mathbf{Ø} & 0 \\ \mathbf{S} \mathbf{Ø} & \mathbf{C} \mathbf{Ø} & 0 \\ \mathbf{0} & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{C} \lambda & 0 & -\mathbf{S} \lambda \\ 0 & 1 & 0 \\ \mathbf{S} \lambda & 0 & \mathbf{C} \lambda \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & \mathbf{C} \psi_{\mathbf{I}} & \mathbf{S} \psi_{\mathbf{I}} \\ 0 & -\mathbf{S} \psi_{\mathbf{I}} & \mathbf{C} \psi_{\mathbf{I}} \end{bmatrix}$$

where

$$S\phi = \frac{Y}{D}$$

$$S\lambda = \frac{Z}{R}$$

$$C\phi = \frac{X}{D}$$

$$C\lambda = \frac{D}{R}$$

$$D = \sqrt{X^2 + Y^2}$$

$$R = \sqrt{D^2 + Z^2}$$

and

X, Y, Z = initial (t =  $t_0$ ) ECI position coordinates  $\emptyset$  and  $\lambda$  = the initial longitude and geocentric latitude, respectively  $\psi_t$  = the azimuth orientation of the coordinate system.

#### 2.3.1.5 Terminal-condition Coordinate System

These coordinate systems are used when it is desired to propagate the effects of terminal-control errors generated by other systems for which there can be no further corrections (e.g., guidance steering and thrust tailoff errors at thrust termination of a ballistic missile). The transformation for terminal-position errors is

$$\mathbf{M_{ET1}} = \begin{bmatrix} \mathbf{C} \phi & -\mathbf{S} \phi & \mathbf{0} \\ \mathbf{S} \phi & \mathbf{C} \phi & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{1} \end{bmatrix} \begin{bmatrix} \mathbf{C} \lambda & \mathbf{0} & -\mathbf{S} \lambda \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{S} \lambda & \mathbf{0} & \mathbf{C} \lambda \end{bmatrix} \begin{bmatrix} \mathbf{1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{C} \psi & \mathbf{S} \psi \\ \mathbf{0} & -\mathbf{S} \psi & \mathbf{C} \psi \end{bmatrix}$$

where

$$SØ = \frac{Y}{D}$$
  $S\lambda = \frac{D}{R}$   $S\psi = \frac{V_E}{V_H}$ 

$$C\emptyset = \frac{X}{D}$$
  $C\lambda = \frac{Z}{R}$   $C\psi = \frac{V_N}{V_H}$ 

$$D = \sqrt{X^2 + Y^2}$$
  $R = \sqrt{D^2 + Z^2}$ 

$$V_{E} = \frac{-Y\dot{X} + X\dot{Y}}{D}$$

$$V_{N} = \frac{-Z(X\dot{X} + Y\dot{Y}) + \dot{Z}D^{2}}{RD}$$

$$v_{H} = \sqrt{v_{N}^2 + v_{E}^2}$$

and

X, Y, Z = terminal ECI position coordinates

 $\dot{X}$   $\dot{Y}$   $\dot{Z}$  = terminal ECI velocity coordinates

 $V_E V_N V_H = east$ , north, and horizontal velocity vector components

 $\phi$ ,  $\lambda$ ,  $\psi =$ longitude, latitude, and velocity vector azimuth at the termination time

The transformation for terminal velocity errors is

$$\mathbf{M_{ET2}} = \mathbf{M_{ET1}} \begin{bmatrix} \mathbf{C_Y} & \mathbf{0} & \mathbf{S_Y} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ -\mathbf{S_Y} & \mathbf{0} & \mathbf{C_Y} \end{bmatrix}$$

where

$$s_Y = \frac{x\dot{x} + y\dot{y} + z\dot{z}}{RV}$$

$$C_Y = \frac{V_H}{V}$$
  $V = (\dot{x}^2 + \dot{y}^2 + \dot{z}^2)^{1/2}$ 

and

- y is the flight path angle and equals the angle that the velocity vector makes with the horizontal plane
- V is the magnitude of the velocity vector.

These coordinate systems are illustrated in Figure 6.

The other coordinate systems, used for output data and reset, are described in Section 2.4.1 and Appendix D.

#### 2. 3. 2 Navigation Kinematics

For purposes of error analyses, it is of interest to derive the sensitivities of navigation and platform orientation errors as a function of the anomalies of system parameters (which are random variables). These sensitivities are then used with the statistics of the system parameters to develop the statistical characteristics of the navigation data. For this purpose, the differential equations are linearized so that all the advantages of linear analysis can be utilized. The following sections develop this procedure.

#### 2. 3. 2. 1 Equations of Motion

The differential equation, expressed in ECI coordinates, that describes the vehicle equations of motion for an assumed point mass system is

$$\ddot{\ddot{\mathbf{X}}} = -\frac{\mu}{\mathbf{R}^3} \left[ \ddot{\mathbf{X}} + \ddot{\mathbf{G}} \right] + \dot{\ddot{\mathbf{X}}}_{\mathbf{s}}$$

where

 $\mu$  = gravitational constant

R = magnitude-of-position vector

 $\overline{G}$  = vector of higher-order gravity terms

 $\frac{\mathbf{x}}{\mathbf{X}}$  = acceleration vector of the vehicle

x
s = sensed acceleration vector due to all external forces (thrust, drag, etc.)

The navigation system's computer mechanizes and solves this equation with the appropriate initial conditions of position and velocity  $(X_0 \text{ and } X_0)$ . The sensed acceleration components are measured by the accelerometers and transformed into ECI coordinates resulting in

$$\ddot{\bar{X}}_{sm} = [M_{EP}M_{PA}]_1 \bar{A}_{oc}$$

where

X
sm = the sensed acceleration measured and transformed into ECI coordinates

[M<sub>EP</sub>M<sub>PA</sub>]<sub>1</sub> = the transformation between accelerometer and ECI coordinates, which the computer uses

A c = accelerometer measurements corrected for calibrated anomalies

<sup>\*</sup>The choice of coordinate systems made here was for convenience. The results are invariant with the computational coordinate system chosen, provided that the assumption of perfect computer algorithms is valid.

The corrected accelerometer measurements are the result of input accelerations and functionally related correction terms. Thus, the accelerometer equation becomes

$$\overline{\mathbf{A}}_{oc} = \overline{\mathbf{A}}_{e} + \mathbf{f} (\overline{\mathbf{A}})$$

$$= \left[ \mathbf{M}_{AP} \mathbf{M}_{PE} \right]_{2} \ddot{\overline{\mathbf{X}}}_{e} + \mathbf{f} (\overline{\mathbf{A}})$$

where

A = uncorrected accelerometer measurements

f(A) = the equation for the accelerometer anomalies, which includes corrections for biases, scale factor, non-linearity, etc., based on instrument calibrations. (This function is discussed in Section 2. 3. 3, Error Sources)

[MAPMPE]<sub>2</sub> = the transformation between actual accelerometer axes and ECI coordinates, a function of platform errors, accelerometer alignments, nonlinearities, etc.

Therefore, the equation that is solved by the navigation computer is

$$\ddot{\overline{\mathbf{X}}} = -\frac{\mu}{R^3} [\overline{\mathbf{X}} + \overline{\mathbf{G}}] + [\mathbf{M}_{\mathrm{EP}} \mathbf{M}_{\mathrm{PA}}]_1 \{ [\mathbf{M}_{\mathrm{AP}} \mathbf{M}_{\mathrm{PE}}]_2 \ddot{\overline{\mathbf{X}}}_{\mathrm{s}} + \boldsymbol{f}(\overline{\overline{\mathbf{A}}}) \}$$

Generally, it is not required that a distinction be made between  $[M_{EP}^{\phantom{EP}M}_{PA}]_1$  and  $[M_{AP}^{\phantom{AP}M}_{PE}]_2$ , except in cases where a given error source affects both computer and platform transformations, e.g., initial position errors.

#### 2. 3. 2. 2 Constraints and Assumptions

Before proceeding to the linearization of the navigation system equations, the following constraints are imposed.

a. Nominal Trajectory Reference

The parameters that affect the sensed acceleration vector (e.g., thrust, weight, wind, control system, etc.) are

statistically independent of the navigation parameters (accelerometers, gyros, etc.). Therefore, to include them in the analysis would result in trajectory deviations constrained by the guidance system, but not necessarily in navigation errors of the measured trajectory. The only way in which the two sets of parameters could be entered into the analysis would be from nonlinearities for which Monte Carlo techniques would be required to develop their effects. Fortunately, these nonlinearities are small and can be assessed independently by performing a guidance error analysis and the navigation system error analysis, separately, using the same reference trajectory. The navigation error analysis can be repeated for the maximum perturbed trajectory developed in the guidance error analysis to determine if further analysis is required.

#### b. First-Order Partials

If the equations are expanded into a Taylor series, the relative magnitudes of second-order partials can be determined. For example, by taking one component of the gravity expression

$$X = -\frac{\mu}{R^3} X = -\frac{\mu}{X^2}$$
 (assuming R = X, Y = Z = 0)

and expanding it to

$$\Delta \ddot{X} = \frac{\partial \ddot{X}}{\partial X} \Delta X + \frac{\partial^2 \ddot{X}}{\partial X^2} \frac{(\Delta X)^2}{2!} + \cdots$$

$$=\frac{2\mu}{x^3}\left(1-\frac{3\Delta X}{2X}+\cdots\right)\Delta X$$

it is seen that the maximum effect of the second-order partial is a function of  $\Delta R/R$ . Since  $\Delta R/R <<< 1$  for any reasonable system, it can be neglected. Many analyses of inertial guidance systems neglect completely the first-order gravity partials\* or treat them as constants. \*\*

<sup>&</sup>quot;See for example Reference 2, p 304: "Use of Normalized Integrals."

<sup>\*\*</sup> See for example Reference 3.

With a similar analysis, the second-order gravity terms (G) can be eliminated, even though they present linear terms in the equations.

#### c. Small-Angle Approximations

Applying the small-angle approximation to platform and computer errors is justified on the basis of comparing second-order partials. With this approximation, small-angle rotations can be represented as vectors and the following vector matrix relationships can be used.

#### (1) Vector Transformations

$$\vec{p}_i = M_{ij} \vec{p}_j$$

where

= angular errors expressed in the i coordinate system due to angular errors in the j coordinate system | |

M<sub>ij</sub> = the transformation matrix to the i coordinate system from the j coordinate system.

For example

$$\overline{\phi}_{i} = \overline{\phi}_{E} = \begin{bmatrix} \phi_{x} \\ \phi_{y} \\ \phi_{z} \end{bmatrix} = M_{EP} \overline{\phi}_{P} = M_{EP} \begin{bmatrix} \phi_{1} \\ \phi_{2} \\ \phi_{3} \end{bmatrix}$$

#### (2) Matrix Differentials

$$[\delta \mathbf{M}_{ij}]_{i} = [\Phi_{i}] \mathbf{M}_{ij} = \begin{bmatrix} 0 & \phi_{3} & -\phi_{2} \\ -\phi_{3} & 0 & \phi_{1} \\ \phi_{2} & -\phi_{1} & 0 \end{bmatrix} \mathbf{M}_{ij}$$

See Reference 4, pp 251 to 253.

where

 $\begin{bmatrix} \delta M_{ij} \end{bmatrix}_i$  = the change in  $M_{ij}$  due to small rotations in the i coordinate system.

[\$\Phi\_i\$] = a skew symmetric matrix formed from the small angle rotations in the i coordinate system.

For example

$$\begin{bmatrix} \delta M_{PE} \end{bmatrix}_{P} = \begin{bmatrix} 0 & \phi_{3} & -\phi_{2} \\ -\phi_{3} & 0 & \phi_{i} \\ \phi_{2} & -\phi_{i} & 0 \end{bmatrix} M_{PE} = \begin{bmatrix} \phi_{P} \end{bmatrix} M_{PE}$$

when  $\phi_i$  are small rotations in platform coordinates.

Also

$$[\delta M_{EP}]_{P} = [\delta M_{PE}]_{P}^{T} = -M_{EP}[\Phi_{P}]$$

If the small rotations are expressed as rates times time ( $\phi \delta t = \omega \delta t$ ), then in the limit as  $\delta t \rightarrow 0$ , the matrix differential equation is

$$\frac{\left[\delta M_{EP}\right]_{P}}{\delta t} = M_{EP} = -M_{EP} \begin{bmatrix} 0 & \omega_{3} & -\omega_{2} \\ -\omega_{3} & 0 & \omega_{1} \\ \omega_{2} & -\omega_{1} & 0 \end{bmatrix} = -M_{EP} [\Omega_{P}]$$

and

$$\dot{M}_{\rm PE} = [\Omega_{\rm p}] M_{\rm PE}$$

#### (3) Matrix Transformations

$$\{\phi_j\} = M_{ji} \{\phi_i\} M_{ij}$$

where

[ • ] = skew symmetric matrix expressed in the j coordinate system due to rotations in the i coordinate system.

For example

$$\{ \mathbf{\Phi}_{\mathbf{E}} \} = \mathbf{M}_{\mathbf{EP}} [\mathbf{\Phi}_{\mathbf{P}}] \mathbf{M}_{\mathbf{PE}}$$

that is

$$\begin{bmatrix} 0 & \phi_{\mathbf{z}} & -\phi_{\mathbf{y}} \\ -\phi_{\mathbf{z}} & 0 & \phi_{\mathbf{x}} \end{bmatrix} = \mathbf{M}_{EP} \begin{bmatrix} 0 & \phi_{3} & -\phi_{2} \\ -\phi_{3} & 0 & \phi_{1} \\ \phi_{y} & -\phi_{\mathbf{x}} & 0 \end{bmatrix} \mathbf{M}_{PE}$$

This can be shown by using vector matrix relationships as follows: Let vectors in the P coordinate system be a lated as

$$\overline{Y}_{\mathbf{P}} = \overline{\phi}_{\mathbf{P}} \times \overline{A}_{\mathbf{P}} = -\overline{A}_{\mathbf{P}} \times \overline{\phi}_{\mathbf{P}}$$

$$= \begin{bmatrix}
0 & A_3 & -A_2 \\
-A_3 & 0 & A_1 \\
A_2 & -A_1 & 0
\end{bmatrix} \overline{\phi}_{\mathbf{P}} = -\begin{bmatrix}
0 & \phi_3 & -\phi_2 \\
-\phi_3 & 0 & \phi_1 \\
\phi_2 & -\phi_1 & 0
\end{bmatrix} \overline{A}_{\mathbf{P}}$$

$$= - [\phi_{\mathbf{P}}] \overline{A}_{\mathbf{P}}$$

Transforming the above vectors into E coordinates results in

$$\overline{Y}_{E} = M_{EP}\overline{Y}_{P} = -M_{EP}[\Phi_{P}]\overline{A}_{P}$$

$$\overline{\phi}_{E} = M_{EP}\overline{\phi}_{P}$$

$$\overline{A}_{E} = M_{EP}\overline{A}_{P}$$

The vectors  $\overline{Y}$ ,  $\overline{\phi}$ , and  $\overline{A}$  are invariant under an orthogonal transformation; therefore

$$\overline{Y}_{E} = \overline{\phi}_{E} \times \overline{A}_{E} = -[\Phi_{E}] \overline{A}_{E} = -[\Phi_{E}] M_{EP} \overline{A}_{P}$$

Equating the two above expressions for  $\overline{\overline{Y}}_{\mathrm{E}}$  results in

$$[\Phi_{\rm E}]M_{\rm EP} = M_{\rm EP}[\Phi_{\rm P}]$$

or

$$[\Phi_{\rm E}] = M_{\rm EP}[\Phi_{\rm P}] M_{\rm PE}$$

#### 2. 3. 2. 3 Linearization of the Differential Equation

The linearisation procedure is established by taking the partial derivatives with respect to each error source. The notation used is:  $\delta = \partial/\partial \epsilon_i = \text{parti.}^{-1}$  derivative with respect to the i<sup>th</sup> error source.

Neglecting the higher-order gravity term, we find that the navigation system equation to be linearized is

$$\ddot{\overline{\mathbf{X}}} = -\frac{\mu}{R^3} \, \overline{\mathbf{X}} + \left[ \, \mathbf{M_{EP}} \mathbf{M_{PA}} \, \right]_1 \left[ \, \mathbf{M_{AP}} \mathbf{M_{PE}} \, \right]_2 \, \ddot{\overline{\mathbf{X}}}_{\mathbf{s}} + \left[ \, \mathbf{M_{EA}} \, \right] \, \boldsymbol{\mathcal{F}} \, (\overline{\mathbf{A}})$$

When the following assumptions are applied

- a. µ is a known constant
- b.  $\delta \ddot{\overline{X}}_{g} = 0$ , the nominal trajectory reference
- c.  $0M_{EA} f(\overline{A}) = 0$ , products of small perturbations are zero (see Section 2.3.3.2 for  $f(\overline{A})$ )

the linearized equation becomes

$$\delta \ddot{\overline{\mathbf{X}}} = -\frac{\mu}{R^3} \delta \overline{\mathbf{X}} + \frac{3\mu}{R^4} \overline{\mathbf{X}} \delta \mathbf{R} + \{\mathbf{M_{EA}} \delta \mathbf{M_{AE2}} + \delta \mathbf{M_{EA1}} \mathbf{M_{AE}} \} \ddot{\overline{\mathbf{X}}}_{\mathbf{S}} + \mathbf{M_{EA}} \delta \mathbf{f} (\overline{\mathbf{A}})$$

The following terms in the above expression are expanded as

a. 
$$R = \sqrt{x^2 + y^2 + z^2}$$

$$\therefore \quad \delta_R = x^T \delta \overline{x}/R$$

b. 
$$\delta M_{AE2} = \delta [M_{AP}M_{PE}]_2 = \delta M_{AP}M_{PE} + M_{AP}\delta M_{PE}$$

Since  $\delta M_{AP}$  is in error due to a misalignment of the accelerometer true input axis from the one calibrated, it is treated as an accelerometer error source. Consequently,  $\delta M_{AP} = 0$  for these equations. The matrix  $\delta M_{PE}$  results from platform angular misalignments. Therefore

$$\delta M_{AE2} = M_{AP} [\delta M_{PE}]_{P} = M_{AP} [\Phi_{P}] M_{PE}$$

where

[\$\Phi\_p\$] = the skew symmetric matrix made up of platform angular errors expressed in platform coordinates

c. 
$$\delta M_{EA1} = \delta [M_{EP}M_{PA}]_1 = \delta M_{EP}M_{PA} + M_{EP}\delta M_{PA}$$

Since MpA is calculated from MAP, there is no error in MpA, that is,  $\delta MpA = 0$ . Here  $\delta MEP$  results from computer errors. Therefore

$$\delta M_{EA1} = [\delta M_{EP}]_P M_{PA} = -M_{EP} [\Theta_P] M_{PA}$$

where

[ P ] = the skew symmetric matrix made up of computer errors expressed in platform coordinates.

By using these relationships, the equation reduces to

$$\begin{split} \delta \ddot{\overline{X}} &= \frac{\mu}{R^3} \left[ \frac{3\overline{X}\overline{X}^T}{R^2} - I \right] \delta \overline{X} + \left\{ M_{\mathbf{E}\mathbf{A}} M_{\mathbf{A}\mathbf{P}} [\Phi_{\mathbf{P}}] M_{\mathbf{P}\mathbf{E}} \right. \\ &\quad \left. - M_{\mathbf{E}\mathbf{P}} [\Theta_{\mathbf{P}}] M_{\mathbf{P}\mathbf{A}} M_{\mathbf{A}\mathbf{E}} \right\} \ddot{\overline{X}}_{\mathbf{s}} + M_{\mathbf{E}\mathbf{A}} \delta \mathbf{f}(\overline{\mathbf{A}}) \\ &= M_{\mathbf{G}} \delta \overline{X} + M_{\mathbf{E}\mathbf{P}} \{\Phi_{\mathbf{P}} - \Theta_{\mathbf{P}}\} M_{\mathbf{P}\mathbf{E}} \ddot{\overline{X}}_{\mathbf{s}} + M_{\mathbf{E}\mathbf{A}} \delta \mathbf{f}(\overline{\mathbf{A}}) \end{split}$$

where

$$M_{G} = \frac{\mu}{R^{3}} \left[ \frac{3XX^{T}}{R^{2}} - 1 \right]$$

$$= \frac{\mu}{R^{3}} \left[ \frac{3X^{2}}{R^{2}} - 1 - \frac{3XY}{R^{2}} - \frac{3XZ}{R^{2}} - \frac{3YZ}{R^{2}} \right]$$
(Symmetric) 
$$\frac{3Z^{2}}{R^{2}} - 1$$

Using the properties discussed above, these equations are further reduced to

$$\delta \ddot{\mathbf{X}} = \mathbf{M}_{\mathbf{G}} \delta \ddot{\mathbf{X}} + \mathbf{M}_{\mathbf{A}} \ \overline{\mathbf{\Psi}} + \mathbf{M}_{\mathbf{E}\mathbf{A}} \delta \mathbf{f} \ (\overline{\mathbf{A}})$$

where

$$\mathbf{M}_{\mathbf{A}} = \begin{bmatrix} 0 & -\mathbf{Z}_{\mathbf{s}} & \mathbf{Y}_{\mathbf{s}} \\ \mathbf{Z}_{\mathbf{s}} & 0 & -\mathbf{X}_{\mathbf{s}} \\ \mathbf{Z}_{\mathbf{s}} & \mathbf{X}_{\mathbf{s}} & 0 \end{bmatrix}$$

$$\ddot{X}_s$$
,  $\ddot{Y}_s$ ,  $\ddot{Z}_s$  = components of  $\ddot{X}_s$ 

 $\overline{\psi} = \overline{Q} - \overline{\theta}$  = vector expressed in ECI coordinates, which is the difference between computer axes and platform axes,\* due to the various error sources (see Section 2.3.3)

This notation is the same as the one given in Reference 2, p 161.

θ = the vector expressed in ECI coordinates of computer errors

 $\delta f(\bar{A})$  = the vector expressed in accelerometer coordinates of the accelerometer errors.

These then constitute the basic differential equations (variational equations) for computing navigation error sensitivities, as a function of the navigation system error sources. These equations are put into a pseudo-state vector matrix form as

$\dot{x}_1$			1	, ,	× <sub>1</sub>		[ ]
×2		0	I	0	<b>x</b> <sub>2</sub>		0
×3					<b>x</b> <sub>3</sub>		
×4					× <sub>4</sub>		i
× <sub>5</sub>	=	<sup>M</sup> G	0	M <sub>A</sub>	<b>x</b> <sub>5</sub>	+	FA
×6					*6		
× <sub>7</sub>					* <sub>7</sub>		
× <sub>8</sub>		0	0	0	× <sub>8</sub>		Fψ
× <sub>9</sub>					<b>*</b> 9		

$$\frac{\dot{x}}{\dot{x}_i} = M_{x} \dot{x}_i + \bar{F}_i$$

where

 $x_1 x_2 x_3$  are XYZ position partials due to i<sup>th</sup> error source  $x_4 x_5 x_6$  are  $\dot{X}\dot{Y}\dot{Z}$  velocity partials due to i<sup>th</sup> error source  $x_7 x_8 x_9$  are  $\psi_x, \psi_y, \psi_z$  orientation partials due to i<sup>th</sup> error source (also see Section 2.3.3)

$$\mathbf{F}_{\mathbf{A}} = \mathbf{M}_{\mathbf{E}\mathbf{A}} \frac{\partial f(\mathbf{A})}{\partial \epsilon_{\mathbf{i}}}$$
 is the forcing function of accelerometer errors due to ith error source

$$F_{\psi} = \frac{\partial \hat{\psi}}{\partial \epsilon_i}$$
 is the forcing function of orientation rate errors due to ith error source

is the state vector representing the navigation error sensitivity due to ith error source.

### 2.3.3 Error Sources

The error sources of the unaided inertial guidance system fall into the general categories of initial conditions, accelerometer, gyro, and platform errors.

In addition, terminal errors are included to be able to account for guidance and control errors.

The general notation used for the identification of error sources is a seven-character symbol. Not all are explicitly used when it is convenient to drop certain characters without loss of generality, or when an error source is explicitly defined otherwise. Each character is defined in Table 1.

Table G-1 (in Appendix G) gives the symbol, description, and units for each error-source type presently considered. Additions to this list are easily accommodated when a certain component does not fit the model error considered here. For purposes of describing error-source models, the phase index is dropped and the error source is represented as a unit vector to derive sensitivities, that is

$$\mathbf{EKlm}; \quad \mathbf{EKl1} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad , \quad \mathbf{EKl2} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \quad , \quad \mathbf{EKl3} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

NOTE: One of the l indices is dropped for initial- and terminal-type error sources, since l = 3 for these categories.

Table 1. General Notation Used for Identification of Error Sources

Character	Symbol E	Description  Identifies it as an error source symbol
2	K	Categorical index where K equals:
Ľ	K	I - initial condition error P - platform error G - gyro error A - accelerometer error T - terminal condition error
3 and 4	ı	Numerical ordering of the error-source types within each category $l = 00, 01, 02, \dots, 99$
5	m	Identifies a component or axis number m = 1, 2, or 3
6 and 7	n	Phase index used to identify at what time the error source was activated (see Section 2.3.4) n = 01, 12
		(For Example, EA102-11 identifies the No.2 accelerometer Type 10 error-source active during the 11th phase of the error analysis.)

# 2.3.3.1 Initial Condition Errors

As indicated in Section 2.3.1, there are two options for specifying the initial position and velocity errors. For Option 1, the errors cannot be explicitly defined but generally would be the same as for Option 2 (with a change in azimuth direction). In the definitions for initial-condition errors given in Table G-1, it is assumed that Option 2 is being used and that the platform is aligned with respect to vertical. In a launch from an earth site ( $t_0 \le 0$ ), any uncertainty of the launch location will result in initial-condition errors of position and velocity, and in the transformation matrix  $M_{\rm EP}$  of the computer. These are obtained as follows.

### 2.3.3.1.1 Initial Position Errors

The position error sensitivities transform into ECI coordinates as

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = M_{EI} \begin{bmatrix} EI1m \end{bmatrix} \qquad (m = 1, 2, 3)$$

Initial velocity for navigation is computed, where  $t_0 \le 0$ , as follows

$$\nabla_{o} = \overline{\omega} \times \overline{X}_{o} = (\omega_{e} \overline{Z}_{u}) \times (X_{c} \overline{X}_{u} + Y_{o} \overline{Y}_{u} + Z_{o} \overline{Z}_{u})$$
$$= -\omega_{e} Y_{o} \overline{X}_{u} + \omega_{e} X_{o} \overline{Y}_{u} = \dot{X}_{o} \overline{X}_{u} + \dot{Y}_{o} \overline{Y}_{u}$$

where

$$\bar{X}_u$$
,  $\bar{Y}_u$ ,  $\bar{Z}_u$  = ECI unit vectors
$$\omega_e = \text{earth rotation rate}$$

Therefore, initial position errors result in the velocity errors

$$\dot{\delta X}_{o} = -\omega_{e} \delta Y_{o} = -\omega_{e} x_{2} = x_{4}$$

$$\dot{\delta Y}_{o} = \omega_{e} \delta X_{o} = \omega_{e} x_{1} = x_{5}$$

or

$$\begin{bmatrix} \mathbf{x_4} \\ \mathbf{x_5} \\ \mathbf{x_6} \end{bmatrix} = \mathbf{\omega}_{\mathbf{e}} \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \mathbf{M}_{\mathbf{EI}} \begin{bmatrix} \mathbf{EIIm} \end{bmatrix} \qquad (\mathbf{t_0} \le 0)$$

The transformation matrix used by the computer is developed from the initial position data, therefore errors in position result in errors in  $M_{EP}$  ( $M_{EP}$  =  $M_{PE}$  see Section 2.3.1). A downrange error results in a negative rotation about the 2-axis of  $M_{PE}$  and a cross-range error in a positive rotation about the 3-axis. There is no error due to altitude errors. The angular errors are proportional to  $1/R_{O}$ ; therefore, the computer error in launch coordinates is

$$\overline{\theta} = \begin{bmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \end{bmatrix} = \frac{1}{R_o} \begin{bmatrix} 0 \\ -EI13 \\ EI12 \end{bmatrix}.$$

This is transformed into the ECI coordinates

$$\begin{bmatrix} \mathbf{x}_{-} \\ \mathbf{x}_{0} \end{bmatrix} = \overline{\Psi} = -\mathbf{M}_{EI} \overline{\theta} = \frac{1}{R_{0}} \mathbf{M}_{EI} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} EIIm \end{bmatrix} \qquad (t_{0} \le 0)$$

When  $t_0 > 0$ , there is no explicit coupling introduced into velocity and orientation elements of the state vector for position errors and the elements  $x_4 cdots x_9 = 0$ .

# 2.3.3.1.2 Initial Velocity Errors

Initial velocity errors are transformed directly into ECI coordinates as

$$\begin{bmatrix} x_4 \\ x_5 \\ x_6 \end{bmatrix} = M_{EI} \begin{bmatrix} EI2m \end{bmatrix} \qquad (m = 1, 2, 3)$$

$$x_1x_2x_3x_7x_8x_9 = 0$$

# 2.3.3.1.3 Initial Platform-Orientation Errors

The platform errors  $(\emptyset)$  are initial rotations about the platform axes and are transformed into ECI coordinates as

$$\begin{bmatrix} x_7 \\ x_8 \\ x_9 \end{bmatrix} = \overline{\Psi} = M_{EP} \overrightarrow{D} = M_{EP} \begin{bmatrix} Ei3m \end{bmatrix} \qquad (m = 1, 2, 3)$$

$$\mathbf{x}_1 \cdot \ldots \cdot \mathbf{x}_6 = 0$$

### 2.3.3.2 Accelerometer Error Sources

In the design and manufacture of accelerometer components, every attempt is made to achieve an output that is a function only of input acceleration along one of its axes. Unfortunately, this is never achievable due to inherent design characteristics and manufacturing tolerances. The general equation

<sup>\*</sup>See Reference 2 for a discussion of design characteristics, etc.

for an accelerometer's output at a given time can be written as

$$A_{0} = K_{0} + K_{1}A_{1} + K_{2}A_{1}^{2} + K_{3}A_{1}^{3} + K_{4}A_{2} + K_{5}A_{3} + K_{6}A_{1}A_{2} + K_{7}A_{1}A_{3}$$

$$+ K_{8}(A_{2}^{2} + A_{3}^{2})^{1/2} + K_{9}A_{1}(A_{2}^{2} + A_{3}^{2})^{1/2} + K_{10}A_{2}^{2} + K_{11}A_{3}^{2}$$

$$+ K_{12}A_{2}A_{3} + R$$

where

A<sub>1</sub> = the sensed acceleration along the defined (theoretical) input axis

 $A_2 A_3$  = sensed accelerations normal to  $A_1$ 

K<sub>1</sub> = coefficients that may be functions of time and are the result of design characteristics, manufacturing tolerances, or environmental effects (vibration, temperature, etc.)

R = a remainder term, which includes all higher-order terms assumed to be sufficiently small to neglect.

One notable remainder term, not treated here, is a dynamic response to acceleration transients. Of course, any one component design does not have all the terms presented above; and only those that are significant are included in a given error analysis. The purpose of component calibrations is to measure these coefficients and thereby compensate for their effects. It is assumed that the compensation is achieved by the following corrections to the accelerometer output

$$A_{oc} = A_o - (K_{oc} + K_{2c}A_o^2 + ... + K_{5c}A_{o3} + ... K_{12c}A_{o2}A_{o3})$$

<sup>\*</sup>Compensations could also be achieved by biasing the target conditions in the guidance equations, etc.

where

 $\frac{A}{oc} = \frac{\text{the corrected output of an accelerometer, where all constants}}{\text{and accelerometer outputs have been scaled, based on the calibrated scale factor } K_{1c} \text{ of each accelerometer}$ 

Kic = the correction coefficients derived from instrument calibration or based on inherent design characteristics. (Not all are determinable from the above methods.)

A = (i = 2, 3) = the accelerations normal to the accelerometer's input axis, derived from the outputs of all three accelerometers as follows

$$\overline{A}_{02} = M_{A2}\overline{A}_{0}$$

$$\overline{A}_{o3} = M_{A5}\overline{A}_{o}$$

where

 $\overline{A}_0$  = the vector of acceleremeter outputs

A = a vector composed of the acceleration components along the 2-axis of each acceler ometer

 $\overline{A}_{03}$  = a vector composed the acceleration components along the 3-axis of each accommeter

 ${
m M}_{
m A2}$  and  ${
m M}_{
m A3}$  are defined in Section 2.3.1. Since the  ${
m K}_{
m 1c}$  coefficients are sufficiently small with respect to  ${
m K}_{
m 1c}$  (which implies linear design), their products are negligible and the equation reduces to

$$A_{oc} = (K_0 - K_{0c}) + K_1 A_1 + (K_2 - K_{2c}) A_1^2 + \dots (K_{12} - K_{12c}) A_2 A_3$$

Taking the partial derivatives of this equation results in

$$\delta A_{oc} = \delta K_0 + \delta K_1 A_1 + \delta K_2 A_1^2 + \dots \delta K_{12} A_2 A_3$$

where  $\delta A_i = 0$  (nominal trajectory).

Combining the equations of each accelerometer and placing them into the sensitivity form, the final vector matrix form is

$$\delta f(\overline{A}) = \delta \overline{A}_{oc} = [I] \{EA00m\} + \begin{bmatrix} A_{A11} & 0 & 0 \\ 0 & A_{A21} & 0 \\ 0 & 0 & A_{A31} \end{bmatrix} \{EA01m\}$$

$$+ \dots + \begin{bmatrix} A_{A12}A_{A13} & 0 & 0 \\ 0 & A_{A22}A_{A23} & 0 \\ 0 & 0 & A_{A32}A_{A33} \end{bmatrix} \{EA12m\}$$

$$m = (1, 2, 3)$$

where

$$\overline{A}_{A1} = \begin{bmatrix} A_{A11} \\ A_{A21} \\ A_{A31} \end{bmatrix} = M_{AE} \overline{X}_{s}$$

acceleration components along input axes

$$\begin{bmatrix} A_{A12} \\ A_{A22} \\ A_{A32} \end{bmatrix} = M_{A2} \overline{A}_{A1}$$

acceleration components along 2-axis

$$\begin{bmatrix} A_{A13} \\ A_{A23} \\ A_{A33} \end{bmatrix} = M_{A3} \overline{A}_{A1}$$

acceleration components along 3-axis

# 2.3.3.3 Gyro Erro. Sources

For the purpose of describing the error-source model for gyro components, it is convenient to discuss the model in terms of a single-degree-of-freedom integrating gyro. The general equation for gyro rates can be written

$$\dot{\emptyset} = C_0 + C_1 A_1 + C_2 A_3 + C_3 A_1 A_3 + C_4 \omega_3 + C_5 \omega_2 + C_6 \omega_1 + C_7 A_2 A_3$$
$$+ C_8 A_2 + C_9 A_1^2 + C_{10} A_3^2 + C_{11} A_1 A_2 + R$$

where

A<sub>1</sub> A<sub>2</sub> A<sub>3</sub> = sensed accelerations along the input, output, and spin reference axes

 $\omega_1$   $\omega_2$   $\omega_3$  = rates about the input, output, and spin reference exes

coefficients, which may be functions of time and and the
result of design characteristics, manufacturing tolerances,
or environmental effects (vibration, temperature, etc.)

R = a remainder term, which includes all higher-order terms assumed to be sufficiently small to neglect.

One notable term is dynamic response to transient inputs. It is assumed that the platform and/or gyro servo loops are designed with sufficient bandpass and static gain to make the effects of transients or sustained rotational dynamic inputs negligible.

As in the case of accelerometers, not all coefficients are applicable to a given design; only those indicative of the particular components are considered in any one analysis. Also, component calibration measures some of these coefficients and the compensation for their effects is assumed to be included in the navigation system equations. The compensation method assumed is the calculation of compensating torquing signals to the gyros. Thus, the compensated gyro rate equation is

$$\dot{\phi}_{c} = \dot{\phi} - (C_{0c} + C_{1c}A_{o1} + \dots + C_{4c}\omega_{o3} + \dots + C_{11c}A_{o1}A_{o2})$$

where

$$\overline{A}_{o1} = M_{GP}M_{PA}\overline{A}_{o}$$
 = acceleration along gyro input axes
 $\overline{A}_{o2} = M_{G2}\overline{A}_{o1}$  = acceleration along gyro 2-axes
 $\overline{A}_{o3} = M_{G3}\overline{A}_{o1}$  = acceleration along gyro 3-axes
 $\overline{\omega}_{o1} = M_{GP}\overline{\omega}_{oP}$  = rates about gyro input axes
 $\overline{\omega}_{o2} = M_{G2}\overline{\omega}_{o1}$  = rates about gyro 2-axes
 $\overline{\omega}_{o3} = M_{G3}\overline{\omega}_{o1}$  = rates about gyro 3-axes

 $\overline{A}_{o}$  is as defined in Section 2.3.3.2  $\overline{\omega}_{oP}$  = measured or computed vector rates of platform axes  $M_{Ci}$  is as defined in Section 2.3.1

<sup>&</sup>quot;Use of the compensation of the transformation matrix is more generally in practice, which is equivalent.

By following the same approach as for the accelerometers, the final equations for gyro error sensitivities in vector matrix form become

$$\dot{\bar{\mathbf{T}}} = \bar{\mathbf{F}}_{\psi} = \mathbf{M}_{\mathbf{EG}} \dot{\bar{\mathbf{D}}}_{\mathbf{c}}$$

where

$$\dot{\mathcal{D}}_{c} = [I] \{EG00m\} + \begin{bmatrix} A_{G11} & 0 & 0 \\ 0 & A_{G21} & 0 \\ 0 & 0 & A_{G31} \end{bmatrix} \{EG01m\}$$

$$+ \dots \begin{bmatrix} \omega_{11} & 0 & 0 \\ 0 & \omega_{21} & 0 \\ 0 & 0 & \omega_{31} \end{bmatrix} \{ \text{EG 06 m} \}$$

$$+ \dots + \begin{bmatrix} A_{G11}A_{G12} & 0 & 0 \\ 0 & A_{G11}A_{G22} & 0 \\ 0 & 0 & A_{G31}A_{G32} \end{bmatrix} \{EG11m\}$$

$$(m = 1, 2, 3)$$

where

$$\overline{A}_{G1} = \begin{bmatrix} A_{G11} \\ A_{G21} \\ A_{G31} \end{bmatrix} = M_{GE} \overline{X}_{s}$$

acceleration components along gyro input axes

$$\begin{bmatrix} A_{G12} \\ A_{G22} \\ A_{G32} \end{bmatrix} = M_{G2} \overline{A}_{G1}$$

acceleration components along gyro 2-axis

$$\begin{bmatrix} A_{G13} \\ A_{G23} \\ A_{G33} \end{bmatrix} = M_{G3} \overline{A}_{G1}$$

acceleration components along gyro 3-axis

$$\overline{\omega}_{1} = \begin{bmatrix} \omega_{11} \\ \omega_{21} \\ \omega_{31} \end{bmatrix} = M_{GP} \begin{bmatrix} \omega_{1} \\ \omega_{2} \\ \omega_{3} \end{bmatrix}$$

rates about gyro input axes

$$\begin{bmatrix} \omega_{12} \\ \omega_{22} \\ \omega_{32} \end{bmatrix} = M_{G2} \overline{\omega}_{1}$$

rate components about gyro 2-axis

$$\begin{bmatrix} \omega_{13} \\ \omega_{23} \\ \omega_{33} \end{bmatrix} = M_{G3} \overline{\omega}_{1}$$

rate components about gyro 3-axis

### 2.3.3.4 Platform Errors

In addition to the initial condition errors discussed in Section 2.3.3.1, acceleration-sensitive errors arise due to the structural deformation of the gimbals under acceleration loads, and to static servo response due to platform mass unbalances. The general equation for platform acceleration-sensitive errors can be written in the vector matrix form

$$\vec{\phi}_{\mathbf{p}} = \begin{bmatrix} \phi_{1} \\ \phi_{2} \\ \phi_{3} \end{bmatrix} = \begin{bmatrix} A_{\mathbf{p}2} & 0 \\ 0 & A_{\mathbf{p}3} \\ 0 & A_{\mathbf{p}1} \end{bmatrix} \{ \mathbf{EP01m} \} + \begin{bmatrix} A_{\mathbf{p}3} & 0 \\ 0 & A_{\mathbf{p}1} \\ 0 & A_{\mathbf{p}2} \end{bmatrix} \{ \mathbf{EP02m} \}$$

$$\begin{bmatrix}
A_{P2}^{A}_{P3} & 0 \\
A_{P1}^{A}_{P3} & \\
0 & A_{P1}^{E}_{P2}
\end{bmatrix}$$
(EP03m) (m = 1, 2, 3)

$$\overline{\psi} = \begin{bmatrix} x_7 \\ x_8 \\ x_9 \end{bmatrix} = M_{EP} \overline{\phi}_P \qquad (\overline{F}_{\psi} = 0)$$

where

$$\vec{A}_{p} = \begin{bmatrix} A_{p1} \\ A_{p2} \end{bmatrix} = M_{pE} \ddot{\vec{x}}_{s}$$
 acceleration remponents along platform was

### 2.3.3.5 Terminal Condition Errors

The terminal condition errors transform into the following ECI coordinates by utilizing the transformation matrices developed in Section 2.3.1.

### Position Errors

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = M_{ET1} \{ET_1 m\} \quad (m = 1, 2, 3)$$

$$x_4 \dots x_9 = 0$$

### Velocity Errors

$$\begin{bmatrix} x_4 \\ x_5 \\ x_6 \end{bmatrix} = M_{ET2} \{ET2m\} \quad (m = 1, 2, 3)$$
$$x_1 x_2 x_3 x_7 x_8 x_9 = 0$$

### 2.3.4 Transition Matrix

Since the majority of error sources are acceleration-sensitive, their forcing functions (excluding accelerometer bias and gyro bias drift) are zero during free-flight sequences; therefore, it is more efficient computationally to propagate the sensitivity vectors across free flight, by using the transition matrix rather than by solving each error-source sensitivity independently. Additionally, when an error-source type has time-dependent statistical characteristics, it becomes both convenient and efficient to subdivide the total trajectory time into phases and treat each error source of this type as an independent error source reinitialized  $(\overline{\mathbf{x}}_i(t) = 0)$  at each phase time. Error source types that were active during previous phases are called inactive vectors, while errors sources that are active during the present

phase are termed active vectors. For any one type of error source, all its inactive vectors are updated to the present time by using the transition matrix(es) and combined statistically (see Section 2.4.3) to derive the total effect on the navigation data statistical characteristics. Thus, the following procedure is used to update or propagate vector sensitivities

$$\overline{x}_{i}(t) = \Phi(t, \tau)\overline{x}_{i}(\tau)$$

where  $\Phi$  (t,  $\tau$ ) is the transition matrix obtained from the solution of the homogeneous differential equations

$$\Phi(t, \tau) = M(t)\Phi(t, \tau), \qquad \Phi(\tau, \tau) = I$$

where

$$M(t) = \begin{bmatrix} 0 & I & 0 \\ M_{G}(t) & 0 & M_{A}(t) \\ 0 & 0 & 0 \end{bmatrix}$$

 $M_{C}$  and  $M_{A}$  are defined in Section 2.3.2.

The solution of this equation is achieved by solving the homogeneous differential equations (in ECI coordinates) for each initial condition. Since during free flight  $M_A(t) = 0$ , the solution requires only six independent solutions; during powered flight nine independent solutions are required. In addition, the following property of the transition matrix(es) is used

$$\Phi(t_i t_k) = \Phi(t_i t_j) \Phi(t_j t_k)$$
  $t_i \ge t_j \ge t_k$ 

# 2.3.5 Trajectory Data and Free-flight Equations of Motion

C

To make an error analysis, the following data is required for the differential equations and the error-source equations:

t	time
XYZ	nominal position components in ECI coordinate system
хуż	nominal velocity components in ECI coordinates
X X X S	nominal sensed acceleration components in ECI
ω <sub>1</sub> ω <sub>2</sub> ω <sub>3</sub>	nominal platform (body) rates in platform (body) coordinates
M <sub>PE</sub> (t)	direction cosines of platform (body) axes with respect to ECI axes

This data is generated by a trajectory program for a particular vahicle configuration and mission requirement and is written on a magnetic tape, which constitutes a basic input for the error analysis. The last two categories ( $\omega_{\rm Pi}$  and  $M_{\rm PE}$ ) are required only for analyzing a strapped-down configuration. For a torqued-platform configuration, the rates ( $\omega_{\rm i}$ ) are input as a table of rates vs time and  $M_{\rm PE}$ (t) is calculated from

$$\dot{M}_{PE} = [\Omega_{P}] M_{PE}$$

where these matrices are as defined in Sections 2.3.1 and 2.3.2.

When error propagation must be evaluated beyond the time for which there is data from the trajectory tape, the program has the capability to generate the required data  $[M_G = f(X \mid Y \mid Zt)]$  for calculating the transition matrix and

drag error sensitivity. The data is generated from the free-flight equations of motion, based on a simplified oblate earth model (see Reference 5), as follows

$$\begin{bmatrix} \ddot{X} \\ \ddot{Y} \\ \ddot{z} \end{bmatrix} = \epsilon_1 \frac{X}{R^3}$$
$$\epsilon_2 \frac{Z}{R^3}$$

where

$$\epsilon_{1} = -\frac{GM}{R^{2}} \left[ R^{2} + JA^{2} \left( 1 - \frac{5Z^{2}}{R^{2}} \right) - \frac{HA^{3}Z}{R^{2}} \left( -3 + \frac{7Z^{2}}{R^{2}} \right) + \frac{DA^{4}}{R^{2}} \left( \frac{9Z^{4}}{R^{4}} - \frac{6Z^{2}}{R^{2}} + \frac{3}{7} \right) \right]$$

$$\epsilon_{2} = -\frac{GM}{R^{2}} \left[ 2JA^{2} - \frac{HA^{3}}{R^{2}} Z \left( -3 + \frac{3R^{2}}{5Z^{2}} \right) - \frac{DA^{4}}{R^{2}} \left( \frac{4Z^{2}}{R^{2}} - \frac{12}{7} \right) \right] + \epsilon_{1}$$

where GM, J, A, H, and D are nominal constants, defined in Table G-2 (in Appendix G).

The initial conditions for these equations are obtained from the trajectory tape at termination of the tape data, or they can be input. The three criteria for terminating the equations of motion are

a. Specified time  $(t_{\overline{T}})$ 

An option is available to terminate (abort) the trajectory tape data at a time prior to the end of the tape.

b. Specified range angle  $(\theta_T)$  from termination of the trajectory tape data, i.e., when  $\theta = \theta_T$  where

$$\theta = \cos^{-1} \frac{X_T X + Y_T Y + Z_T Z}{R_T R}$$

 $X_T^{Y}_{T}^{Z}_{T}$  and  $R_T^{}$  are the values at the tape termination time

Note:  $0 < \theta_{\rm T} < \pi$ 

c. Specified altitude  $h_T$ . There are two criteria for this termination: The trajectory can be terminated when  $h = h_T$  and the slope (h) is positive, or when the slope is negative.

### 2.4 DATA PROCESSING EQUATIONS

### 2.4.1 Basic Coordinate Systems

For the purpose of output data presentation, two coordinate systems are available: the ECI coordinate system and the LH (Local Horizontal) system. The latter is sometimes referred to as the orbit plane, and/or the Radial/Tangential/Normal (RTN) coordinate system. The transformation between ECI coordinates and local coordinates is developed from the nominal trajectory position and velocity vectors. In local coordinates, X is defined as down range, i.e., as directed along the projection of the inertial velocity vector onto the plane normal to the geocentric radius vector; Y is vertical; and Z is cross range, forming a right-hand coordinate system. The local coordinate system is an inertial system at time t, defined by the nominal conditions only, and is used in the transformation of position, velocity, and orientation sensitivity vectors as well as those of transition matrices and covariance matrices. The matrix is defined as

$$M_{\text{LE}} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\psi & -S\psi \\ 0 & S\psi & C\psi \end{bmatrix} \begin{bmatrix} C\lambda & 0 & S\lambda \\ 0 & 1 & 0 \\ -S\lambda & 0 & C\lambda \end{bmatrix} \begin{bmatrix} C\emptyset & S\emptyset & 0 \\ -S\emptyset & C\emptyset & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$M_{EL} = M_{LE}^{T}$$

where

$$S\phi = \frac{Y}{D}$$
  $S\lambda = \frac{Z}{R}$   $S\psi = \frac{V_E}{V_H}$ 

$$C \not O = \frac{X}{D}$$
  $C \lambda = \frac{D}{R}$   $C \psi = \frac{V_N}{VH}$ 

$$D = \sqrt{x^2 + y^2}$$
  $R = \sqrt{D^2 + Z^2}$ 

$$V_{E} = \frac{-Y\dot{X} + X\dot{Y}}{D} \qquad V_{N} = \frac{-Z(X\dot{X} + Y\dot{Y}) + \dot{Z}D^{2}}{RD}$$

$$V_{H} = \sqrt{V_{E}^{2} + V_{N}^{2}}$$

and  $X Y Z \dot{X} \dot{Y} \dot{Z}$  are ECI components of the nominal position and velocity vectors at time t.

NOTE:  $\lambda$ ,  $\psi$  are left-hand rotations.

It is also convenient to form the matrix M<sub>LE</sub> as

$$\underline{\mathbf{M_{LE}}} = \begin{bmatrix} \mathbf{M_{LE}} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{M_{LE}} & \mathbf{0} \\ \mathbf{0} & \mathbf{0} & \mathbf{M_{LE}} \end{bmatrix}$$

$$\frac{M_{EL}}{M_{EE}} = \frac{M_{LE}^{T}}{M_{EE}}$$

## 2.4.2 Vector Errors

Vector errors are derived by scaling the sensitivity vectors by an appropriate constant. The constant used in this operation is given the symbol  $\sigma_i$ . (i ranges from 1 to n, which is the total number of error sources, i.e., all active and inactive vectors. See Section 2.3.4.) The units of  $\sigma_i$  for each type of error source are given in Table G-1. Table G-3 gives the conversion factors  $K_i$  used by the program for scaling  $\sigma_i$  into the units of the sensitivity vectors. The operation, therefore, is

$$\Delta \mathbf{X}_{i} = \sigma_{i} \mathbf{K}_{i} \mathbf{\bar{x}}_{i} \triangleq \sigma_{i} \mathbf{\bar{x}}_{i}$$

where the last expression is used throughout, implying the first.

 $\Delta \bar{X}_i$  is the error vector in ECI coordinates. The usual implication of  $\sigma$  is that it represents the standard deviation of the particular error source. However, it could also represent the mean value of an error source or be a constant that produces sensitivity vector output in any desired units. When it is desired to output the vector in local horizontal coordinates, the following transformation is made

$$\Delta \overline{X}_{i} \mid_{LH} = M_{LE} \overline{\Delta X}_{i}$$

# 2.4.3 Covariance Matrix

The basic equation for navigation error is

$$\Delta \mathbf{X} = \sum_{i=1}^{n} \overline{\mathbf{x}}_{i} \epsilon_{i}$$

In this equation,  $\epsilon_i$  is the magnitude of the i<sup>th</sup> error source. Each error source is considered a random variable, the means, variances, and correlations of which are assumed to be known. The accuracy of any navigation system performance is measured in terms of the probability that  $\overline{\Delta X}$  (or some function of  $\Delta \overline{X}$  - see Section 2.4.5) is within certain specified values. To maximize this probability, it is necessary to compensate for the effects of the means of the error sources. This can be done by the methods discussed in Section 2.3.3, or by offsetting the guidance constants so that the effects are negated at some specified time point. For the latter method, the  $\sigma$  can be input to represent the mean value of each error source and the resulting vectors summed, that is

$$E(\Delta \overline{X}) = \sum_{i=1}^{n} \overline{x}_{i} E(\epsilon_{i})$$

where

$$E(\epsilon_i) = \sigma_i$$
 representing  $E(\epsilon_i)$ 

E = the expectation operator

This calculation is not made in the program, although the magnitude of the mean (expected) value of the navigation vector can be obtained from the covariance matrix output described below, if each error source is correlated with the other by unity. Alternately, the error vectors can be summed by utilizing desk calculators. When it is assumed that the mean values have been compensated, the second statistical moments of navigation data are determined in foovariance) matrix form by

$$\mathbb{E}(\Delta \mathbb{X} \Delta \mathbb{X}^{\mathsf{T}}) = \mathbb{E}(\bar{\mathbf{x}}_{1} \epsilon_{1} + \bar{\mathbf{x}}_{2} \epsilon_{2} + \cdots)(\bar{\mathbf{x}}_{1}^{\mathsf{T}} \epsilon_{1} + \bar{\mathbf{x}}_{2}^{\mathsf{T}} \epsilon_{2} + \cdots)$$

$$\sum_{ECI}^{\dagger} = \sum_{i=1}^{n} \sum_{j=1}^{n} \sigma_{i} \sigma_{j} \rho_{ij} \tilde{x}_{i} \tilde{x}_{j}^{T}$$

where

ρ<sub>ij</sub> = the correlation coefficient between the i<sup>th</sup> and j<sup>th</sup> error source. (In this way, both time and cross correlation of error sources are handled.)

ECI = a 9 × 9 matrix in which the diagonal elements represent the variances of the navigation data and the off-diagonal elements are the covariances.

Since this is a symm trical matrix, the correlation coefficients of the navigation data are calculated and presented in the lower half of the matrix. The correlation coefficients are obtained from

$$\rho_{mn} = \frac{\mathbb{E}(\Delta X_{m} \Delta X_{n})}{\sigma_{m} \sigma_{n}} \qquad m \neq n$$

where  $E(\Delta X_m \Delta X_n)$  is the mn<sup>th</sup> elements of the covariance matrix and  $\sigma_m$ ,  $\sigma_n$  are the m and n standard deviations of the m and n coordinates calculated from the square root of the respective diagonal terms. The  $\sigma$ 's of the navigation data are also presented in the output.

When vector errors are presented in LH coordinates, the covariance matrix is also presented in this coordinate system. It is computed by

$$\sum_{LH} = \frac{M_{LE}}{ECI} = \frac{\sum_{ECI} M_{EL}}{ECI}$$

All of the above operations presuppose the condition of linearity, which is usually satisfied, but should not be assumed always to be true. (This is mentioned merely as a precaution about the underlying assumptions of the program.)

## 2.4.4 Transition Matrix and Trajectory Variables

As stated in Section 2.3.4, the transition matrices are used to propagate not only sensitivity vectors across free flight, but inactive vectors for data processing as well. In addition, when free-flight time histories are desired, the transition matrix plays a paramount role. For various analytical studies, it is desired to obtain the transition matrix, and so its output is made available. Like the previous outputs, it is available in either the ECI or LH coordinate systems. Since it is computed in ECI coordinates, the operation required to present it in local coordinates is easily obtained from

$$\Delta \overline{X}_{i}(t) = \Phi(t, \tau) \Delta \overline{X}_{i}(\tau)$$

$$\Delta X_{i}(t) \Big|_{LH} = \frac{M_{LE}(t) \Delta \overline{X}_{i}(t)}{=}$$

$$= M_{LE}(t) \Phi(t, \tau) M_{EL}(\tau) \Delta \overline{X}_{i}(\tau) \Big|_{LH}$$

$$\Phi_{LH}(t, \tau) = M_{LE}(t) \Phi(t, \tau) M_{EL}(\tau)$$

In addition to the transition matrix, it is convenient and sometimes necessary to know the reference trajectory conditions for which the transition matrix is valid. These are presented at both times (t and  $\tau$ ) and in both ECI and local reference coordinates, the latter being defined and computed from ECI coordinates as

LAT (deg) Geocentric latitude  $= \sin^{-1} \frac{Z}{R} - \frac{\pi}{2} \le LAT \le \frac{\pi}{2}$ 

LONG (deg) Longitude measured positively east from Greenwich  $=\tan^{-1}\frac{v}{X}+\cancel{p}_{L}-\omega_{e}t \qquad 0\leq \text{LONG}<2\pi$ 

where  $\phi_L$  is used to reference the ECI coordinates to Greenwich when the trajectory reference is not.

ALT (n mi) Altitude in nautical miles above the surface of an oblate earth

$$=\frac{R-R_e}{6076.1033}$$

where

$$R_e = \frac{A(1-e)}{(1+(e^2-2e)\cos^2\lambda)^{1/2}}$$

See Section 2. 3. 5 for definitions.

VEL (ft/sec) Inertial velocity magnitude

$$=(\dot{x}^2+\dot{y}^2+\dot{z}^2)^{1/2}$$

FPA (deg) Flight path angle, defined as the angle the inertial velocity vector makes with the local geocentric horizontal

$$= \sin^{-1} \frac{x\dot{x} + y\dot{y} + z\dot{z}}{RV} \qquad -\frac{\pi}{2} \le \text{FPA} \le \frac{\pi}{2}$$

AZ (deg) Azimuth of inertial velocity vector measured clockwise

$$= \tan^{-1} \frac{V_E}{V_N} \qquad 0 \le AZ \le 2\pi$$

See Section 2.4.1 for definition of  $V_{\mathbf{F}}$  and  $V_{\mathbf{N}}$ .

#### 2.4.5 Mission Evaluation

This is an optional output of the program and operates on the final or end conditions of a particular error analysis. It is called upon when a specified mission termination criterion is to be evaluated. The parameters necessary to evaluate mission success can occur in a variety of categories, only a few of which are considered here.

#### 2.4.5.1 Fixed Altitude

This criterion is used primarily for re-entry evaluation and presents the coordinates of down-range (MD) and cross-range (MC) miss at a fixed altitude with respect to earth fixed-target coordinates; in addition, the time dispersion (MT) is presented. The orientation of the down-range miss coordinate is along the projection of the relative velocity vector onto the plane normal to the target geocentric radius vector. The method of computing these quantities is

$$\begin{split} \overline{\mathbf{V}}_{\mathbf{R}} &= \overline{\mathbf{V}} - \overline{\mathbf{V}}_{\mathbf{T}} \\ &= (\dot{\mathbf{X}} + \boldsymbol{\omega}_{\mathbf{e}} \mathbf{Y}) \overline{\mathbf{X}}_{\mathbf{u}} + (\dot{\mathbf{Y}} - \boldsymbol{\omega}_{\mathbf{e}} \mathbf{X}) \overline{\mathbf{Y}}_{\mathbf{u}} + \dot{\mathbf{Z}} \overline{\mathbf{Z}}_{\mathbf{u}} \\ &= \dot{\mathbf{X}}_{\mathbf{R}} \overline{\mathbf{X}}_{\mathbf{u}} + \dot{\mathbf{Y}}_{\mathbf{R}} \overline{\mathbf{Y}}_{\mathbf{u}} + \dot{\mathbf{Z}}_{\mathbf{R}} \overline{\mathbf{Z}}_{\mathbf{u}} \end{split}$$

= target velocity in ECI coordinates where:

 $\overline{V}_R$  = relative vers  $\overline{X}_u \overline{Y}_u \overline{Z}_u$  = ECI unit vectors = relative velocity in ECI coordinates

 $\dot{\mathbf{Y}} \dot{\mathbf{Y}} \dot{\mathbf{Z}} \mathbf{X} \mathbf{Y} \mathbf{Z} = components$  of the nominal position and velocity vectors at the target

 $\dot{X}_{R} \dot{Y}_{R} \dot{Z}_{R} = \text{the components of } \overline{V}_{R} \text{ in ECI coordinates}$ 

The relative velocity vector is transformed into the coordinate system at the target by

$$\begin{bmatrix} \dot{x}_{RR} \\ \dot{y}_{RR} \\ \dot{z}_{RR} \end{bmatrix} = M_{RE1} \begin{bmatrix} \dot{x}_{R} \\ \dot{y}_{R} \\ \dot{z}_{R} \end{bmatrix}$$

where

$$\begin{split} \mathbf{M_{RE1}} &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & C\psi & -S\psi \\ \bar{0} & S\psi & C\psi \end{bmatrix} \begin{bmatrix} C\lambda & 0 & S\lambda \\ 0 & 1 & 0 \\ -S\lambda & 0 & C\lambda \end{bmatrix} \begin{bmatrix} C\phi & S\phi & 0 \\ -S\phi & C\phi & 0 \\ 0 & 0 & 1 \end{bmatrix} \\ & S\phi &= \frac{Y}{D} \qquad S\lambda &= \frac{Z}{R} \qquad S\psi &= \frac{V_{RE}}{V_{RH}} \\ & C\phi &= \frac{X}{D} \qquad C\lambda &= \frac{D}{R} \qquad C\psi &= \frac{V_{RN}}{V_{RH}} \\ & D &= \sqrt{X^2 + Y^2} \qquad V_{RE} &= \frac{-Y\dot{X}_R + X\dot{Y}_R}{D} \\ & V_{RN} &= \frac{-Z(\dot{X}_R X + Y\dot{Y}_R) + \dot{Z}_R D^2}{RD} \\ & V_{RH} &= \sqrt{V_{RE}^2 + V_{RN}^2} \end{split}$$

and X Y Z  $\dot{X}_R$   $\dot{Y}_R$   $\dot{Z}_R$  are ECI components of the nominal target coordinates and relative velocity vector at time t.

Thus, the relative velocity components in the target coordinates are:  $\dot{X}_{RR}$  the altitude rate,  $\dot{Y}_{RR}$  the velocity component in the defined cross-range direction (\* zero), and  $\dot{Z}_{RR}$  in the defined down-range direction. When  $\dot{V}_{RE} = \dot{V}_{RN} = 0$ , vertical re-entry,  $\psi$  is undefined. In this case,  $\psi$  is set to zero so that down-range displacements would be directed north and cross-range east.

Based on the above definitions for a coordinate system, a position error vector can be transformed into this coordinate system to determine the altitude, cross-range and down-range dispersions at the nominal time by

$$\begin{bmatrix} \Delta X \\ \Delta Y \\ \Delta Z \end{bmatrix} = M_{REl} \begin{bmatrix} \Delta X \\ \Delta Y \\ \Delta Z \end{bmatrix}$$

where  $\Delta X_T \Delta Y_T \Delta Z_T$  are altitude, cross-range, and down-range dispersions at the nominal time and  $\Delta X \Delta Y \Delta Z$  are ECI dispersions for a given error source.

To derive the first-order dispersions for the condition of zero altitude error  $(\Delta X_T = 0)$ , the following constraint equation is used

$$\Delta X_{T}(t + \Delta t) = 0 = \Delta X_{T}(t) + \dot{X}_{RR}(t)\Delta t$$

from which the time dispersion is calculated as

$$\Delta t = M_T = -\frac{\Delta X_T}{\dot{X}_{RR}}$$

Using this relation, the cross-range and down-range misses at time  $t+\Delta t$  are obtained by

$$\Delta Y_{T}(t + \Delta t) = M_{C} = \Delta Y_{T}(t) + \hat{T}_{RR}(t)\Delta t$$

$$= \Delta Y_{T}$$

$$\Delta Z_{T}(t + \Delta t) = M_{D} = \Delta Z_{T}(t) + \dot{Z}_{RR}(t)\Delta t$$
$$= \Delta Z_{T} - \frac{\dot{Z}_{RR}}{\dot{X}_{RR}} \Delta X_{T}$$

Thus

$$\begin{bmatrix} \mathbf{M}_{\mathrm{T}} \\ \mathbf{M}_{\mathrm{C}} \\ \mathbf{M}_{\mathrm{D}} \end{bmatrix} = \begin{bmatrix} \frac{1}{\mathbf{X}_{\mathrm{RR}}} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \frac{\dot{\mathbf{Z}}_{\mathrm{RR}}}{\mathbf{X}_{\mathrm{RR}}} & \mathbf{0} & \mathbf{1} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{X}_{\mathrm{T}} \\ \Delta \mathbf{Y}_{\mathrm{T}} \\ \Delta \mathbf{Z}_{\mathrm{T}} \end{bmatrix}$$

$$\begin{bmatrix} M_{T} \\ M_{C} \\ M_{D} \end{bmatrix} = M_{TR1} M_{RE1} \begin{bmatrix} \Delta X \\ \Delta Y \\ \Lambda Z \end{bmatrix}$$

The position vector error for each error source is thus transformed into its dispersion parameters at the target. The covariance matrix of these parameters is developed by partitioning the ECI covariance matrix to include

only the position variances and covariances from which the following covariance matrix is determined

$$\sum_{\mathbf{MEI}} = \mathbf{M_{TRI}} \mathbf{M_{REI}} \sum_{\mathbf{EC!}} (\mathbf{M_{TRI}} \mathbf{M_{REI}})^{T}$$

where

mEl = the covariance matrix for mission evaluation Option 1

= the partitioned covariance matrix in ECI coordinates

The nominal trajectory conditions are also listed with this output and include

LAT, LONG, ALT As described in Section 2.2.4

VEL/R (ft/sec) Magnitude of relative velocity rector

$$= \sqrt{\dot{x}_{R}^{2} + \dot{y}_{R}^{2} + \dot{z}_{R}^{2}}$$

FPA/R (deg)

Relative flight path angle, defined as the angle the relative velocity vector makes with the local horizontal

$$= \sin^{-1} \frac{X\dot{X}_R + Y\dot{Y}_R + Z\dot{Z}_R}{RV_P} \qquad -\frac{\pi}{2} \leq FPA/R \leq \frac{\pi}{2}$$

AZ/R (deg)

Azimuth of the relative velocity vector, measured clockwise from north

$$= \tan^{-1} \frac{V_{RE}}{V_{RN}} \qquad 0 \le AZ/R \le 2\pi$$

# 2.4.5.2 Fixed-range Angle

This criterion is similar to the fixed-altitude case, except the relative range coordinate  $(\Delta Z_{\widetilde{T}})$  is fixed and the altitude, cross-range, and time dispersions are determined. The constraint equation is

$$\Delta Z_{T}(t + \Delta t) = 0 = \Delta Z_{T}(t) + \dot{Z}_{RR}(t)\Delta t$$

from which the time, cross-range, and altitude dispersions are

$$\Delta Y_{T}(t + \Delta t) = M_{C} = \Delta Y_{T}$$

$$\Delta X_{T}(t + \Delta t) = M_{C} = \Delta Y_{T}$$

$$\Delta X_{T}(t + \Delta t) = M_{V} = \Delta X_{T}(t) + \dot{X}_{RR}(t)\Delta t$$

$$= \Delta X_{T} - \frac{\dot{X}_{RR}}{\dot{Z}_{RR}} \Delta Z_{T}$$

Thus

$$\begin{bmatrix} \mathbf{M}_{\mathbf{T}} \\ \mathbf{M}_{\mathbf{C}} \\ \mathbf{M}_{\mathbf{V}} \end{bmatrix} = \begin{bmatrix} \mathbf{0} & \mathbf{0} & \frac{1}{\dot{\mathbf{Z}}_{\mathbf{RR}}} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{1} & \mathbf{0} & -\frac{\dot{\mathbf{X}}_{\mathbf{RR}}}{\dot{\mathbf{Z}}_{\mathbf{RR}}} \end{bmatrix} \begin{bmatrix} \Delta \mathbf{X}_{\mathbf{T}} \\ \Delta \mathbf{Y}_{\mathbf{T}} \end{bmatrix} = \mathbf{M}_{\mathbf{TR2}} \mathbf{M}_{\mathbf{RE1}} \begin{bmatrix} \Delta \mathbf{X} \\ \Delta \mathbf{Y} \\ \Delta \mathbf{Z} \end{bmatrix}$$

The vector error outputs and covariance are handled in the same way as in the fixed-altitude case.

## 2.4.5.3 Generalized Linear Transformation

This option is used when linear transformations between ECI position and velocity errors, and some other parameters are known, e.g., the midcourse maneuver velocity sensitivities, as a function of injection errors for a space probe. A matrix is developed from (up to 10) input matrices, and then used to transform injection errors into the desired parameter errors. Each error-source vector is transformed and a covariance matrix is calculated from the partitioned ECI covariance matrix, computed as follows.

The matrix is formed from

$$M = [M_1][M_2] + \cdots [M_n]$$
  $n \le 10$ 

The vector errors are transformed by

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ = [M] & \Delta X \\ \Delta X \\ \Delta X \\ 5 \\ 6 & \Delta X \end{bmatrix}$$

The covariance matrix is calculated as

$$\sum_{M \in 3} = M \sum_{E \subset I} M^{T}$$

## 2.4.6 Platform Reference Attitude

When running a torqued platform or strapped-down case, reference platform orientation is automatically presented as a function of time. Listed in the output are the first two rows of the platform matrix (MpE) and three angles defined and computed as

THETA (θ in deg) Pitch: the angle that the platform 1-axis makes with the local horizontal plane

$$= \sin^{-1}\left(\frac{X(1X)}{R} + \frac{Y(1Y)}{R} + \frac{Z(1Z)}{R}\right) - \frac{\pi}{2} \le \theta \le \frac{\pi}{2}$$

where (1X), (1Y), (1Z) are the elements of the first row of MpE representing the direction cosines of P<sub>1</sub> with respect to the ECI coordinates axes

FSI (ψ in deg)

Heading or Yaw: the angle that the projection of the platform 1-axis onto the horizontal plane makes with north, positive clockwise

$$= \tan^{-1} \frac{1E}{1N} \qquad 0 \le \psi < 2\pi$$

where 
$$1E = \frac{-Y(1X) + Y(1Y)}{D}$$

$$1N = \frac{-Z[X(1X) + Y(1Y)] + D^{2}(1Z)}{RD}$$

PHI ( $\phi$  in deg) Roll: the angle that the platform 2-axis makes with the local horizontal plane

$$\emptyset = -\sin^{-1}\left(\frac{X(2X)}{R} + \frac{Y(2Y)}{R} + \frac{Z(2Z)}{R}\right) - \frac{\pi}{2} \le \emptyset \le \frac{\pi}{2}$$

where (2X), (2Y), (2Z) are the elements of the second row of M representing the direction cosines of P<sub>2</sub> with respect to the ECI coordinates axes.

### SECTION 3

### COMPUTER PROGRAM INPUT/OUTPUT

### 3. 1 INTRODUCTION

This section is intended as a guide to users of the error analysis program in preparing the input data. Brief descriptions of the program capabilities and the procedures for data input are presented, and the available output data formats are described. There are standard forms for preparing the necessary data input, and they are shown in Appendix A.

The program actually consists of two separate programs: The first, called ERAN, computes error sensitivities based on given trajectory data, navigation system instrument configuration, and a model of the component error sources. Trajectory data is supplied via a tape generated by a trajectory program(s) (N-STAGE, TRIP, MVS, etc.). The instrument configuration is supplied as the input data of component orientations. The error models are supplied on an error-source schedule sheet that specifies the error sources to be considered for this configuration and when they are active. Based on this information, the ERAN program computes sensitivity coefficients, and cutputs these onto an ERAN tape.

The second program, called GUTP, basically processes the ERAN tape into the prescribed formats. Inputs to this program are the logical controls, i.e., the desired frequency of output, coordinate systems, formats, etc., and the specification of standard deviations of the error sources, along with any correlation coefficients between error sources. The ERAN tape can be processed many times without rerunning the ERAN Program.

# 3. 2 ERAN INPUT DATA

# 3. 2. 1 Trajectory Tape

Prior to running the error analysis program, a trajectory tape must be prepared that contains the following information relative to the nominal mission:

t	Time		
X, Y, Z,	Nominal position coordinates in the ECI system		
R	Magnitude of position (radius) vector		
ΧÝŻ	Nominal velocity coordinates in the ECI system		
X, Y, Z,	Nominal sensed acceleration coordinates in the ECI system		
ω <sub>1</sub> ω <sub>2</sub> ω <sub>3</sub>	Rates of platform (body) axis in platform (body) coordinates (optional)		
1X 1Y 1Z	Direction cosines of the platform (body)		
2X 2Y 2Z	axes with respect to the ECI		
3X 3Y 3Z	coordinate system (optional)		

Each file on the trajectory tape contains the information for one ERAN case and consists of the following logical records:

### 1st Record

Word 1 = 1B27

Word 2 = N

Word 3 = 0

(N = size of a data record, i.e., 11 or 23)

### Continuous Data Point Record

Word 1 = 1B35 Word 5 = Z Word 2 = t Word 6 = R Word 3 = X Word 7 =  $\ddot{X}_8$ Word 4 = Y Word 8 =  $\ddot{Y}_8$ 

Word  $9 = \ddot{Z}_{\perp}$ Word 17 = 1Y Word  $10 = \dot{X}$ Word 18 = 1Z Word  $11 = \dot{Y}$ Word 19 = 2XWord 12 = ZWord 20 = 2YWord  $13 = \omega_{\star}$ Word 21 = 2ZWord 14 =  $\omega_2$ Word 22 = 3XWord 15 =  $\omega_a$ Word 23 = 3Y Word 16 = 1XWord 24 = 3Z

(Words 13 to 24 are omitted if N = 11)

# Left Side of a Trajectory Discontinuity

Word 1 = 3B35

Words 2 through 24 are the same for all data records

# Right Side of a Trajectory Discontinuity

Word 1 = 5B35

Words 2 through 24 are the same for all data records

# Last Record of a Trajectory

Word l = 1B29

### **EQF**

All Aerospace Corporation trajectory programs are mechanized to prepare a trajectory tape in the proper format for input to ERAN. The tape writing intervals should be no greater than 4 seconds during powered-flight phases and 32 seconds during coast or free-flight phases. Higher tape densities would cause no problem, but lower densities would tend to degrade the accuracy of the integrations. The integration step size used for ERAN is

not necessarily the same as that of the input tape interval, but is controlled by input data. The ERAN Program interpolates between trajectory data points to obtain proper values for integration. The integration routine used by ERAN is based on a fourth-order Runge-Kutta method.

## 3. 2. 2 Error Sources

The Error Source Schedule (see Table A-1 in Appendix A) is used to identify which of the available error sources are to be run, and for which time periods (phases) they are to be considered. Table G-1 defines the symbol and units for each error source in the order it appears on the Error Source Schedule. Initial and terminal error sources are listed individually, while component (accelerometers and gyros) and platform errors are listed as error types. Thus, when a component or platform-error type is considered, sensitivities for all three components or axes are automatically and independently run. Each source or type of error can be considered in one or all of 12 possible independent phases of the trajectory. This phase capability is provided to accommodate time-correlated errors and/or independent error-source magnitude changes.\* It becomes increasingly more important as the mission time duration increases.

Sections 3.2.2.1 through 3.2.2.5 present a summary of the error-source types and/or error-model equations (see Section 2.3.3).

#### 3. 2. 2. 1 Initial Condition Errors

EI11 - EI13	Initial Position Errors
E121 - E123	Initial Velocity Errors
EI31 - EI33	Initial Platform Alignment Errors

If the initial time of the trajectory is equal to or less than zero, the program assumes a launch from an earth fixed pad and automatically calculates

Phase logic will be used to identify and control "Reset," a feature that updates navigation data as a function of external measurements (see Appendix D).

an initial velocity and vertical alignment error consistent with the initial position error.

# 3. 2. 2. 2 Accelerometer Errors

$$\Delta A = EA00 + EA01(A_1) + EA02(A_1^2) + EA03(A_1^3)$$

$$+ EA04(A_2) + EA05(A_3) + EA06(A_1A_2)$$

$$+ EA07(A_1A_3) + EA08(A_2^2 + A_3^2)^{1/2}$$

$$+ EA09(A_1) (A_2^2 + A_3^2)^{1/2} + EA10(A_2^2)$$

$$+ EA11(A_3^2) + EA12(A_2A_3)$$

where

 $\Delta A$  = the i<sup>th</sup> accelerometer error (i = 1, 2, 3)

EAl = (l = 00, 01, ...), as defined in Table G-1

A<sub>1</sub> = input axis acceleration of i<sup>th</sup> accelerometer

A<sub>2</sub>, A<sub>3</sub> = acceleration components normal to input axis

# 3.2.2.3 Gyro Errors

$$\dot{\phi} = \text{EG00} + \text{EG01}(A_1) + \text{EG02}(A_3) + \text{EG03}(A_1A_3) 
+ \text{EG04}(\omega_3) + \text{EG05}(\omega_2) + \text{EG06}(\omega_1) 
+ \text{EG07}(A_2A_3) + \text{EG08}(A_2) + \text{EG09}(A_1^2) 
+ \text{EG10}(A_3^2) + \text{EG11}(A_1A_2)$$

where

## 3. 2. 2. 4 Platform Errors

$$\phi_i = \text{EP01i}(A_j) + \text{EP02i}(A_k) + \text{EP03i}(A_jA_k)$$

where

\$\Phi\_i = \text{platform angular error about i}^{th} \text{ axis (i = 1, 2, 3)}

A\_j, A\_k = \text{platform acceleration components normal to i}^{th} \text{ axis}

EP1 = (1 = 00, 01, ...), as defined in Table G-1

#### 3.2.2.5 Terminal Errors

ET11 → ET13 Terminal Position Errors
ET21 → ET23 Terminal Velocity Errors

Note: These errors can be considered only on the last phase of the error analysis run and can be applied only at the trajectory tape abort time (see Section 3.2.3) or at the end of the trajectory tape.

The procedure for filling out the error-source schedule is as follows:

a. Determine which error sources are to be considered.

- b. Establish if any of these error sources are to have nonunity autocorrelation functions; i.e., establish whether multiphase logic is required.
- c. In the first column, insert an "X" in each row element that describes the error soul e to be considered.
- d. In the second (and following) columns, insert an "X" in the row elements corresponding to the error sources that require phase logic control for that particular phase\* (see example).

The error sources that have been called for by inserting X's in the appropriate squares in Column 1 will be initialized and become active at the start of the case, TSUBO (see Section 3.2.3.5). Insertions of X's into the appropriate squares in Column 2 will cause those error sources to be reinitialized at the start of the second phase (i. e., when the time of the simulation is equal to the value entered into TGOP (see Section 3.2.3.5). The sensitivity vectors from the first phase for those error sources will then become inactive. These inactive vectors will be updated at the desired output times by the transition matrix and be combined statistically with the active vectors to derive the total effect on the navigation data statistical characteristics (see Section 2.3.4). Similarly, X's in the third column will cause those error sources to be reinitialized when the time of the simulation is equal to the value entered into TGOP + 1, etc. In this manner, up to 12 independent sensitivity vectors can be created for each error source on the schedule sheet.

This completes the input on the Error Source Schedule sheet. It essentially indicates to ERAN which error source sensitivities to calculate and whether any of these types require phase logic control.

It will be necessary in setting up the input data for **QUTP** to assign sigma values (the standard deviations of each error source) and correlation

<sup>\*</sup>Error sources that change standard deviations or have time-varying correlation coefficients.

coefficients, when applicable, between error sources. The identification of a given sigma value with a sensitivity vector is accomplished by mentally assigning a number to each error source. The numerical ordering of error sources is determined by starting in the first column of the Error Source Schedule and counting down, then going to the second column, and so forth. Note that three independent error sources are associated with each "X" in an element of a component or platform error.

## 3. 2. 3 Orientation and Control Data

The data sheet used to set up the platform and component orientations and to input the necessary program control data and constants is shown as Table A-2 in Appendix A. Control data and constants have preassigned values; therefore, only those numbers that deviate from them need be input. The symbols used are summarized in Table G-2, along with their preassigned numerical values and units.

## 3. 2. 3. 1 Initial Platform Alignment

There are two options for specifying the initial platform orientation (see Figure 2). The first assumes that the platform 1-axis  $(P_1)$  is aligned along the geocentric vertical. The azimuth orientation is specified through an input of PSIP  $(\psi_p)$ , a left-hand rotation in platform coordinates). With no input in PSIP, the platform would be aligned so that the 3-axis  $(P_3)$  would be north and the 2-axis  $(P_2)$  east. With a positive  $\psi_p$ , the  $P_3$  axis would be rotated toward the east

The second option allows for a more general initial platform orientation; here, three angles are specified for aligning the platform. The initial alignment is such that the  $P_1$ ,  $P_2$ , and  $P_3$  axes are along the ECI X, Y, and Z axes, respectively. PHIP  $(\Phi_p)$  votates the platform positively about its 3-axis; LAMP  $(\lambda_p)$  rotates the platform negatively about its 2-axis; and PSIP  $(\psi_p)$  rotates it negatively about its 1-axis, in that order. The option is used when it is desired to align to geodetic or astronomic latitude as a

vertical reference for ground alignment, or when platforms are assumed to be aligned in orbit with some stellar instruments.

#### 3. 2. 3. 2 Initial Conditions

There are two options for initial condition specifications (see Figure 5). If no input to PSII  $(\psi_{1})$  is given, the program assumes the initial conditions to be referenced to platform axes; thus, down range is along the  $P_{3}$  axis, cross range along the  $P_{2}$  axis, and altitude along the  $P_{1}$  axis. If an input of PSII  $(\psi_{1})$  is specified, the program assumes that vertical or altitude errors are along the geocentric vertical, and down-range errors are referenced  $\psi_{1}$  from north. Cross-range errors are therefore  $\psi_{1}$  + 90° from north.

## 3. 2. 3. 3 Gyro Orientation

The initial orientation of the gyros and their axes is illustrated in Figure 3. Gyro alignment is made by specification of an axis of rotation (1, 2, or 3) and an argument (angle) of rotation. The program allows up to five independent rotations in any order desired. Each rotation operates on the gyros as a triad; i. e., all three gyros are being rotated and thus maintain their axis orientation with respect to each other during these rotations. The axes of rotation referred to above are those of the No. 1 gyro. Upon completion of this set of rotations, there remains an additional degree of rotational freedom of each gyro about its input axis, specified by  $PSI_{\underline{i}}(\psi_{\underline{i}})$  (i = No. 1, 2, or 3 gyro).

#### 3.2.3.4 Accelerometer Orientation

There are two options available for the alignment of accelerometers (see Figure 4). The first is the specification of an orthogonal triad and the method is identical with that described for the gyro components; i.e., an axis and argument are specified for aligning the accelerometer input axes. Then an additional degree of freedom about each accelerometer's input axis is specified by BETA<sub>i</sub> ( $\beta_i$ ) (i = No. 1, 2, or 3 accelerometer).

The second option allows for nonorthogonal accelerometer configurations. Here the method of specification (of an axis and an argument) is the same; however, each accelerometer is specified independently. The initial orientation of each accelerometer is the same with its 1-, 2-, and 3-axes along those of platforms  $P_1$ ,  $P_2$ , and  $P_3$ , respectively. The data sheet for nonorthogonal accelerometers is shown as Table A-3 in Appendix A. To exercise this option, a non-zero entry must be made in data location field ACCEL 10; conversely, a zero entry negates the option.

## 3, 2, 3, 5 ERAN Control Data

This entry controls the ERAN tape writing frequency. If no entry is made, the tape writing frequency for this case will be two records per trajectory discontinuity and two records per ERAN phase discontinuity. If a non-zero entry is made, a single record will be written at each multiple of 100 sec for powered flight, and of 1000 sec for free flight, unless otherwise specified in PPF and PFF.

PPF This entry controls the tape writing interval during powered flight for values other than the standard 100 sec, when  $\emptyset$ UT  $\neq$  0.

PFF Similarly this entry controls the tape writing intervals during free flight for values other than the standard 1000 sec.

TSUBO This is initial time and can be any time greater than or equal to the first time point on the trajectory tape (file). If the first time point (t) on the tape is not zero (t = 0), then the desired starting time must be entered.

TSUBA This is abort time and can be any time less than the last time point on the tape (file). If an entry is omitted, the tape will be processed from TSUBO to the end of the trajectory tape (file).

When the trajectory tape contains more than one trajectory, this entry identifies the trajectory (file) to be processed (e.g., if the entry is N, ERAN will process the N<sup>th</sup> file on the tape). If omitted, the next trajectory will be processed. For the first ERAN case this would be File 1.

When consecutive files are being processed on a trajectory tape, starting with File 1, the program will run most efficiently when no entry is made to TRAJ. When an N entry is made, the program will process the N file for that case and all subsequent cases until TRAJ is altered by input.

ENDC This entry controls the use of the equations of motion in ERAN.

These equations model an oblate atmosphere-free earth, used

to propagate errors beyond abort time TSUBA. The pair of entries (ENDC and 1) control the termination of the propagation. The options for inputting to ENDC are as follows:

	a.	No Entry	terminate at abort time
	ъ.	TIME	terminate at that value of time (sec), which is specified in the next entry (>TSUBA)
	c.	THETA	terminate at the value of range angle (dog) boyond the termination of the trajectory tape, which is specified in the next entry $(0 < 9 < 180)$
	d.	ALTP	terminate at that value of altitude (ft) with a position slope, which is specified in the next entry
	e.	ALTM	same as (d) above, with negative slope.
i			location field where the numerical value of the ol is to be input.
MAXT	mot	ion. It is pre	s the maximum running time of the equations of set to 36,000 sec; i.e., when t = 36,000 the run less a greater value is entered.
DTNP	fligh		s the ERAN integration step size during powered vill cause the program to integrate at its nominal step. *
DINF	fligh	nt. No entry w	s the ERAN integration step size during free vill cause the program to integrate at its tegration step. *
BMT	will	not be inertia	ed to tdentify a case where the platform (body) axes lly oriented during the run. A non-zero entry gram to seek one of the options described below.
BRTAB	forn entr table deri	n turning rates y will cause the e of input rate ved by integra	o identify the option to be used for obtaining plats and platform direction cosines. A non-zero see program to determine platform rates from a s. From this data the direction cosines are ting the matrix differential equation of direction will cause the program to read this data (rates

Note: The program integration routine converges on each multiple of the tape writing interval when QUT = 0. Therefore, when the value of PPF is less than DTNP, the former would be the integration step size used in powered flight. Similarly, when the value of PFF is less than DTNF, the former is used for the free flight integration step size.

and direction cosines) from the trajectory tape.

TGGP
This entry and the ten that follow it are used to identify the time to terminate a phase. No entry is needed to terminate the last phase; consequently, for cases in which there is only one phase, no entry is required.

# 3.2.3.6 Earth Model Constants

OMEGE rotation rate of the earth

A equatorial radius of the earth

GM gravity constant used in the equations of motion

e ellipticity of the earth

J constant in the earth's potential function

H constant in the earth's potential function

D constant in the earth's potential function

MU gravity constant (equals GM) used in the variational equations.

The numerical values of these constants are given in Table G-2.

## 3. 2. 3. 7 ERAN Case Control Data

Since multiple cases from one trajectory tape can be run sequentially in using the ERAN program, two cards are necessary to instruct the program as follows:

END The preceeding cards contain all the data necessary to run this case.

ENDIOE This is the last case processed by ERAN. Since it is preprinted on the standard form, it must be crossed out for all cases except the last.

#### 3.2.4 Tabular Input

#### 3.2.4.1 Turning-rate Table

The standard form for platform turning rates, which the program uses if the BRTAB flag (see Section 3.2.3) is non-zero, is shown as Table A-4 in Appendix A. The definitions of symbols and the method to be used to input data are as follows:

ORDER refers to the order of data interpolation to be used by the program to establish rates between data inputs. A 1 entry will

cause the program to use linear interpolation, a 2 quadratic, etc. The interpolation routine used is a kth order Lagrangian N identifies the total number of time points in the table that follows first time point of table  $(t_1 \le TSUBO)$ last  $(N^{th})$  time point of table  $(t_N \ge TSUBA)$ rate about platform (body) 1-axis at time t<sub>1</sub> rate about platform(body) 1-axis at time t<sub>N</sub> rate about platform (body) 2-axis at time t<sub>1</sub> ω<sub>21</sub> rate about platform(body)2-axis at time t<sub>N</sub> <sup>ω</sup>2N rate about platform(body) 3-axis at time t, <sup>ω</sup>31 rate about platform(body) 3-axis at time t<sub>N</sub> <sup>ω</sup>3N Note: If the table contains many zeros in sequence, they can be entered by writing a Z in the prefix field and the number of zeros to be generated in the value field. As an example, the table for a case of 20 time points, zero

rates about the 1- and 3-axis, and the first two rates about the 2-axis, also zero, would look like Table 2.

Table 2. Sample for a Case of 20 Time Points

PRE	LOC	Value	Remarks
1		20	
		value of t	
		•	
-		value of t <sub>20</sub>	
Z		$ve^{1}ue of \omega_{2}(t_{3})$	20 zero rates about 1-axis and 2 zero rates about 2-axis
			D- GAID
	: . :-		
Z		value ɔf ω <sub>2</sub> (t <sub>20</sub> ) 20	20 zero rates about 3-axis

Also note that the reverse side of the standard form can be used to continue the rate table.

## 3. 2. 4. 2 Equation of Motion Initialization

The program is mechanized so that the equations of motion can be initialized independent of a trajectory tape input. This feature is used when it is desired to obtain transition matrices or to use one of the mission evaluation options to derive miss coefficients. The format\* for this data is given as Table A-5 in Appendix A.

<sup>\*</sup>A printed standard form is not available.

# 3. 2. 5 Multiple Cases

As mentioned previously, ERAN has the capability to run multiple cases from a single trajectory tape. The data used for the first run is retained for the second (and subsequent) runs; thus, only data that requires changes from the preceding runs needs be input. When it is desired to eliminate the effects of an orientation option used in a previous case, it is necessary to input a minus zero in an appropriate location. The three options and the methods of cancelation are as follows:

a.	Platform Orientation
	Option 2

input minus 0 in PHIP

b. Initial Condition
Orientation Option 2

input minus 0 in PSII

c. Nonorthogonal Accelerometer

input minus 0 in ACCEL 10, which is the input location for the first axis of rotation of the No. 2 accelerometer component

This last operation will negate the logic that was set up by the previous nonorthogonal case and will therefore interpret the data for the No. 1 component as that required for a triad.

Extreme caution should be exercised when attempting to change the Error Source Schedule for an operation where there are more than 6 phases. Some knowledge of the input routine is necessary to present the intrinsic problem.

The D option (i. e., D in the prefix field of the input word), used to input the Error Source Schedule, causes two words to be stored in the computer, with the last 6 characters being stored in the location immediately following the location of the first 6. When there are no entries in Columns 7 through 12, however, only the first 6 characters are stored and the second location remains unaltered. It is then apparent that an X, entered beyond Column 6 for a previous case, cannot be eliminated without entering at least one X

into some other column beyond the 6th for the case in question. Cancellation of the error source for all phases can be achieved by entering zeros into the appropriate locations for the sigma value (see Sections 3.3.3.1 and 3.4). Phase logic, for an error source during phases 7 through 11, can be eliminated when there are less than 12 phases to the case by entering an X in Column 12. Should that be the only entry on the line, the error source would be eliminated for the entire case.

# 3.3 OUTPUT DATA

The output data processor program (ØUTP) takes the data generated by ERAN and produces output data at the required times, with the prescribed transformations and the proper format. The options available for the above data follow.

## 3. 3. 1 Output (Print) Times

- Option 0 Output the data only at the terminal condition of the case.
- Option 1 Output at the phase discontinuities plus the terminal conditions.
- Option 2 Output data called for by Options 0 and 1 and at all trajectory discontinuities where the sensed acceleration goes from non-zero to zero or from zero to non-zero, including the initial time.
- Option 3 Process every time point on ERAN tape as determined by the tape density control.

## 3.3.2 Output Coordinate Systems

- Presents data in an Earth Centered Inertial System, where the Z-axis is the earth's polar axis and the X- and Y-axes are in the equatorial plane. Generally, the convention is that the X-axis passes through the Greenwich meridian at time zero, and Y completes a right-hand system; however, these coordinates are determined by the particular trajectory program used to generate the input tape.
- Presents data in a local horizontal coordinate system, which is inertial and developed from the nominal trajectory position and velocity vectors. X is down range, i.e., directed along the projection of the inertial velocity vector onto the plane normal to the radius vector; Y is vertical, i.e., along the geocentric radius vector; and Z is cross range, forming a right-hand coordinate system.
- EVALU Presents additional data at the terminal condition only with a prescribed transformation. \* Presently there are the following three options for this output:
  - EVALUI: Presents the down-range (M<sub>D</sub>), cross-range (M<sub>C</sub>), and timing (M<sub>T</sub>) errors (misses) at a fixed altitude

<sup>\*</sup>A special format is used for these transformations (see Section 3.3.3.4).

EVALU2: Presents the cross-range (MC), vertical (MV), and

timing (M<sub>T</sub>) errors (misses) at a fixed range

EVALU3: General - represents transformation developed from

input matrices.

# 3. 3. 3 Output Data Formats

The five present formats for output data will be described in Sections 3.3.3.1 through 3.3.3.5. Examples of the formats are presented with the test cases in Appendix C.

## 3. 3. 3. 1 Vector Errors

In order to present the vector errors at a particular time, ØUTP first updates all inactive vector sensitivities (previous phase sensitivity vectors) by premultiplying them by an appropriate transition matrix. Next it scales the vector sensitivities by the proper sigma level (input data of the sigma of a particular error source). This results in a vector error in the ECI coordinate system. Finally, it performs a coordinate transformation, when required. This data is presented in a standard format where

<u>Line 1</u> gives the run date and job identification (see Section 3.4)

Line 2 is the case identification

Line 3 is the nominal time and coordinate system identification

Line 4 is column headings where DPX, DPY, DPZ are delta-position coordinates to the nearest ft

DVX, DVY, DVZ are delta-velocity coordinates to the nearest 0.01 ft/sec

DOX, DOY, DOZ are delta-platform orientation coordinates to the nearest 0.1 sec

Line 5-up is vector error, where the left column identifies the vector as follows:

Four characters are used to identify the error-source type, and the component or axis it represents. The identification generally follows the symbols given in Table G-1 with the following changes:

Two characters are used to identify the phase in which this particular error source was initiated (01 to 12)

Initial Condition

Accelerometers

and gyros

Platform

Terminal Conditions

E is replaced by O

E is dropped and the error type is followed by 1, 2, or 3, indicating which component it represents

E is dropped and the error type is followed by 1, 2, or 3 indicating which platform axis it represents

E is replaced by T, and T is replaced by O

Note that the order in which the error vectors are presented is that given in Section 3, 2, 2.

#### 3.3.3.2 Covariance Matrix

The covariance matrix is formed from the expression

$$\sum_{ECI} = \sum_{i=1}^{n} \sum_{j=1}^{n} \rho_{ij} \sigma_{i} \sigma_{j} \overline{x}_{i} \overline{x}_{j}^{T}$$

where

= covariance matrix in ECI coordinates (9 × 9 matrix)

n = total number of error sources

 $\rho_{ij}$  = correlation coefficient between the i<sup>th</sup> and j<sup>th</sup> error source. When i=j,  $\rho$ =1; when i\u00edj,  $\rho$ =0 unless input otherwise

 $\sigma_i$ :  $\sigma_j$  = standard deviations of the i<sup>th</sup> and j<sup>th</sup> error sources

E sensitivity vector of ith error source

 $\bar{x}_{i}^{T}$  = transpose of  $j^{th}$  sensitivity vector

To obtain the covariance matrix in the local horizontal coordinate system, the following operation is performed

$$\sum_{LH} = \underbrace{M_{LE}}_{FCI} \underbrace{M_{LE}}_{T}^{T}$$

where

= covariance matrix in local horizontal coordinates

MLE = matrix (9 × 9) which transforms a sensitivity vector from ECI to local coordinates

 $M_{LE}^{T}$  = transpose of  $M_{LE} = M_{EL}$ 

The presentation of this data at a particular time is in a standard format, where

Line 1 = case identification

Line 2 = nominal time and coordinate system identification

Line 3 identifies it as the covariance matrix

Line 4 = column heading (same definition as vector errors)

Lines 5 to

= covariance matrix in the following format:

diagonal presents variances of navigation errors in floating point upper elements present covariances of navigation errors in floating point

lower elements present correlation coefficients in fixed point.

Line 14 = standard deviations (sigmas) of the navigation errors formed from the square root of the variances

Line 15 = trajectory variables in ECI coordinates

Line 16 = trajectory variables in earth reference coordinate system,

where:

LAT = geocentric latitude (deg)

LONG = longitude from Greenwich meridian (deg)

ALT = altitude (n mi) above the surface of an oblate

earth (n mi)

VEL = inertial . locity (ft/sec)

FPA = flight path angle defined as the angle the inertial velocity vector makes with the local geocentric horizontal (deg)

= azimuth of the inertial velocity vector, measured

## 3.3.3.3 Transition Matrix

AZ

The transition matrix is used in the ERAN Program to propagate sensitivity vectors across the free-flight sections of a trajectory, rather than integrating each set of error-source equations.\* It is used by ØUTP when presenting a time history of vector errors during free flight in the same manner, i. e., to propagate the sensitivity vectors. ØUTP also uses the transition matrix to update an inactive vector (one generated in a previous phase), when running multiphase cases.

clackwise from north.

The transition matrix is generated in the usual manner - be solving the homogeneous differential equations (in ECI coordinates) for each initial condition error. To obtain the transition matrix in the local horizontal coordinate system, the following operation is performed:

$$\begin{array}{ll} \Phi(t,\tau) = & M_{LE}(t)\Phi(t,\tau)M_{LE} \\ \text{LH} & \text{ECI} \end{array}^T(\tau) \end{array}$$

In the present formulation of the program, it is assumed that the accelerometers are disconnected at termination of a powered phase.

where

<b>O</b> (t, s) LH	= transition matrix in local horizontal coordinates
Φ(t, τ) ECI	= transition matrix in ECI coordinates
M <sub>LE</sub> (t)	= matrix at time t, which transforms a sensitivity vector from ECI to local coordinates
$M_{LE}^{T(\tau)}$	= transpose of M <sub>LE</sub> at time τ

There is an option to control the output of the transition matrix (see Section 3.4). When called for, the matrix will be presented at each discontinuity (phase or trajectory tape). \* In addition, if a time history (print Option 3) is called for, the transition matrix will be presented at the same times as the vector errors and covariance matrix. The presentation of the transition matrix is in a standard format, where

Line 1	= case identification
Line 2	= identifies it as the transition matrix and the applicable time arguments (t, τ)
Line 3	= the coordinate system identification
Line 4	= format identification
Line 5	= column headings
Line 6-14	= transition matrix
Line 15	= trajectory variables in ECI coordinates at time T
Line 16	= trajectory variables in ECI coordinates at time t
Line 17	= trajectory variables in earth reference coordinate system at time τ
Line 18	= trajectory variables in earth reference coordinate system at time t

# 3.3.3.4 Mission Evaluation

As indicated in Section 3.3.2, there are presently three options available for presenting data at the end of the case that can be used for evaluating the

Except for free flight, a transition matrix is not computed in Phase 1.

success of the mission. The data presented when one of these options is called for consists of vector errors and a covariance matrix. The format for each option is as follows:

EVALUI Presents data at the reference altitude instead of the reference time

#### Vector Errors

Line 1

Line 2

nominal time and criterion (ALT)

Line 3

column headings, where:

MT = timing error to the nearest 0.001 sec

MC = cross-range miss to the nearest ft

MD = down-range miss to the nearest ft

vector errors, where the left column identifies (described in Section 3.3.1) the vectors

#### Covariance Matrix

identifies it as a covariance matrix Line 1 Line 2 column heading Line 3-5 covariance matrix output (same format as described in Section 3.3.2) Line 6 sigma values Line 7 headings for nominal trajectory conditions at termination Line 8 trajectory conditions where: LAT, LONG, ALT are as defined in Section 3.3.3.2 VEL/P = magnitude of relative\* velocity vector FPA/R = magnitude of relative flight path angle (deg) AZ/R = azimuth of relative velocity vector (deg)

<sup>\*</sup>Velocity vector with respect to rotating earth.

EVALU2

Presents data at the reference range angle instead of at the reference time. The data format is the same as for EVALU1 except as noted below.

Line 2 criterion (ALT replaced by RANGE)

Line 3 MD is replaced by MV (vertical miss to the nearest ft)

This option is used for special cases in which the linear transformation between ECI position and velocity errors and some arbitrary parameters are known; e.g., the midcourse maneuver velocity components as a function of injection errors for a space probe, some orbit elements, etc.

#### Vector Errors

Line 1 case identification

Line 2 nominal time and identification of EVALUATION

OPTION 3

Line 3 column heading (1, 2 .... 6)

Line 4-up vector errors (floating point) where the left column identifies (as described in Section 3.3.3.1) the vector

## Covariance Matrix

Line l covariance matrix identification

Line 2 column headings (1, 2 .... 6)

Line 3-8 covariance matrix (same format as described in

Section 3. 3. 3. 2)

Line 9 sigma values

## 3. 3. 3. 5 Platform Reference Attitude Time History

When a torqued platform or strapped-down case is being run, a time history of attitudes and direction coaines are given at the end of the case. The times are the same as those called for by the print option. The format for presentation of this data is as follows:

Line 1 identification of type of output

Line 2 column headings, where

THETA (θ) = angle (deg) platform 1-axis makes with the local horizontal plane

PSI (ψ) = angle (deg) the projection that the platform 3-axis onto the horizontal plane makes with north

PFI (\$\phi\$) = angle (deg) the platform 2-axis makes with the local horizontal plane

For a strapped-down case these angles would be missile pitch, yaw, and roll angles, respectively.

1X, 1Y, 1Z = direction cosines of the platform 1-axis, with respect to the ECI coordinate system

2X, 2Y, 2Z = direction cosines of the platform 2-axis, with respect to the ECI coordinate system

Line 3-up time history of above data

# 3.4 ØUTP INPUT DATA

SØPT

PHIL

EVALU

**FØPT** 

**SIGMA** 

The standard form for input data to QUTP is presented as Table A-6 in Appendix A. The definitions and procedure for filling out this sheet are as follows:

Up to 60 characters (30 each), which will be printed as the first line of vector error output

Up to 60 characters (30 each), which will be printed as the second line of vector errors and first line of all other outputs

Print time option as discussed in Section 3.3.1. No input will produce Option O.

Controls output coordinate system. No input results in LH coordinate system. +ECI results in both ECI and LH output. -ECI outputs only in ECI coordinates.

The number of the case (N) to be processed, N being the Nth trajectory processed by ERAN (but not necessarily the Nth trajectory on trajectory tape).

When outputting consecutive ERAN cases, starting with Case 1, the program will operate most effectively if no entry is made to CASE. When an N entry is made, the program will process the Nth case until CASE is altered by input.

A non-zero entry will result in storing the sigma values for the next (and subsequent) runs; whereas a zero entry will result in setting all sigma entries to zero after the present case has been completed.

Correction term for longitude output. To be used when the trajectory ECI system is not referenced to Greenwich.

Identifies the mission evaluation option (if any) to be output.

Non-zero entry will result in transition matrix(es) output.

In the LOC. field, the vector number is input and the sigma value for that vector is put in the value field.\*
Only when a SIGMA value changes is it required to input a new value; otherwise, it will assume the sigma

An entry of zero will cause that vector to be eliminated from the case.

value of the previous vector error. As an example, if unit sensitivites are desired, then a 1 in the LOC. field and a 1 in the VALUE field will result in output with unit scaling of all error sources. However, when the SOPT option is used for multiple cases, all desired changes to the sigma table must be entered explicity. In the above example, all desired changes from their assigned unit values would have to be entered; e.g., a change of the sigma value for the first error source would only alter that value, all others retaining their unit values.

RHØ

These are correlation coefficients. Two entries are required to input a correlation coefficient: The first identifies the error sources (by vector number) that are correlated, and the next gives the value of the correlation coefficients. All correlation coefficient data is retained in storage; therefore, when running multiple cases, care must be exercised to not get unwanted correlation into the covariance matrix calculations. A double-zero in the field for assigning vector numbers of a correlation coefficient will result in eliminating the effects (if any) of that previously stored correlation coefficient, as well as of all those that followed on the input sheet.

END

Same control as discussed for ERAN

ENDJØB

Same control as discussed for ERAN

ØUTP has the same logic of data storage (except as noted in the SØPT option) for multiple cases as ERAN. Therefore, only changes to data need be entered for runs following the first. To negate the SYSTM option, six zeros must be entered (i.e., when LH output alone is desired after some other option on the previous case has been chosen).

Note units of error sources in Table G-1.

When the EVALU3 option is used, the format for the input data sheet is presented as Table A-7 in Appendix A. The linear transformation matrix [M] used in this option is formed from products of input matrices by

$$[M] = [M_1][M_2][M_3] \cdots [M_n]$$

 $n \le 10$ 

where  $[M_i]$  is a  $(6 \times 6)$  matrix input.

<sup>\*</sup>A preprint standard form is not available.

#### **SECTION 4**

#### SAMPLE CASES

Three test cases were designed to demonstrate the procedures for filling out input data sheets when exercising the various program options available, and to present data in all of the output formats. The data sheets used to set up the test cases are presented in Appendix B and the output listings from these runs in Appendix C.

The trajectory used for the test cases was one that had been designed to place a payload into a 24-hour synchronous equatorial orbit. Following are the major trajectory sequences:

0 - 464	Powered flight from launch to booster burnout
464 - 477	Separation sequence (coast)
477 - 498	Inject into 100-mile parking orbit
498 - 1380	Coast to first equatorial crossing
1380 - 1685	Inject into transfer orbit
1685 - 20177	Coast in transfer orbit to apogee of 19,300 n mi
0177 - 20288	Inject into synchronous equatorial orbit

The salient features of the test cases and the pertinent input/output options used to obtain these features are now described.

## 4.1 TEST CASE 1

This is the evaluation of the uncertainty of instantaneous impact prediction (IIP) for premature thrust termination, by using the inertial navigator data and assuming a vacuum re-entry. The same option could be used for evaluating hallistic missile accuracy or guided re-entry vehicle accuracy at a fixed altitude.

The configuration of the inertial navigator was one in which the platform 1-axis was aligned with the geodetic vertical and the 3-axis was north. \* The input axes of the gyros and accelerometers were aligned along the platform axes. The error sources considered were initial position (3), initial platform alignment (3), accelerometer bias (3), accelerometer scale factor (3) and gyro bias drift (3). To evaluate the impact accuracy of a thrust termination at 400 sec, the trajectory tape was aborted at 400 sec and the equations of motion were used to integrate during free flight; they were terminated when the altitude went through zero on a negative slope. Although the trajectory tape had only one file, it was necessary to enter all in TRAJ in order to obtain multiple processing of the trajectory. The data sheets used for this run are shown as B-1, Error Source Schedule and B-2, Orientation and Control Data in Appendix B. Since two more cases were to be run by ERAN before being processed by ØUTP, the ENDJØB O card was scratched out in B-2.

The processing of this data was controlled by ØUTP and the data sheet used is shown as B-9. Since it was desired to process the ERAN tape in sequential order, it was not necessary to enter anything in CASE. If processing in a different order, or reprocessing any particular case, had been wanted, it could have been done by using the CASE control. It was required to obtain output in ECI coordinates at the powered flight termination and at

Since the trajectory was run on a spherical earth model, the geodetic and geocentric latitudes are equal.

impact, and to evaluate the impact errors by using mission evaluation Option 1. As it was desired to save the SIGMA data for the next case, the SØPT option was called for. The lg errors for this case are shown in Table 3.

Table 3. One-Sigma Errors for Test Case 1

Vector Number(s)	Error Source	Sigma Value
1, 2, 3	initial position	500 ft (three axes)
4, 5, 6	initial platform orientation	30 sec (three axes)
7, 8, 9	accelerometer bias	10-4g (3 components)
10, 11, 12	accelerometer scale factor	10-4g/g (3 components)
13, 14, 25	gyro bias drift	0.1 deg/hr (3 components)

The bias and scale-factor error sources of each accelerometer were correlated with a correlation coefficient of 0.5, i.e., the number one accelerometer bias error (7) was correlated with its scale-factor error (10), etc. Since additional cases were to be processed by ØUTP, the ENDJØB O card was scratched, completing the input for this case.

## 4.2 TEST CASE 2

In this case, an evaluation is made of the altitude, cross-range, and time errors at a fixed range after completion of one orbit. The configuration of the inertial navigator was the same as in Test Case I, but it was arrived at in a different way. The platform 1-axis was aligned with the vertical as before, but the 3-axis was aligned east. To retain the same gyro orientation with respect to the trajectory, it was necessary to rotate the gyro cluster 90' about its 1-axis. The accelerometer alignment was controlled by using the nonorthogonal accelerometer option (see B-4). The error sources considered were the same as in Case 1, with the addition of terminal errors (applied at the abort time). The trajectory tape was aborted at 500 sec to insert the terminal condition errors (thrust tailoff, guidance equations, etc.) and the equations of motion used for one orbit (approximately 5500 sec). It was desired to have a time history output; therefore, ØUT was made non-zero, PPF was set at 400 and PFF at 2000. The data sheets used to make this run are shown as B-3 through B-5 in Appendix B. It was also necessary to scratch the ENDJØB card.

The data sheet for output processing of this case is shown as B-10. Using Option 3, time history, results in additional output at 400 sec during powered flight and every 2000 sec during orbit. It was desired to have only the LH coordinate system output; therefore, six zeros (000000) were entered in SYSTM to negate the logic from the Case 1 option. The mission evaluation Option 2 was used and the SØPT option cancelled. Since the SIGMA's for the first 15 error sources were held over from Case 1, only the terminal condition error-source sigma values were required. Since no changes in the correlation coefficients from Case 1 were desired, entries in RHØ were not necessary. The ENDJØB card was scratched, completing the input data required for this case.

# 4.3 TEST CASE 3

Û

This was an evaluation of the errors at injection into the final orbit. The gyro drift was "ssumed to have an exponential autocorrelation function with a time constant of 2 hr. The accelerometer bias during the trajectory's final powers, equence had a standard deviation three times larger than, and uncorrelated with, that of the initial trajectory sequences. The platform 1-axis was aligned with the geocentric vertical and the 3-axis was north. The initial condition position errors were referenced to platform axes. The platform was torqued about its 3-axis (approximately missile pitch axis) to maintain a small (<20°) angle between the missile and the platform axis throughout the trajectory. The accelerometer and gyro alignment with respect to platform axes was the same as in Case 1. The error sources were the same, with the addition of a gyro-torquing scale-factor error.

To achieve the evaluation described above, the trajectory was divided into 3 phases, with the first terminating in 2 hr, the second in 4 hr, and the third phase at the end of the trajectory (5.63 hr). This allowed an approximation of the effect of the gyro-error autocorrelation function. (More phases would more nearly approach the true effect.)

The changes in the Error Source Schedule were in EAOO, EGOO, EGO6, and the terminal condition errors (see B-6 in Appendix B). The body turning rates are given in B-7, and the changes in the control data (B-8) were the following:

PSIP = 0, aligns platform 3-axis north ( $\psi = 0$ )

PHIP = -0, changes platform alignment option back to 1 and aligns is

with respect to geocentric vertical

PSII : -0, changes IC option back to I and causes initial position

errors to be along platform axes

I GYRO = 0, references gyros to platform axes

I ACCEL = 0, references accelerometers to platform axes

1 10 = 0, changes accelerometer option back to 1, i.e., orthogonal orientation

TSUBA = chosen to be a time greater than (or could have been equal to)
the end of the trajectory tape

ENDC = 0, eliminates use of the equations of motion

ØUT = 0, eliminates use of the intermediate tape writing intervals

BMT = 1, indicates a non-inertial platform case

BRTAB = 1, indicates rates are supplied by an input table

 $TG\PhiP = 7200$ , indicates time to end the first phase

1 = 14400, indicates time to end the second phase

The final phase is ended by the termination control.

The data sheet for the output processing of this case is given in B-11. The print option was 2 (phase and trajectory discontinuities) and EVALU set at zero to eliminate its output. Although the SIGMA's were the same for the first 15, they had to be re-entered because the SOPT option was zeroed out in the previous case. The vector errors for this case are shown in Table 4.

Table 4. Vector Errors for Test Case 3

Vestor Numbers	Error Source	Sigma Value
1, 2, 3	initial position	500 ft (3 axes)
4, 5, 6	initial platform orientation	30 sec (3 axes)
7, 8, 9 (phase 1)	accelerometer bias	10-4g (3 components)
10, 11, 12	accelerometer scale factor	$10^{-4}$ g/g (3 components)
13, 14, 15 (phase 1)	gyro drift	0.1 deg/hr (3 components)
16, 17	gyro torquer scale factor	0 (Nos. 1 and 2 gyros)
18	gyro torquer scale factor	10-4 (No. 3 gyro)
19, 20, 21 (phase 2)	gyro drift	0.1 deg/hr
22, 23, 24 (phase 3)	accelerometer bias	$3\times10^{-4}$ g (3 components)
25, 26, 27 (phase 3)	gyro drift	0.1 deg/hr
28, 29, 30	terminal velocity errors	0.1 ft/sec

The correlation of accelerometer bias and scale factor during Phase 1 was assumed to be the same as in Cases 1 and 2, but it had to be re-entered because additional correlation coefficients were being entered. The time correlation of gyro errors were calculated as

$$\rho_{ij} = \exp{-\frac{(t_i - t_j)}{7200}}$$

where  $\rho_{ij}$  is the appropriate correlation coefficient, and

$$(t_i - t_j)^* = 14400 - 7200 = 1200$$
  
 $20288 - 7200 = 13088$   
 $20288 - 14400 = 5888$ 

This completes the description of the input data required for this case.

Printouts listing the cards used for ERAN data and ØUTP data are given for each run. Along with the output listings, they are included in Appendix C.

Finer or coarser time intervals could have been chosen to approximate the autocorrelation function  $\exp - \frac{t}{T}$ , with more or less phases required for the approximation.

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# APPENDIX A STANDARD INPUT DATA FORMS

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Table A-1. ERAN Error Source Schedule

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Table A-2. ERAN Orientation and Control Data

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Table A-3. ERAN Nonorthogonal Acceleromater Orientation

## X-3 7090 INPUT DATA



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			+		Specification of Orientation of No. 2 Accelerometer for Option 2
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		23			Angle " " "
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## Table A-4. ERAN Turning Rates in Platform Coordinates

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Table A-5. ERAN Equation of Motion Initialization

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Table A-6. ØUTP Case Control and Data Input Form

#### 7090 INPUT DATA



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Table A-7. ØUTP EVALU 3 Input Data Form.

## X-3 7090 INPUT DATA

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COMPUTATION & DATA PROCESSING CENTER

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B-1. Error Source Schedule for Test Case 1

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B-2. Orientation and Control Data for Test Case 1

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B-3. Error Source Schedule for Test Case 2

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B-4. Nonorthogonal Accelerometer Orientation for Test Case 2

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B-5. Orientation and Control Data for Test Case 2

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B-6. Error Source Schedule for Test Case 3

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B-7. Turning Rates in Platform Coordinates for Test Case 3

X-1 7010 HIPUT DATA POOL2A-S1 (Rev. 11/5/64)



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B-8. Orientation and Control Data for Test Case 3

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B-9. Case Control and Data Input Form for Test Case 1

X-1 7090 INPUT DATA P0012A-62 (Rev. 11/18/64)



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B-10. Case Control and Data Input Form For Test Case 2

X-1 7090 INPUT DATA
PG012A-S2 (Rev. 11/18/34)

ABROOFACE CORPORATION
COMPUTATION A BATA PROCESSING CENTER

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B-11. Case Control and Data Input Form for Test Case 3

### APPENDIX C

### OUTPUT LISTINGS FOR SAMPLE CASES

C-1.	ERAN Input Data	C-3
C-2.	Test Case 1	C-5
C-3.	Test Case 2	C-19
C-4.	Test Case 3	C-45
C-5.	<b>Ø</b> UTP Input Data	C-73

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C-1. ERAN Input Data

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CARD	9	;	TG0P 720C	-	1440
CARD	ş	45	END 0		
CARD	2	46	END 1080		

C-1. ERAN Input Data (Concluded)

11/11/65 JOHN DOE BLDG N 64 RM 2 TEST CASE 1

		0.0-
Δ.		000 000 000 000 000 000 000 000 000 00
RY TAPE 562		900 0.0 0.0 0.0 0.0 0.0
FRAJECTORY		50.0 -0.00 -0.00 -0.00
EVAL 1.		0000- 0000- 0000- 0000- 000-
DISPERSIONS	SYSTEM LH	0.03 -0.00 0.00
116	OURDINATE S	290 200 200 00 00 00 00 00 00 00 00 00 00
	3	500° 500° -0- -0-
	ė	× 2000000
	TIME	111-01 0132-01 013-01 0131-02 0132-01 0431-02

C-2. Test Case 1

TRAJECTORY TAPE 562 CUORDINATE SYSTEM LH

*1 0 * 4 % L L L L L L L L L L L L L L L L L L							
CUVARIANCE MAIRIA							
DPY	740	X	מע	240	<b>100</b>	DOV	700
0.2500E 0& -0.1305E-02	,	-0.8941E-07	E-02 -0.8941E-07 -0.1601E 02 -0.8714E 01	-0.8714E 01	0.26306-05	0.2630E-05 -0.1526E-04	0.2467E 04
0.2500E 06	0.2500E 06 -0.9766E-03	0.1601E 02	0.5960E-07	0.4470E-07	0.9367E-06	0.9367E-06 -0.3422E-05 -0.5521E-05	-0.5521E-05
-0.000	0.2500E 06	0.8714E 01	0.2980E-07	0.2980E-07	-0.2467E 04	0.2980E-07 -0.2467E 04 -0.3287E-05 -0.6692E-05	-0.6692E-05
0.8784	0.4780	0.1329E-02	•0	0.9095E-12	-0.8599E-01	0.9095E-12 -0.8599E-01 -0.3544E-09 -0.4955E-09	-0.4955E-09
000000	000000	•0	0.1026E-02		0.7586E-10	0.5581E-03 0.7586E-10 -0.9313E-09 -0.1580E 00	-0.1560E 00
0.000	0000.0	0000.0	1.0100	0.3037E-03	0.3037E-03 -0.1693E-10	•	-0.85996-01
0.0000	-0.1623	-0.0776	000000	-0.0000	0.9243E 03		0.2044E-06 -0.3756E-06
-0.000	-0.0000	-0.000	-0.0000	•	0.000.0	0.9000E 03	0.9000E 03 -0.1164E-04
-0.000	-0.0000	0000-3-	-0.1623	-0.1623	-0.0000	0000-0-	0.9243E 03

C-2. Test Case 1 (Continued)

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30.4030

30.0000

30.4030

9.0174

0.0320

0.0365

500.0000

200.000

\$16. A \$00\* . JUO 2007 0. A 2 90.000

> 219.17 FPA -0.000

XDUT 1320,79 VEL 1338,85

2 9991646. ALT -1.10

> Y -18112597. LONG -80.578

> > 3005559. LAT 28.555

TRAJECTORY VARIABLES.
X
TIME X
30059

YDOT

11/11/65 JOHN DOE BLDG N 64 RM 2 TEST CASE 1

TAPE 562
TRAJECTORY
:
EVAL
DISPERSIONS
116

TIME*	•		COURDINATE	SYSTEM ECI					
	DP X	A d O	240	DVX	DVV	240	DOX	A00	700
111-01	72.	-433.	239.	0.03	10.0	•	0.0-	0.0	•
112-01	39.	-236.	-439.	0.02	00.00	ċ	6.4-	<b>9.</b> 0-	ī
113-01	493.	82.	•	0.0-	0.0	ċ	<b>*</b> •0	-2.3	ĩ
11-01	c	įဝ		c	•	•	4.3	-25.0	ì
10-21	ć	်င		•	•	ċ	29.6	4.9	-
0133-01		Ö	o	o	•	ċ	-2.3	14.1	Ñ

-2. Test Case 1 (Continued)

TIME	°0	00	IIP DISPERSIOM COORDINATE SYSTEM	IIP DISPERSIONS EVAL 1. DINATE SYSTEM ECI		TRAJECTORY TAPE 562	562	
COVARIA	COVARIANCE MATRIX							
X 40	A d O	740	DVX	440	7.00	00%	Ana	700
0.2500E 06	0.2441E-02	0.2685E-03 -0.1490E-06	-0.1490E-06	0.1823E 02	•	0.7629E-05	0.7629E-05 -0.1179E 04 -0.2138E	-0.2138E 04
0.000	0.2500E 06	0.2500E 06 -0.4053E-03 -0.1823F 02	-0.1823F 02	0.1490E-06	•	0.1179E 04	0.1179E 04 -0.1335E-04 -0.3547E 03	-0.3547E 03
000000	-0.0000	0.2500E 06	0.1795E-07	0.2750E-07	ö	0.2138E 04	0.3547E J3 -0.1257E-05	-0.1257E-05
-0.0000	-1.0000	0.000.0	0.1329E-02	0.1329E-02 -0.1091E-10	•	-0.8599E-01	0.13486-08	0.2587E-01
0000.1	0000.0	0.000.0	-0.0000	0.1329E-02	•	0.58216-09	0.5821E-09 -0.8599E-01 -0.1559E 00	-0.1559E 00
••	0.	٥.	•0	•0	•	• 0	•0	•0
0.000.0	0.0776	9.1407	-0.0776	0,000	• •	0.92 JBE 03	0.3033E 01 -0.1673E 01	-0.1673E 01
-6.0783	-0.000	0.0236	0000000	-0.0783	•	0.0033	0.9061E 03	0.1008E 02
-0.1410	-0.0234	0000-0-	0.0234	-0.1410	•	-0.0018	0.0111	0.9188E 03
SI GMA 500.0000	200.0000	200.0000	0.0365	0.0365	ò	30.3947	30.1009	30.3114
TRAJECTÚ TIME 0.	KY V ARIABLE 30	559. . 555	Y -18112597. LONG -80.578	2 9991646. ALT -1.10	×	XDOT Y0OT 1320.79 21 VEL FP 1338.85 -0	9.17 A .000	2007 0. A2 90.000

C-2. Test Case 1 (Continued)

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CASE
TEST
RM 2
4
BLDG
900
COHN
1/11/65

ITP DISPERSIONS EVAL 1.

	700	0.0-	0.1	4.9	-0.0	9.0-	-30.0	•	°,	٠٥-	ဝို	•0-	•	0.0-	6.0-	-40.0
	000	0.0-	6.0-	0.0	29.5	5.1	1.0-	ċ	•	•	•	•	•	39.3	7.6	-0.5
	XOO	-0-0	-4.8	7.0	-5.3	29.4	9.0-	9	ဝှ	•	•0-	• •	٥-	-7.6	39.3	-0-8
	200	-0.00	-0.08	-0.01	2.78	-1.22	0.03	-0.00	-0.03	-1.24	-0.00	-0.04	0.0	2.03	-0,40	0.01
	DVY	0.64	-0.01	-0,49	-0.00	90.0	2.74	1.36	0.25	-0.01	10.1	0.39	00.0	00.0	0.04	2.03
SYSTEM LH	DVX	-0.03	0.02	0.01	-0.00	-0.04	-1.75	-0.25	1.21	-0.03	-0.13	1.88	00.0	00.0	-0.02	-0.19
COORDIMATE S	740	-0-	505	-17.	519.	-387.	80	9	-5.	-252-	•0-	<b>.</b>	•	283.	-110.	2.
Ü	OPY	617.	<u></u>	ဝ	-0-	12,	458.	263.	° 64	-1-	282.	69.	•	·0-	•	7997
400.000	0.0	-101-	18.	514.	-2.	-11.	-481.	-50.	248.	-5.	-53.	350.	•	-1-	-4-	-162.
=74[]		10-1710	0112-01	0113-01	0131-01	0132-01	0133-01	1)-1004	A002-01	A003-01	A011-01	A012-01	A013-01	6901-01	6002-01	6063-01

C-2. Test Case 1 (Continued)

2007 -2034.31 A4 97.069	DOT 6120.72 FPA 1.289	>	xDOT :9573.37 VEL 20608.70	2 10008745. ALT 96.25	Y -17659617. LONG -69.848	660. T .751	VAR I AB	TRAJECTOKY TIME 400.000
50.242	50.00	50.2341	3.8735	4.1029	3 3.3283	2 909.7613	945.3012	SIGMA 900.3628
0.2524E 0	000000	00000-0-	-0.0004	-0.8039	0.5026	-0.0007	-0.5131	0.5185
0.2831E-0	0.250lE 04	0.0018	0.7830	000000	-0.0504	0.5031	-0.000	-0.0020
-0.5433E-0	0.4543E 01 -0.5433E-0	0.2523E 04	-0.4254	0.0004	-0.0005	-0.5089	0.0018	-0.0007
-0-3116-0	0-1517E 03 -0.7511E-0	0.1500E 02 -0.8278E 32	0.1500E 02	-0.0017	-0.0104	0.7934	-0.0026	-0-0111
-0.1657E 0	0.254(E-03 -0.1657E 0	0.8864E-01	0.1683E 02 -0.2700E-01	0.1683E 02	-0.4152	-0.6006	0.8281	0.5028
9.8404E U	-0.61476-01	0.1108E 02 -0.5670E 01 -0.1340E 00 -0.7776E-01 -0.6147E-01 9.8404E U	-0.1340E 00	-0.5670E 01	0.1108E 02	-0.0058	-0.2939	0.8046
-0.3288E 0	0.2289€ 05 -0.3288E 0	-0.2326E 05	0.2796E 04	-0.2355E 01	0.8277E 06 -0.1763E 02 -0.2355E 01 0.2796E 04 -0.2326E 05	0.8277E 0	-0.0018	-0.0063
-3.2437E 0	-0.7200E 00	0.9524E 02	-0.9533E 01	0.3212E 04	0.8936E 06 -9.1591E 04 -0.9245E 03 0.3212E 04 -0.9533E 01 0.8524E 02 -0.7200E 00 -3.2437E 0	6 -0.1591E 0	0.8936E 0	-0-3689
0.2346€ 0	-0.9187E 02	0.2411E 04 -0.1858E 04 -0.3865E 02 -0.3253E 02 -0.9187E 02	-0.3865E 02	-0.1858E 04		0.8107E 06 -0.3140E 06 -0.5684E 04	-0-3140E O	0.8107E 06
700	<b>D0</b>	<b>DOX</b>	7,0	AAQ	DVX	740	NPY	N & Q
							COVARIANCE MATRIX	COVARI
	295	TRAJECTORY TAPE 562		SIONS EVAL 1	IIP DISPERSIONS EVAL 1. COORDINATE SYSTEM LH		000*00+	11ME=

C-2. Test Case 1 (Continued)

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CASE
TËST
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RM 2
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BLDG
DOE
N O
11/11/65

PAJECTURY TAPE 562

IIP DISPERSIONS EYAL 1.

O

		0.0																		
		0-0-																		
	7.00	0.30	0.0		77.0	-2.44	3.0	44.	P • • •	99.0	10.0	50.		P+-0	0.01	-0.0	1.78		<b>9</b> .0	•
	DVY	-0-13	0.05		* * * * * * * * * * * * * * * * * * * *	-1.32	0.52	-2.Al		07.1-	0.19	4 C		A	0.29	-0-02	70.0-		0.15	60
SYSTEM ECI	DVX	0.18	0.01	F - 0-		91.0	#0.0-	-0-74		77.0	1.23	-0.10	71.0		AR - T	0.0	27.0		20.02	20.0
COORDINATE	740	298.	-++-	-41	-484	• • • • • • • • • • • • • • • • • • • •	940	250.	130		-	222.	137	,	•	÷	- 249.		3	(3) Fin
	DPY	-53	- NAV	170.	-24.7			-532.	-212		o o	119.	-248	F	: .	•	-135.	**		-2113
400.000	Dex	. BOI	•	463.	38.	4	9	-305-	40.		***	-50-	<b>63</b> °	167	****	:	16.	Q.		-60.
1186		10-1710	10-2110	0113-01	6131-01	1016410	10-3610	10-5610	A001-02	10000	10-7064	4003-01	A011-01	A012-01		10-6104	10-1009	C00261		10-500

Test Case 2 (Continued) C-2.

			90	90	6	70	63	5	5	~	*	27.	
		700	-0.1166E	-0.3037E	0.5979E 03	-0.1715E 02	-0.1607E	0.5805E 01	-0.1673	0.1008€	0.2519E 04	50.1675	2007 -2034.31 A2 97.069
295		Ana	-3.8116E D4	0.8318E 04 -0.6158E 03 -0.3037E	0.2756E 05	-0.2032E 02	0.2257E 02 -0.5700E 01 -0.1607E 03	0.1733E 03	0.3033E 31 -0.1673E 01	0.2506E 04 0.1008E 02	0.00.0	9090*09	0.72 A -289
TRAJECTORY TAPE 562		00x	0.1134E 04 -0.6439E 03 -0.4827E 32 -3.8116E 04 -0.1166E 05	0.8318E 04	0.1189E 05	0.2203£ 01 -0.1481E 01 -0.2574E 03 -3.2032E 02	0.2257E 02	0.1982E 02	0.2524E 04	0.9612	-0.0007	50.2378	*
		7AG	-0.64395 03	0.3763E 04 -0.4983E 03	0.3022E 04	-0.1481E 01	0.1881E 02 -0.1890E 01	0,1593E 02	5860.0	0.8677	0.0290	3.9908	X6UT 19573.37 VEL 20608.70
TIP DISPERSIONS EVAL L. DINATE: SYSTEM LGI		άΛά	0.1134E 04	0.3763E 04	-0.4451E 03	0.2203E 01	0.1881E 02	-0.1092	0.1036	-0.0263	-0.3303	4.3367	1000d745. ALT 96.25
COORDINATE SYSTEM		DVX	0.1633E 04	0.3043E 03	0.8739E 06 -0.2265E 03 -0.4451E 03	0.8181E 01	0.1176	-0.129я	-0.0016	-0.1419	-0-1195	2.8603	Y -17655677- LO36 -69.848
		740	0.1905E 06 -0.1095E 06	0.2034E OT -0,9346E 05	0.8739E 06	-0.0824	-0.1098	0.8101	0.2532	0.6316	0.0127	934.8287	660. T •75.
400-000	COVARIANCE MATRIX	3.40		0.1034E 07	-0,1038	0.1046	0.8535	-0.1228	0.1629	-0.0121	-0.5951	1016.7356	VAR I AB
TIME=	COVARIA	06	0.6243E 06	0.2371	-0.1483	0.7227	0.3310	-9.2042	-0.0012	-0.2052	-0*5340	SIGMA 790.097	TRAJECTUKY TIME 400,000

G-2. Test Case 1 (Continued)

11/11/65 JOHN DOE BLDG N 64 RM 2 TEST CASE 1

IIP DISPERSIONS EVAL 1.

	700	-0.0	٠.	<b>6.</b>	0.0	-0-1	-30.0	ခဲ့	Ģ	ò	o o	o ·	•	0.0	6.0-	٠-04-
	DOY	0.0	-2.6	0.1	55.4	16.0	-0-3	•	•	•	•	•	•	33.8	21.3	-0- &
	X00	0.0-	-4.2	1.0	-16.0	25.4	9.0-	•	°	•	o o	0	•	-21.3	33.8	-0-1
	DVZ	-0.00	-0.34	-0.00	2.21	-0.89	0.02	00.0	-0.02	-0.97	0.0	-0.03	0.03	1.67	-0-30	0.01
	000	1.41	00.0	-0.51	-0.00	0.07	2.91	1.76	0.86	-0.02	1.41	1.31	0.0	00.0	0.05	2.29
SYSTEM LH	DVX	-0.27	0.01	-0.09	-0.00	-0.05	-2.23	-0.10	0.78	-0.02	-0.51	1.22	0.00	0.0	-0.03	-1.33
COORDINATE ST	240	9	423.	-21.	1488.	-191-	18.	•	-12.	-682.	ô	-22.	24.	1001	-247.	•
บั	DPY	905	7.	•	-2.	28.	1146.	767.	412.	-6-	663.	616.	•	•	20.	907.
780.710	XAC	-432.	21.	*66*	-2.	-36.	-1563.	-423	565.	-12.	-356-	849.	ċ	1	-17.	-196.
11 ME =		0111-02	0112-01	0113-01	0131-01	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	6001-01	6003-01	6003-01

C-2. Test Case 1 (Continued)

50.2428 0.1094E 02 -0.9454E 01 -0.6547E-01 -0.6920E-01 0.4304E-01 0.1195E 03 0.1912E-01 -0.1816E 03 0.1656E-02 0.2567E 04 -0.2632E-02 0.8127E 05 0.5945E 02 -0.2583E 01 -0.7065E 05 0.6239E 04 -0.7548E 05 0.5251E 05 -0.5899E 02 0.9278E 02 -0.5414E-01 0.2524E 04 2007 -7178.12 20 0.7468E 04 -0.6768E 04 -0.5777E 02 -0.5436E 02 -0.8157E 02 0.1398E 02 50.0691 -0.000 DCY YDOT 14903-67 TRAJECTORY TAPE 562 0.2711E 02 -0.7763E-01 0.2777E-01 50.1740 0.9586E 01 -0.1023E 03 0.2517E 04 0.0044 0.0000 DOX XDOT 13745.86 0.5293E 07 -0.2464E 05 -0.3740E 04 0.1179E 05 -0.4233E 02 3.0961 -0.0003 -0.6584 0.5985 200 IIP DISPERSIONS EVAL 1. COORDINATE SYSTEM LH 0.4540E 07 -0.3905E 02 -0.4349E 02 8237621. ALT 5.2069 0.0001 -0.0048 -0.6940 0.0001 **0** 3.3070 -13609586. Long 0.0003 -0.5490 0.7193 -0.0064 -0.0004 ρVΧ 0.5494E 07 -0.2639E 07 -0.3490E 05 2130.7428 0.4922 -0.0039 -0.0055 -0.7060 -0.0006 0.9457 **240** 13544742. TRAJECTORY VARIABLES. 780.710 2300.6896 COVARIANCE MATRIX -3.0050 -0.0059 0000€ -0.0000 -0.6112 -0.4916 0.9845 DPY 780.710 S1GMA 2343.9505 0.6897 -0.4894 -0.0970 0.9635 0.0080 0.0005 -0.0007 -0.5545

Test Case 1 (Continued) C-2.

107-160

FPA

VEL 21507.98

-3.49

-48.399

23.220

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	:
ASE 1	S EVAL
TEST CASE	DISPERSIONS
RH 2	11P 01SF
3LDG N 64	_
00E BL	
NHOP	
1/11/165	

	700	0.0	0.0-	-4.3	14.3	•	79.4	•	•	ó	<b>.</b>	<b>.</b>	•	19.1	ċ	35.1	
	ADO	0.0	-0.8	-2.3	-26.0	<b>6.</b>	14.1	•	ċ	•	•	ċ	•	-34.7	6.5	18.9	
	DOX	0.0	6.4-	<b>*</b> •0	4.3	59.6	-2.3	ċ	ċ	ċ	ċ	ċ	ċ	5.8	39.5	-3.1	
	7/0	0.63	0.30	-0.17	-1.94	0.82	1.73	9 <b>9.</b> 0	0.15	0.85	69.0	0.22	-0.03	-1.46	0.29	1.26	
	DVV	-1.08	0.17	0.28	-1.05	0.35	-3.22	-1.56	-0.09	94.0	-1.22	-0.12	-0.02	-0.79	01.0	-2.28	
SYSTEM ECI	DVX	0.11	-0.01	-0.39	0.12	-0.04	0.20	19.0	1.14	-0.08	0.52	1.17	00.0	0.10	-0-01	94.0	
OURDINATE S	240	474.	-374.	-117.	-1307.	720.	860.	417.	22.	598.	359.	32°	-21.	-879.	229.	568	
J	DPY	-844	-193.	305	-707-	339.	-1679.	-149.	73.	322.	-645.	112.	-111-	-475	96	-1064.	
780.710	X	259.	***	378.	82.	-54	-643-	176.	6969	-54-	157.	1042	2.	57.	-14.	-16.	
TIME=		10-11-0	0112-01	0113-01	10-1410	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	5001-01	10-2005	2003-01	

C-2. Test Case 1 (Continued)

TIME	780	780.710	_	Š	IIP DISPERSIONS EVAL I. COORDINATE SYSTEM ECI	RSIONS	EVAL		7	IRAJECIORY TAPE 562	APE	295	-	
COVARI	COVARIANCE - MATRIX	X												
DPX	DPY		240		DVX	044		7.00		00X		¥00	700	
0.2803E 07		90	0.4236E 06 -0.2928E 06	90	0.4102£ 04		9E 03	-0.1398	0	-0.4624E	03	0.1539E 03 -0.1398E 03 -0.4624E 03 -0.1196E 05 -0.1163E		90
0.0941	0.72326	01	-0.1424E	01	0.7232E 07 -0.1424E 07 -0.2512E 04		8E 05	0.1308E 05 -0.3854E 04	E 0		0.5	0.1630E 05 -0.7251E 04 -0.1022E 06	-0.1022E	80
-0.0760	-0.2302		0.5292E 07	10	0.1287E 04 -0.3695E 04 0.8322E 04	-0.369	SE 04	0.8322	9	0.1765E 05	90	0.9293E 05	0.75976 04	\$
0.8448	-0.3220		0.1929		0.8411E 01 -0.5696E 01	-0.569	6E 01		E 0	0.3120E 01 -0.2515E 01	0	0.5912E 01	0.2734 02	2
0.0165	0.9769		-0.3228	·	-0.3946	0.247	7E 02	0.2477E 02 -0.8596E 01	О		05	0.1898E 02 -0.3238E 02 -0.196:		80
-0.0220	-0.3769		0.9516		0.2830	-0.4543	Ŵ.	0.1445E 02	E 0.	0.9507E 01	10	0.1556E 03	0.347% 02	02
-0.0055	0.1206		0.1527	·	-0.0173	0.0759	6	0.0498		0.2524E 04	ő	0,33336 01 -0.16736	-0.1673E	70
-0.1427	-0.0539		0.8069		0.0407	-0.1300	0	0.8176		0.0012		0.2506E 04	0.1008E 02	20
-0.1383	-0.7571		0.0658		0.1878	-0.7866	ø	0.1823		-0.0001		0*00*0	0.2519E 04	*
51GMA 1674.3517	7 2689-2147	147	2300.4373	573	2.9002		4.9768		3.8318	3 50.2378	378	50.0606	50.1875	. 22
TRAJECTO TIME 780.7	RY VARIA 10	8LES 1354	BLES. 1354742. LAT 23.220	7,	Y -13609586. LDNG -48.399	823	2 8237621. ALT -3.49		XD0T 13745 VEL 21507	XDOT 13745-86 VEL 21507-98	7007 1490 FP	YDOT 14903.67 FPA -4.708	2007 -7178.12 A2 107.160	

C-2. Test Case 1 (Continued)

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IAPE 302	ALT	QH	4523.	20.	499.	20.	,02.	47.2.	3777.	2823.	-76.	3274.	4221.	m	22.	85.	4170.	
INAJECIUNT IAPE 302	CRITERION	HC.	•	422.	-31.	1468.	-196.	50.	•	-27.	-681.	9	-40.	24.	1000	-247.	~	
il distensions eval 1.	780.710	R	0.249	0.002	0.000	-0.00	0.008	0.316	0.211	0.114	-0.002	0.183	0.170	0.00	0.00	0.005	0.250	
	TIME		10-1110	0112-01	0113-01	0131-01	C132-01	0133-01	A001-01	A002-( 1	A003-01	A011-01	A012-01	A013-01	G001-01	6002-01	6003-01	

C-2. Test Case 1 (Continued)

COVARIANCE MATRIX

MT 0.402382E 00 0.833867E 01 0.726621E 04
MC 0.00617 0.454193E 07 0.110958E 06
MD 0.98446 0.00447 0.135389E 09

NOMINAL TERMINAL CONDITIONS

11636.

2131.

0.634

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LAT LONG ALT VEL/R FPA/R 23.220 -48.399 -3.49 20194.793 -10.346

AZ/R 108.351

C-2. Test Case 1 (Concluded)

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11/11/65 JOHN DOE BLDG N 64 RM 2 TEST CASE 2

ORBIT DISPERSIONS EVALU 2 TARJECTORY TAPE 562

11.ME=	•	J	OURDINATE	SYSTEM LH					
	×20	7.00	740	DVX	<b>A</b> A0	0 0 2	XCO	<b>00</b>	700
10-1110	ċ	. 500°		0.03	-0.00	•	-0.0	•	0.0
0112-01	ċ		500.	0.02	-0.00	-0.00	6.4-	0.0-	0.0
10-6110	500.	·0- //		-0.00	-0.03	-0.05	0.0	0.0	<b>6.</b>
10-1610	3	• •		•	ò	ė,	0.0	30.0	0.0
0132-01	•	•		•	<b>.</b>	ó	0.0	-0-0	30.0
0133-01	•	•		•	°	ó	30.0	0-0-	-0.0

C-3. Test Case 2

700	-04 0.2467E 04	0.9367E-06 -0.3422E-05 -0.5521E-05	0.2980E-07 -0.2467E 04 -0.3287E-05 -0.6692E-05	0.9035E-12 -0.8599E-01 -0.3544E-09 -0.4935E-09	0.7586E-10 -0.9313E-09 -0.1580E 00	-0.8599E-01	0.5962E-06 -0.1096E-05	0.900CE 03 -0.1144E-04	0.9243E 33
¥00	-0.1526E	-0.3422E	-0.3287E	-0.3544E	-0.9313E	•		0.900CE	-0~0000
X00	0.2630E-05 -0.1526E-04		-0.2467E 04	-0.8599E-01	0.7586E-10	0.3037E-03 -0.1693E-10	0.9243E 03	0.000.0	-0.0000
7.0	-0.8714E 01	0.4470E-07	0.2980E-07	0.90956-12	0.55816-03	0.3037E-03	-0*0000	•0	-0.1623
AAO	-0.1601E 02	0.5960E-07	0.2980E-07	<b>0</b> ,	G.1026E-02	1.0000	000000	-0.000	-0.1623
DAX	-0.8941E-07	0.1601E 02	0.8714E 01	C.1329E-02	0.	000000	-0.0776	-0.000	-0.000
0P.	-0.1327E-02	0.2500E 06 -0.9766E-03	0.2500E 06	0.4780	0000.0	0.000	-0.1623	0.000.0-	0000-0-
DPY	.2500E 06 -0.1305E-02 -0.1327E-02 -0.8941E-07 -0.1601E 02 -0.8714E 01	9.2500E 06	-0.0000	0.8784	0.000	0.000	0.000	-0.0000	-0.0000
XdQ	.2500E 06	0000*0-	0000-0-	-0.0000	-1.0000	-1.0000	0000.0	-0.0000	0.1623

200.0000	200.0000	200-0000	0.0365	0.0320	0.0174	30.4030	30.0000	30.4030
TRAJECTORY	TRAJECTORY VARIABLES.							
TIME	*		>	. 7	XDUT	YDOY		1001
• •	3005559	•	-18112597.	9991646.	1320.79	219-17		•
	LA		LONG	ALT	YEL	¥d±		A2
	28	28.555	-80.578	-1.10	1338.85	- 0		000.06

C-3. Test Case 2 (Continued)

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CASE
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CREFT DISPERSIONS EVALU 2

	<b>,</b> 00		•	- ·	•	0.0-	30.0	4		•	5	•	-	· •	•	•	0.0-			-40.0
	AUG				•	< *.62	٦.			•	•	9	ć	, ,	•	•	39.3	•	•	-0-5
	XOO	6.0		•	•	1-2-1	9.0	707		<b>,</b>	•	•	-0-	, -	•	•	9.1-	6 5		8.0-
	DV2	-0.00	90.0-			9	-0.03	-1.22	00.0-		N (	-1.24	00.0-	-0.04	40.0	•	2.03	4.0-		10"0
	A A Q	0.64	-0.0	10.0			-2-14	90.0	1.36	20.0		10.0-	10.1	0.39	00.0		00.0	40.0	•	2.03
SYSTEM LH	DVX	-0.03	0.02	0.0			1.73	+0.0-	-0.25	1.21		50.01	-0-18	2 · 88	00.00		00.0	-0.02	3 (	£1.0-
COORDINATE	240	°	505.	-11.			• • •	-387.	-0-	-5-	10801	-202-	ġ	•	6		.683	-110.		;
	<b>A</b>	617.	-	ò	0-	444		12.	263.	<b>4</b>	-		282	69	•	•	•	÷	777	• 907
+000.000	UPX	-101-	18.	514.	-2.				•05 ·	248.	•		-53.	350.	•	•	:1-	-4.		. 701-
11ME.		10-1116	10-2110	10-1110	0131-01	01840	10-2610	(0133-0)	A001-04	A002-01	10-1004	40000	TC-TUDY	A012-01	A013-01	10.1000	10-1009	600201	10-1000	10-6000

C-3. Test Case 2 (Continued)

1186	400.000	6	ກອວ	COGLDINATE SYSTEM	N X	ORBIT DISPERSIONS EVALU Z DINATE SYSYEM LM			TRAJECTORY TAPE SAZ	N & & & & & & & & & & & & & & & & & & &		
COVARIA	COVARIANCE MATRIX											y.
DFX	<b>A40</b>	740		XAC		<b>AA0</b> .	ENZ		<b>200</b>	AOO		700
11 J7E 96	0.81)7E 06 -0.3140E 06 -0.5684E	-0.5684E	\$	0.2411E	*	-0.1958E 34	4 -0.3865E	05	-0.32536 02	0.2411E 04 -0.1858E 34 -0.3865E 02 -0.3253E 02 -0.9187E 02		0.2346E
6898"0-	0.8936E 06	-0.1591E	- 40	0.9245E	80	0.32126 0	4 -0.9533E	5	0.8524E 0;	0.8936E 06 -0.1591E 04 -0.9245E 03 0.3212E 04 -0.9533E 01 0.8924E 02 -0.7201E 00 -0.2437E	٥	0.2437
-6900-0-	-0.0018	0.827,5	90	0.1763E	20	-0.2355E 0	1 0.2796E	6	-0.2326E as	0.827/C 06 -0.1763E C2 -0.2355F O1 0.2796E O4 -0.2326E 35 0.22896 OS -0.3208E C		0.320BE
0.8046	-0.2939	-0.0058		0.1108E (	20	-0.5670E 0	1 -0.13406	8	-0.77766-01	0.1108E 02 -0.5670E 01 -0.1340E 00 -0.7776E-01 -0.6147E-01		3+0+8-0
-0.5028	0.3281	-0.0006		-0.4152		0.1683E 0	0.1683E 02 -0.2700E-01	10-	0.88646-01	1 3.2556E-03 -0.1657E 0	ī ē	0.1657E
-0.0111	-0.0026	0.7934	ı	-0.0104		1100.0	0.1500F	70	G.1500F UZ -0.8278E 02	0.1517E 03 -0.7511E-0	. <u></u>	0.7511E-
-0.0007	0.0018	-0.5089	,	-0.0005		<b>0</b> •000	-0.4254		0.2523E 04	0.4543E 01 -0.5569E-0	i .ge	0.5569E-
-0,0020	-0.0000	0.5031	•	-0-0004		0000°C	0.7830		0.0018	A.2501E 04		0.36236-0
0.5185	-0.5131	-0.0007		0.5026	·	-0.803\$	-0.0004		-0.000	000000	_	0.2524E (
S16MA 900.3628	945.3012	909.7613	13	3,3283	83	4.1029		3.8735	50.2341	9000*05	30	50.243
TRAJECTORY TIME 400.000	VARIAB	LES. X 7071665. LAT 27.751	-17	Y -17659617. LONG 69.348		2 10008745. ALT 96.25		XDDT 19573.37 VEL 20608.70	>	YDOT 6120.72 FPA 1.269	<b>4</b> 1	-2034.31 -2034.31 A2 97.009

C-3. Test Case 2 (Continued)

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		700	9	6.4	-0.0	30.0	•-0-	•	•	0	o o	9	0	0.0-	6.0-	-46.5
		<b>604</b>		0.0	23.0	0.2	7.7	•	ô	Ó	•	•	ó	44.0	11.9	-0-3
DRY TAPE 562		00x		7.0	-7.7	••	29.0	-0-	•	-0-	-0-	Ģ	•	-11.9	4.0	•••
TRAJECTORY		200	-0-15	-0.01	3.30	-0.02	-1.03	00.0-	-0.03	-1.42	-0.00	-0.03	0.05	2.95	-0.17	0.00
NS EVALU 2		DVV	0-0-	-0.60	0.00	-3.38	0.07	1.60	0.40	-0.01	0.95	9.64	00.0	00.0	0.05	3.01
ORBIT DISPERSIONS	SYSTEM LH	DVX	0.0	00.0	-0.00	1.90	-0°0-	-0.39	1.37	-0.03	-0.21	2.24	0.00	10.0	-0.02	-0.94
1880	COORDINATE S	740	497.	-17.	717.	-9-	-461.	ę	-7.	-336,	÷	-10.	12.	+	-130	<b>.</b>
	_	DPV	7.	•	-	-616-	15.	354.	•06	-2-	341.	130.		Ģ	•	412.
	+99.494	DPX -148.	17.	514.	-3.	635.	-13.	-16-	327.	•	-17.	476.	•		-5.	-241.
	TIME=	0111-01	0112-01	10-6110	0131-01	0132-01	0133-01	A001-01	AD02-01	A003-01	10-110V	A012-01	A913-01	10-1009	10-2005	6003-6E

C-3. Test Case 2 (Continued)

TEME	494	464.664	ھ	Ö	ORSINATE	SYS	ORBIT DISPERSIONS EVALU 2 COORDINATE SYSTEM LH	<b>1</b>		4	TRAJECTORY TAPE 562	<b>U</b>	295		
COVARI	COVARIANCE MATRIX	×													
DPX	A d O		240		X A Q		AA.Q		200		X00		DOA		<b>70</b> C
0.1261E 07	0.5463E	90	-0.1003E	05	0.3727E	40	-0.3001£ (	. 40	-0.5629E	02	-0.37936	20	0.1261E 07 -0.5463E 06 -0.1003E 05 0.3727E 04 -0.3001£ 04 -0.5629E 02 -0.3793E 02 -0.1510E 03	6	G. 3280E
-0-4151	0.1374E	01	-0.4065E	40	-0.1312E	40	0.5319E (	. 40	-0.1835E	20	0.1475E	03	0.1374E 07 -0.4065E 04 -0.1312E 04 ().5319E 04 -0.1835E 02 0.1475E 03 -0.9755E 00 -0.3751E 0	8	-0-3781E
8:00°0-	-0.0030		C.1295E	0	-0.2711E	20	-0.5953E (	<b>TC</b>	0.4605E	*	-0.32336	90	C.1295E D# -0.2711E O2 -0.5953E O1	2	-0.369€€
0.8652	-0.2916		-0.0052		0.1474E	0.5	0.1474E 02 "0.7598E 01 -0.1547E 00 -0.8109E-01	- 10	-0.1547E	00	-0.8109E-	.01	0.2053E 00 0.1005E 0	9	0.10056
-0.5121	0.8694		-0.0010	•	-0-3793		0.2724E (	- 20	-0.4491E-	70	0.2724E 02 -0.4491E-U1 -0.1219E 00	00	0.2707E-02 -0.244E 0	. 20	-0-244E
-0.0104	-0.0033		0.8409	•	-0.0084		-0.0018		0.2316E	05	0.2316E 02 -0.9783E 32	20	0.2205E 03 -0.6797E-0	9	-0.6797E-
-0.0006	0.0023		-0.5117	•	-0.000%		-0.0004	•	-0.3662		0.3082E D4	5	0,6040E 01 -0.3426F-0	7	-0.3426E-
-0.0024	-0.0000		0.5538		0.0010		000000		0.8283		0.0020		0.3061E 04	*	0-1276E-0
0.5262	-0.5777		-0.000%		0.4716		-0.8424	•	-0.0003		-0.0000		0.0000		0.3083E 0
SIGHA 1122, 7529	1172,2344	344	1136.1323	123	3.8387	18	5.2189	6	4.8121	21	55.5146	9	55.3239	5	\$5.52
TRAJECTORY Time \$64.664	TRAJECTORY VARIABLES.  TIME RATE  \$64.664  LA	84.58 844 1	LES. X 84418. LAT 27.202	7	Y -17166351. LONG -65.748		2 9832986. ALT 98.58	* 40 40 13	XD0 231 252	XDOT 23153.78 VEL 25212.21	78	YD07 934 FP	DUT 9347.12 FPA 0.077		2001 -3491.33 A1
			1 - 1 - 1					,	1						:

C-3. Test Case 2 (Continued)

ORBIT DISPERSIONS EVALU 2 TRAJECTORY TAPE 3 PARTIALS AT T= 477.664 WITH RESPECT TO T= 464.664 TRANSITION MATRIX.

2001 - 1992 - 1994 - 1994 - 1996 - 19	9347.12 9461.63 FPA 0.077	<b>*</b>	XDOT 23153-76 22995-75 VEL 25214-21 25211-77	2 9832988. 9785427. ALT 98.58	V -17166351. -17042791. LONG -65.748 -64.834	.18. 96. 202 063	Y VARIABLE	TRAJECTUR 11ME 464-664 477-664 477-664
C. 1(100)	0.6519E-08 -0.1118E-07	0.6519E-08	•0-	•	-0-	• 0	-0-	•
0-83K8E-0	0.99996 30	0.1524E-01	<b>.</b>	•	ċ	ò	•	•
-0.2235E-01	0.9999E 00 -0.1524E-01 -0.2255E-01	0.9999E 00	-0-	-0-	-0-	-0-	-0-	•
ç	ċ	÷	0.9999E 00 -0.	0.6519E-08 -0.1118E-07	0.6519E-08	-0.18396-04	0.3979E-12 -0.1	-0.3979E-12
•0•	•	ė.	0.3725E-08 -0.	0.1524E-01 0.1000E 01	0.1524E-01	0.68216-12	0.3677E-04	0.14016-06
÷	•	-0-	-0,2421E-07 -	0.9998E 00 -0.1524E-01 -0.2421E-07	0.9998E 00	0.5400E-12	-0.1401E-06	-0.1839E-04 -0.1401E-06
	••	•	0.13006 02 -0.	0.1192E-06 -0.2384E-06	0.1192E-06	0.9999E 00	0.8382E-08 -0.1490E-07	0.8382E-08
÷	••	•	0,1300E 02 -6,1192E-06 -0.		0.1981E 00	•	0.1000E: 01	0.15246-01
0	ċ	-0-	00 -0.2682E-06 -	-0.1981E 00 -	0.1300E 02 -0.1981E	-0.2049E-07	0.9998E 00 -0.1524E-01 -0.2049E-07	0.9998E 00
7744	AINA	PHIX	1002	YDDT	XOOT	7	>	×
			SPECT TO	PHIZ MITM RE	PARTIALS OF X,Y,Z,XDOT,YDOT,ZDOT,PHIX,PHIY,PHIZ WITH RESPECT TO	DOT, YDOT, 200	S OF X.Y.Z.X	PARTIAL
						ГН	COORDINATE SYSTEM	CODROIN

C-3. Test Case 2 (Continued)

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		<b>200</b>	0.0	0.1	•	0-0-	30.0	900-	d.	Ģ	9	Ģ	o-	0-	0-0-		4-7-1	
		DOV	0.0-	-1-3	0.0	28.9	0.2	8		ć	0	ő	•	6	46.0	13.0	K .	•
ORY TAPE 562		XQQ	0.0-	-4-7	1.0	-8-1	9.0	28.9	0-	0-	0-	•	0-	0-	-13.0	46.0	6-0-	
TRAJECTORY		DV2	-0°0	-0-16	-0.01	3.37	-0.02	-1.02	-0.00	-0.03	-1,41	-0.00	-0.05	0.05	2.94	-0.17	00.0	
NS EVALU 2		AAG	0.77	-0.01	-0.60	00.0	-3.36	5.07	1.61	0.42	-0.01	96.0	0.68	00.0	00,00	0.05	3.0.5	1
ORBIT DISPERSIONS EVALU 2	SYSTEM LH	DVX	-0.08	0.01	00.0	-0.00	1.94	+0.0-	14.0	1.36	-0.03	-0.23	2,22	00.0	0.01	-0.02	-0.98	
ORBI	COURDINATE S	0P.Z	-1-	495.	-17.	760.	-6-	-414.	9	-7.	-357.	°0-	-10.	13.	479.	-132.	2.	
	J	DPY	.199	2.	ċ	-1-	-650.	16.	373.	100.	-2.	352,	146,	ċ	•	10.	447.	
	477.664	DP.X	-159.	18.	514.	-3•	670.	-14.	-102.	342	-7-	-66-	502.	°	-;-	-5.	-260.	
	TIME*		10-1110	0112-01	0113-01	0131-01	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	10-1005	6002-01	6003-01	

C-3. Test Case 2 (Continued)

TIME*	417.664	49	ORBIT DISPERSIONS EVALU 2 COORDINATE SYSTEM LH	SYSTEM	S EVAL LH		TRAJECTORY TAPE 562	TAPE	295	
COVARIA	COVARIANCE MATRIX									
X dQ	DPY	240	DVX	DVV		DVZ	DOX		ASQ.	700
0.13786 07	0.1378E 07 -0.6059E 06 -0.1107	6 -0.1107E 05		04 -0.314	7E 04	0.3965E 04 -0.3147E 04 -f.5780E 02 -0.3896E 02 -0.1532E	2 -0.3896	E 02	-0.1532E 03	0.3506E 05
-0.4215	0.1499E 0	0.1499E 07 -0.4559E	04 -0.1426E	40	9E 04	0.5659E 04 -3.1974E 02		E 03	0.1468E 03 -0.9672E 00 -0.4085E	-0.4085E 05
-0.0079	-0.0031	0.1419E	07 -0.2881E 02 -0.7141E 01	02 -0.714	1E 01	0.4880E 04 -0.3450E 05	4 -0.3450	E 05	0.3777E 05	0.3777E 05 -0.3777E 02
0.8770	-0.3025	-0.0063	0.1483	02 -0.778	3E 01	0.1483E 02 -0.7783E 01 -0.1524E 00 -0.818&E-01	0 -0.818	E-01	0.2150E 00	0.10496 03
-0.5121	0.8828	-0.0011	-0.3861	0.274	1E 02	0.2741E 02 -0.4783E-01 -0.1246E 00	1 -0.1246	E 00	0.41106-02	0.4110E-02 -0.2479E 03
-0.0103	-0.0034	0.8547	-0.0063	-0.0019	6	0.2298E 02 -0.1018E 03	2 -0.1018	E 03	0.2219E 03	0.2219E 03 -0.6725E-01
9000*0-	0.0021	-0.5118	-0.0004	-0.0004	•	-0.3752	0.3204E 04	<b>1</b> 0 <b>1</b> 0	0.6359E 01	0.6359E 01 -0.3613E-02
-0.0023	-0.0000	0.5620	0100.0	0.000	0	0.8205	0.0020	_	0.3183E 04	0.1268E-01
0.5275	-0.5893	-0.0006	0.4811	-0.8364	*	-0.0002	-0.0000	_	0000.0	0.3206E 04
516NA 1173.9390	1224.456:	1191.0600	3083.68.00		5.2351	4.7939		56.6055	56.4218	56.6213
TAAJECTORY TIME 477.664	VARIAB	LES. 8744396. LAT 27.063	Y -17042791. LONG -64.834	9.6 V	2 9786427. ALT 98.62	XDOT 22995.75 VEL 25211.77	5.75 1.77	00Y 966	001 9661.63 FPA 0.052	2007 -3471.75 A2 99.439

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C-3. Test Case 2 (Continued)

	TRAJECTORY TAPE 562
BLDG N 64 RM 2 TEST CASE 2	ORBIT DISPERSIONS EVALU 2
BLDG N 64 RM	0881
JOHN DOE	
11/11/05	

	<b>7</b> 00	0.0	0.1	4.9	0.0-		0.00	9.0-	-0-		י	• •	•		•	•	0.0-	) (	0.1-	R-04-	
	DOV	0.0	-1.5	0.0	7.80		7.0	<b>.</b>	ď	;	; 5	•	•		;	ċ	47.4		7.4	4	
	DOX	-0.0	1.4-	0.1	- a	9 (	e. 0	28.7	Ç	<b>3</b> 1	•	ģ	-0-		•0-	•	-14.7		4.6	0	
	200	-0.00	-0.18	-0.03		7.5.57	-0.02	-0.99		0	-0.03	-1.47	00-0-		<0.0-	0.05		70.0	-0-13	•	•
	DVV	0.81	-0.01	19.0-			-3.42	0.07	4 4	7.00	84.0	-0.01	10.0		92.0	00.0		00.0	0.05		3.10
SYSTEM LH	DVX	-0.09	10.0			00.0-	2.00	<b>-0.04</b>			1.40	-0.03	70.0	+2.0-	2-25	00-0		10.0	-0.02	,	*0 • 1
COORDINATE	007	1	401		• • • • • • • • • • • • • • • • • • • •	830.	-6-	-404		-0-	-7-	-387.		• •	-111-		1	241.	-135.		<b>2</b> •
	VOO	473	· ·	• •	•	<del>-</del>	-703-	17.	• • • • • • • • • • • • • • • • • • • •	402.	118.	1		3.0	174.		•	-0-	- 11	•	503.
498.375	×	-117		•	514.	-4-	127.		-12	-120.	369.		• ( · ( · ( · ( · ( · ( · ( · ( · ( · (	-100.	565,		•	-1-	4	•	-292.
TIME			10-11-0	10-7110	0113-01	0131-61	10-22-00	10.00	10-6610	1001-01	4002-01		10-COOK	A011-01	4012-01	10.4	10-6104	6001-01	101600	10-2005	0003-01

C-3. Test Case ? (Continued)

			9	9	05	60	60	10-	-05	-0	S	191
		200	0.3894E 05	-0.4618E	0.4249E 05 -0.3903E 02	0.1119E 03	0.6534E-02 -0.2601E 03	0.2299E 03 -0.5551E-01	0.6856E D1 -0.4227E-02	0.1360E-01	C.3408E 04	58.3791
			03	8	9	8	-05	03	10	5		:
262		DOY	0.4416E 04 -0.3451E 04 -(.6133E 02 -0.4075E 02 -0.1544E 03	0.1519E 03 -0.8923E 00 -0.4618E		0.2580E 00	0.6534E		0.6858E	0.3386E 04	0.000	50.1994
<b>.</b>	_		05	03	0.5	10-	9	03	å			919
traječtgry tape 562		DOX	-0.4075E	0.1519E	0.5413E 04 -0.3822E 05	-0.8377E	-0.1525E	0.2367E 02 -0.1081E 03	0.3406E D4	0.0020	-0.0000	58.3610
7 4 4			05	05	6	8	-01	05				149
		240	-().6133E	TE 04 -0.1603E 04 0.633.E 04 -0.2258E 02		0.1549E 02 -0.8176E 01 -0.1520E 00 -0.8377E-01	0.2891E 02 -0.5384E-01 -0.1525E 00	0.2367E	-0.3807	0.8122	-0.0002	4.8647
YAL:			6	5	10	5	05					768
ORBIT DISPERSIONS EVALU 2 DINATE SYSTEM LH		DVV	-0.3451E	0.633.E	-0.9228E	-0.8176E	0.2891E	-0.0021	-0.0005	0.000	-0.8285	5.3768
SYS			5	5	02	05						25.0
COORDINATE SYSTEM		DVX	0.4416E	-0.1603E	0.1632E 07 -0.3163E 02 -0.9228E 01	0.1549E	-0.3863	-0.0079	-0.000	0.0011	0.4870	3.9358
Ö			90	8	01		•					120
		240	-0.1281E 05	-0.5557E	0.1632E	-0.0063	-0.0013	0128.0	-0.5127	0.5717	-0.0005	1277.4120
375	×		80	20				•				27.
498.375	COVARIANCE MATRIX	740	0.1584E 07 -0.7086E 06 -0.128	0.1715E 07 -0.555	-0.0033	-0.3110	0.8992	-0.0035	0.0020	-0.0000	-0.6040	1309.7279
	IR IA		03									NA 632
TIME	700	X 60	0.1584E	-0.4299	-0.0080	0.0916	-0.5100	-0.0100	-0.000	-0.0021	0.5301	\$16HA 1258.4632

C-3. Test Case 2 (Continued)

2007 -4016.04 A2 100.132

YEOT 10315.87 FPA 0.000

XDGT 23061.90 VEL 25581.19

2 9706828. ALT 98.62

7 -16835947. LONG -63.372

9221363. LAT 26.824

TRAJECTORY VARIABLES.
X TINE X 498-375

ORBIT DISPERSIONS EVALU 2 TRAJECTORY TAPE 562 PARTIALS AT T= 500.000 WITH RESPECT TO T= 490.375 3 TRANSITION MATRIX. COORDINATE SYSTEM

2144	-0-	-0-	-0-	-٥-	-0-	-0-	-0.4010E-05	0.1000E 01 -0.7451E-08	0.1000E 01	2007 -4015.04 -4036.29 AZ 100.132
PHI Y	•	•	•	••	•	•	0.1000E 01 -0.1932E-02 -0.4010E-05	0.1000E 01	-0.1863E-08 -0.3725E-08	YDOT 10315.67 10354.42 FPA 0.000
PHIX	-0-	•	-0-	-0-	-0.	-0-	0.1000E 91	0.19326-32	-0.1863E-08	
1007		-0.2235E-07	0.1625E 01	-0.40388-05	-0.7451E-08	0.1000E 01 -0.	-0-	•	-0-	XDOT 23061.90 23040.41 VEL 25581.19 25580.89
x y y xour your 20ur	0.1625E 01 -0.3139E-02 -0.6514E-05	9.1625E 01 -0.2235E-07 -0.	-0.1490E-07	0.1000E 01 -0.1932E-02 -0.4038E-05	0.1000E 01 -0.7451E-08	-0.1118E-07		•0	. 0-	2 9706828. 9700173. ALT 98.62 98.62
xout	0.1625E 01 -	0.3139E-02	-0.1863E-08 -0.1490E-07	0.1000E 01 .	0.1932E-02	•0	•0-	់	-0-	Y -16835937. -16818952. LONG -63.372 -63.257
7	-0.4008E-05	-0.74.1E-08	0.1000E 01 ·	0.9184E-11	-0.4263E-13	-0.2298E-05	•0-	•	•0-	63. 09. 805
>-	0.1000E 01 -0.1932E-02 -0.4008	0.1000E 01 -0.74.1	-0.1118E-07	-0.2220E-08	0.45965-05 -0.4263	-0.1421E-13	•0-	ċ	-0-	Y VARIABL 92 92
×	0.1000E 01	0.1932E-02	•6	-0.2298E-05 -0.2220E-08	0.2220	-0.3553E-14 -0.1421E-13 -0.2298		• 0	•0-	TRAJECTUR TIME 498.375 500.000 498.375

C-3. Test Case 2 (Continued)

RM 2 TEST CASE 2	ORBIT DISPERSIONS EVALU 2
÷	
2	
PLDG N 6.	
906	
<b>X</b>	
11/11/05	

TRAJECTORY TAPE 562

	700	9-	ö	•	9	30.	•	ė	ė	ė	ė	ė	ė	ė	-1-	-20	•	÷	•
	A00	9	5-7-	0.0	29.6	0.5	•••	ċ	ċ	ċ	ċ	•	ċ	47.1	14.1	-0.3	ċ	ċ	•
	<b>DOX</b>	-0.0	~*-	1.0	-8.9		28.6	ė	Ģ	ġ	ċ	ċ	ç	-14.8	47.7	-0-	÷	Ģ	•
	200	-0.00	-0-18	-0.01	3.39	-0.05	-0.99	-0.0°	-0.03	-1-47	00.0	-0.05	0.0	3.00	-0.13	9.0	9.0	00.	-0.00
	AAQ	0.61	-0.01	-0.61	00.0	-3.42	70.0	1.69	0.49	-0.01	0.97	0.76	00.0	00.0	0.0	3.10	2.00	00.0	0.00
SYSTEM LH	DVX	-0.09	0.01	-0.00	-0.00	2.01	+0.0-	-0.47	1.40	-0.03	-0.24	2.22	0.00	10.0	-0.02	-1.05	-0.00	00.0-	1.60
COORDINATE S	740		491.	-18	836.	-6-	-496.	•	•	-389.	•	-111-	14.	546.	-135.	2.	•	ò	•
J	<b>∆ 0 0</b>	674.	3.	•	-1-	-707-	17.	407.	120.	-3.	371.	176.	•	•	11.	508.	•	ં	ċ
200.006	N A	-176.	18.	514.	•	732.	-15.	-122.	371.	.7.	-110.	548.	•	-1-	•	-295.	•	ò	-0-
TIME		0111-03	0112-01	0113-01	0131-01	0132-01	0133-01	A001-01	A002-01	A003-01	A012-01	A012-01	A013-01	2001-01	<b>C005-01</b>	6003-01	1021-02	1022-02	1023-02

C-3. Test Case 2 (Continued)

TIME.	200.000		COORDINATE SYSTEM LH	ERSIONS EVAL		trajectory tape 56.2	6.46 6.46 6.46 6.46 6.46 6.46 6.46 6.46	
COVARI	COYARIANCE MATRIX							
X 40	Adu	2 40	DYX	DVV	2.00	00x	A00	700
0.1601E 07	5.7171E 06	-0.1296E 0	0.1601E 07 -0.7171E 06 -0.1296E 05 0.4447E 04 -0.3471E 04 -0.6153E 02 -0.4089E 02 -0.1543E 03	-0.3471E 04	-0.61532 02	-0.4089E 02	-0.1543E 03	0.3926E 05
-0.4305	0.1733E 07	-0.5634E 0	0.1733E 07 -0.5634E 04 -0.1619E 04	0.6377E 04	0.6377E 04 -C.2277E 02	0.1519E 03	0.1519E 03 -0.8831E 00 -0.4661E	-0.4561E US
-0.0080	-0.0033	0.1649E 0	0.1649E 07 -0.3185E 02 -0.9402E 01	-0.9402E 01	0.5447E 04	0.5447E 04 -0.3853E 05	0.4287E 05 -0.3914E	-0.3914E GZ
0.8653	-0.3026	-0.0061	0.1650E 02	0.1650E 02 -0.820iE 01 -0.1519E 00 -0.8592E-01	-0.1519E 00	-0-8392E-01	0,2583E 00 0.1125E	0.1125E 33
-0.3736	9659°C	-0.0010	-6.2749	0.5393E 02	-0.5422E-01	0.5393E 02 -0.5422E-01 -0.1518E GO	0.6753E-02	0.6753E-02 -0.2606E 03
-0.0070	-0.0025	2809.0	-0.0054	-0.0011	0.4854E 02	0.4854E 02 -0.1086E 03	0.2300E 03	0.2300E 03 -0.6541E-01
-0.0006	0.0020	-0.5128	+0000-0-	+0000*0-	-0.2662	0.3422E 04	0.69976 01	0.6997E 01 -0.1794E-01
-0.0021	0000-0-	0.5723	0.0011	000000	0.5655	0.0020	0.3402E 04	0.1360E-01
0.5303	-0.6031	-0.0005	0.4732	-0.6063	-0.0002	0000 -0-	000000	0.34246 94
S16MA 1265.2606	1316.5268	1284.2856	6 4.0623	7.3440	.416.9	56.4996	58.3272	58.5172
TRAJECTORY 11ME 500.000	VARIABLE 92	1709. 1	Y -16818952. LONG -63.257	2 9700173. ALT 98.62	XDDT 23040.41 VEL 25580.89		YDDF 10354.42 FPA 0.000	4036.29 -4036.29 A£ 100.167

C-3. Test Case 2 (Continued)

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ORBIT DISPERSIONS EVALU 2 TRAJECTORY TAPE 562
PARTIALS AT T\* 2000.000 WITH RESPECT TO T\* 500.000 IJ TRANSITION MATRIX. COURDINATE SYSTEM

PARTIAL	S OF X, Y, Z,	PARTIALS OF X.Y.Z.XDOT.YOOT.ZDOT.PHIX.PHIY.PHIZ WITH RESPECT TO	OT PHIX, PHIY	PHIZ WITH RE	SPECT TO			
×	>	7	XDOT	Y00Y	2007	PHIX	>1Hd	2143
10 3SI	-0.3599E 01	-0.1425E 01 -0.3599E 01 -0.4809E-03 -0.1216E 04 -0.2038E 04 -0.4763E 00 -0.	-0.1216E 04	-0.2038E 04	-0.4763E 00	-0-	•	-0-
6SE 00	0.976SE 03 0.2208E 01	0.2916E-03	0.2037E 04	0.8195E 03	0.1286E 01 -0.	•	•	-0-
• 40-399	0.4566E-05 -0.2909E-03 -0.211	-0.2118E 00	-0.75372 00	18E 00 -0.7537E 00 -0.4475E-02	0.8213E 03 -0.	•	•	٠٥.
62E-02 .	-0.1162E-02 -J.1442E-02 -0.531	-0.5311E-06	-0.1426E 01	11E-06 -0.1426E 01 -0.9768E 00 -0.7727E-03 -0.	-0.7727E-03	•0•	•	°°
43E-02	0.14436-02 0.52056-02 0.790	0.7905E-07	0.340iE 01	0.22116 01	0.1937E-02 -0.	•	•	•
39E-06	0.7239E-06 -0.5050E-06 -0.116	-0-1163E-02	-0.4331E-05	53E-02 -0.8331E-05 -0.1780E-03 -0.2130E 00 -0.	-0.2130E 00	•	•	• 0 •
•	-0-	-0-	•0-	-0-	-0.	-0.2130E 00 -0.9770E 00 -0.9991E-05	-0.9770€ 00	-0.9991E-05
1	-0.	-0-	-0-	-0-	-0-	0.9770E 00	0.9770E 00 -0.2130E 00	0.7740E-63
•	-0-	٥٠	-0-	-0-	-0.	··0.7624E-03	0.1551E-03	0.1000E 01
TRAJECTUR TIME 500.000 2000.000 500.000	Y VARIABL 92 169	77. 77. 808	7 12070075. 12070075. 1006 -63.257	5700173. -5393493. ALT 98.62	XD01 23040.41 -15703.07 VEL 25580.89	103 103 143	\$	2007 -4038.29 -10417.33 A2 100.187
				1			1000	128.477

C-3. Test Case 2 (Continued)

11/11/65 JOHN COE FLDG N 64 RM 2 (EST CASE 2

TRAJECTORY TAPE 562

ORBIT DISPERSIONS EVALU 2

11ME=	2000.000		COORDINATE SYSTEK	SYSTEK LH					
	DPX	AéΩ		CAX	000	DVZ	XOO	V00	700
10-1110	-3580.	1790.		-1.43	4.73	00.0	0.0	0.0-	9-
0112-01	-38.	456		-0.04	0.07	-0.53	2.4	-4-3	å
0113-01	514,	-		-0.00	-0.61	0.02	0.0-	2.0	•
0131-01	7.	•		0.01	-0.01	- ¥ - 59	-26.1	-16.8	0-
0132-01	5895.	434.		0.65	-3.37	0.02	-0.3	0.0	30.
0133-01	-133.	-1-		-0.02	0.09	0.79	-14.8	26.1	ģ
4001-01	-4014-	1204.		-1.42	4.07	-0.00	-0-	ė	0-
1002-01	-3623.	3870°		-3.07	96.48	0.0	o.	Ģ	q
4003-01	73,	-77.		90.0	41.0-	0.76	0-	Ģ	
10-11-01	-2779.	1007.		-1.00	3.08	-0.00	•	þ	ģ
1012-01	-5631.	6071).		-4.80	10.94	0.02	-0-	9	Ģ
4013-01	-2.	3.		-0.00	00.00	-0.03	0	q	-0-
10-1005	-15.	18.		-0.01	0,03	-1.27	-43.5	-24.1	6
3002-01	-117.	25,		-0.04	0.11	61.0	-24.7	6 3° 8	-
5003-01	-6348-	1240.		-1.92	5.51	0.00	· •	0-	-56-
T02102	-10189.	4098.		-4.88	11.06	-0.00	-0-	9	
T022-02	-2.	<b>.</b>		-0.00	0.01	-1.06	-0-	Ģ	ė
1023-02	-1216.	2037.	-1-	-1.43	3.40	-0.00	9	ģ	-0-

C-3. Test Case 2 (Continued)

2007 -10417.33 AZ 114.861	•	V00f 17345.02 FPA -0.051	20 A A A A A A A A A A A A A A A A A A A		X0UT 15703.07 VEL 25611.65	X001 -15703.07 VEL 25611.65	ë <b>4</b>	2 -5393493. ALT 93.46		V 12070075. LONG 27.112	-	ES. X 1941277. LAT -14.536	BLES. X 169412 LAT -14.9	VARIA	TRAJECTORY TINE 2000-000
56.51	, <b>2</b>	58-4672	6	. 58.3603	8	. 9019-2	03	21.9503		9.1488	9	5566. 7546	9	10240.80	SIGMA 17155.0320 10240.8098
0.34246		-0°0000		-0-0006		900000		-0.2956		0.2162		-0.0001		-0.0613	0.4948
0.3418E 04 -0.: 533E-	Ş	0.3418E		-0. 1.31		0.5598		-0.0005		0.0007		-0.3610		-0.0006	9000-0
-0.4473E-	70	0.3406E 04 "0.1045E 02 -0.4473E-	Š	0.3406E		0.5267		-0.0008		900000		-0.4678		-0.0011	0.0002
0.89326-	70	0.87428 02	05	0.8219E 02	5	0.71336 01		0.0056		-0.0060		-0.8782		0.0068	-0.0037
-0.3797E	8	0.3271E 00 -0.1367E 01 -0.6350E 00 -0.3797E	5	-0-13676	8	0.3271E	03	0.4818E 03		-0.9910		-0.0050		0.9511	-0.9358
0.1157E	8	0.3715E 00	00	0.3430E 00	8	-0.1469E	03	0.8370E 02 -0.1990E 03 -0.1469E 00	<b>7</b> 0	0.8370E		0.0054		-0.9739	8968.0
-0.2562E	3	0.2738E 03 -0.6118E 03 -0.1306E 05 -0.1585E 06 -0.1175E 04 -0.2562E	90	-0.1585E	03	-0.1306E	03	-0.6118E	03	0.2738E	03	0.3099E 08		-0.0058	0.0036
-0.4900E	03	0.1847E 03 -0.6409E 03 -0.3338E 03 -0.4906E	03	-0.6409E	03		90	0.2138E	9	3315E 06 -0.9124F 05 0.2138E 06	90	-0.3315E	60	0.1049E 09 -0.	-0.7825
0.4967E	03	0.4607E 03	03	0.2206E 03	03	-0.1694E	90	0.1407E 06 -0.3524E 06 -0.1694E 03	90		90	0.34546 06	60	-0.1375E	6.2943E 09 -0.1375E 09
200		<b>POQ</b>		DOX		0 0 2		DVY		DVX		740		DPY	X 4G
													×	COVARIANCE MATRIX	COVARIA
		295	<b>3</b>	TRAJECTORY TAPE 562	R		VAL	ERSIONS E	1SP SYS	DRBIT DISPERSIONS EVALU 2 COURDINATE SYSTEM LH	3	_	000	2000-000	TIME=

C-3. Test Case 2 (Continued)

TRANSIT	TRANSITIUN MATRIX.	DARTIALS AT T=	9	UISPERSIDMS EVALU 2 TRAJI	ECT 1	ECTORY TAPE 500.000	295	: •
COORDIN	COORDINATE SYSTEM	5						
PARTIAL	S OF X.Y.Z.	PARTIALS OF X,Y,Z,XDOT,YDOT,ZDOT,PHIX,PHIY,PHIZ MITH RESPECT TO	T.PHIX.PHIY	PHIZ WITH RE	SPECT TO			بد. •
×	>	7	XDOT	YDOT	1007	×	PHIV	21114
-0,2018E 01	-0.14146 02	-0,2018E 01 -0.1414E 02 -0.1143E-02	-0.1334E	05 -0.2518E 04 -0.8324E	-0.8324E 0	01 -0-	•	.0.
-0.8651E 00	0.24646 01	0.2508E-02	0.2512E 04 -0.7365E	-0.7365E 03	0.3692E 0	01 -0.	•	-0-
-0-1951E-02	-0.1130E-01	-0.1951E-02 -0.1130E-01 -0.5165E 00	-0.1102E 02	-0.1102E 02 -0.2527E 01 -0.7192E 03	-0.7192E 0	3 -0.	•	÷ ;
0.1023E-02	-0.1786E-02	0.1023E-02 -0.1786E-02 -0.2566E-05	-0.2025E 01	0.8659E 00	00 -0.1760E-02	2 -0-	•	-0.
0.17666-02	U.1580E-01	0.3426E-05	0,1416E 02	0.2477E 01	0.1246E-01	1 -0.	••	-0-
0.59625-05	0.1636E-04	0.1018E-02	0.12036-01	0.1203E-01 0.7470E-02 -0.5186E 00 -0.	-0.5186E 0	.0- 0	•	-0-
•	ં	•	•	0.	•	-0.5154E 00	0.8570E 00 -0.1067E-02	-0.1067E-92
ė	-0.	-0-	-0-	-0-	•	-0.4570E 00	-0.8570E 00 -0.5154E 00 -0.2460E-02	-0.2460E-02
•	-0-	-0-	-0-	-0-	-0.	-0.2662E-02	-0.2662E-02 -0.3537E-03	0.1000E 01
17AJECTUR 71ME 500-000 4000-000 500-000	Y VARIABL 92 -213	00 00 00 00 00 00 00 00 00 00 00 00 00	Y -16818952. 1230478. LONG -63.257 159.990	2 9700173. -2040570. ALT 98.62 92.50	XDUT 23040, 23040, -2463, VEL 25580, 25580,		YDUT 10354-42 -22494.16 5PA 0.000	2007 -4038.29 12005.66 A2 100.387 61.909

C. 3. Test Case 2 (Continued)

11/11/65 JOHN DDE BLDG 11 64 RM 2 TEST CASE 2

TRAJECTORY TAPE 562

ORBIT DISPERSIONS EVALU 2

	200			- ·	0.4	0.0-	0.05	7			•	•	ģ	ď	, •	- C				•	į	•
	, OO	•	9 4		7,9	-7.2	4.0-	-20-1	9	•		•	•	9	ģ	-11-			•	ř	ř	ř
	XOG		-	7 (	9	29.1	-0.2	-7-1		; ;	<b>:</b>	<b>;</b>	•	á		4.44			) •	<b>5</b>	<b>;</b>	5
	200	10.0	. 6		70.0.	₹ <b>5.0</b> -	0.01	0.01	6.0				70.0	0.05	10.01	-1-00	-0-03		<b>.</b>		KC - V	
	DVY	11.02	80.0		00.0	-0.01	10.06	-0-16	3.73	23.56	# T		20.4	37.00	0.02	0.13	0.03	0.45	12,30		\$0.0 4.14	
YSTEK LH	DAX	-G. 49	-0.02			20.0-	-5.01	01.0	1.56	-2.24			00,00	-3.59	-0.00	-0.05	90.0	3.50	4.33	10.0-	20.01	
CORDINATES	0.62	-7-	-123.	17.		-2870.	2	967.	-3.	•	1257.			•	-41.	-2445-	166.	4	-13-	-3506		
•	DPV	980.	30.		•	•	5182.	-101-	-1313.	3126.	-99-	-212		4975	2.	26.	-55.	-3403.	-3662.	18.	2512.	
<b>4</b> 000.000	DPX	-8966-	-237.	C	•	•67	-9623.	147.	-3482.	-22302.	445.	-4100		-37134.	-14.	-112.	-32.	-422.	-12589.	-42.	-13344.	
- 34 I L		0111-01	0112-01	0113-01		4014610	10-2610	0133-01	A001-01	A002-01	A003-01	A011-01		10-210V	A013-01	10-1003	C002-01	10-6009	1021-02	1022-02	T023-02	

C-3. Test Case 2 (Continued)

T1 ME =	4000.000	0	00	ORBIT DISPERSOCORDINATE SYSTEM	SYS	ORBIT DISPERSIONS EVALU Z DINATE SYSTEM LH		}		) }				
COVARIA	COVARIANCE MATRIX										•			
X	P 4	240		DVX		DVV	240		<b>800</b>	•	<b>D04</b>		706	
0.3089E 10	0.3089E 10 -0.3911E 09	9 0.7660E 06	90	0.2677E	90	06 -0.3255E 07 -0.4221E 04 -0.4303E 34 0.2955E 04 -0.2651E 06	-0.4221E	\$	-0.43036	8	0.2955E (	. 1	0.2651E 06	
-0.6661	0.11166 0	9 -0.1740E	90	-0.9861E	90	0.1116E 09 -0.1740E 06 -0.9861E 05 0.4163E 06		60	0.1235E	8	-0-1535E	<u>.</u>	0.1917E 03 0.1235E 04 -0.1535E 04 0.3257E 04	
0.0025	-0.0030	0.2964E	90	0.8421E	05	0.8421E 02 -0.9506E 03		0	-0.2113	0	0.1270€	)-  -  -  -	0.1474E 05 -0.2113E 06 0.1270E 09 -0.2585E.03	
0.5057	-0.9802	0.0016		0.9069E	05	0.9069E 02 -0.2863E 03 -0.4111E-01 -0.6755E 00	-0.41116	10-	-0.6755	0		7 7	0.1412E 01 -0.3300E 03	
9666-0-	0.6728	-0.0030		-0.5132		0.3432E 04		6	0.55706	6	0.4357E 01 0.5570E 01 -0.3372E 01	5	0.2812E 03	
-0.0252	0900.0	0.9003		-0.0014		0.0247	0.9046	6	-0.7365E	05	0.2434	)- 20	0.9046E 01 -0.7365E 02 0.2434E 02 -0.1147E 01	
-0.0013	0.0020	-0.6654		-0.0012		0.0016	-0.4199		0.34016	6	0.5629E	5	0.3401E 04 0.5629E 01 0.3143E-02	
0.0009	-0.0025	0.0399		0.0025		-0.0010	0.1383		0.0016		0.3423	7 3	0.3423E 04 -0.7744E-03	
-0.0815	0.5269	-0.0008		-0.5922		0.0820	-0.0065		0.000		-0.0000		0.3424E 04	
\$1GHA \$5578.4883	10563.8370	0 5444.5479	419	9.5231	231	58.5827		3.0077	58.3213	213	58.5061	3	58.5179	_
FRAJECTORY TIME 4000.000	VARI	ABLES. -21354558. LAT -5,449		V 1230476. Long 159.990		2 -2040570. ALT 92.50		XD07 -2463.44 VEL 25616.23	<b>5 6</b>	Y001 -2249 FP	YDOT -22494.16 FPA 0.045	Fig od	2001 12005.66 A2 61.909	

C-3. Test Case 2 (Continued)

C-39

2007 -4038.29 -7034.90 A2	YDOT 10354.42 15244.45 FPA	145	23040-41 19303-54 VEL	2 9700173. 6406797. ALT .	7 -16818952- -13934491- LUNG	• · · · · · · · · · · · · · · · · · · ·	Y VARIABL 92 140	TRAJECTUR TIME 500.000 6000.000
0.1000£	-0.4142E-02 -0.1315E-02	-0.4142E	•	• 0-	•0-	•0•	-0-	.0-
0.2365E-	00 0.9642E 00	0.26506 00	•	•	•	•	.0	•
0.3641E-	0.9642E 00 -0.2650E 00	0.9642E	-0-	.0-	•0•	-0-	-0-	. 0,
-0-	<b>.</b>	-0-	0.9653E 00 -0.	-0.4515E-02	-0.2558E-01	-0.3117E-03	-0.3000E-04	-0.2621E-05 -0.3000E-04 -0.3117E-03 -0.2358E-01 -0.4515E-02
••	•	.0	0.3559E-01 -0.	0.9061E 00	0.1473E 02	0.14136-04	0.2256E-01	-0.3146E-C4
•	•	•••	-0.3478E-02	0.1004E 01 -0.2476E 00 -0.3478E-02	0.1004E 01	0.4272E-04 -0.1705E-05	0.4272E-04	-0.3019E-03
•	•	•	0.2201E 03	0.5488E 01	0.3317E 02	0.9649E 00	0.3951E-01	0.2971E-02
•••	•	•	0.6360E 01	0.1976E 03	-0.5094E 02	0.2744E-02 -0.5094E	0.9073E 00	0.2475E 00
-0-	.0	•	02 -0.2986E 02	0.4892E 02 -	-0.15346 05	0.9906E 00 -0.1873E 02 -0.1159E-01 -0.1534E	-0.1873E 02	0.9906E 00
2144	PHIY	PHIX	1007	YDOT	XOUT	7	>	×
			SPECT TO	PARTIALS OF X,Y,Z,XOOT,YDOT,ZDOT,PHIX,PHIY,PHIZ WITH RESPECT TO	IT.PHIX.PHIY.	.001,YD01,2D0	5 OF X.Y.Z.X	PARTIAL!
						5	COORDINATE SYSTEM	COORDIN
	10 T= 500.000	2006	SPECT TO TA	6000.000 WITH RESPECT TO I		PAKLIALS AL IS	TRANSITION MATRIX.	TRANSIT

C-3. Test Case 2 (Continued)

	TRAJECTORY TAPE 562
TEST CASE 2	PERSIONS EVALU 2
8LDG N 64 RM 2	ORBIT DISPERSIONS
8106 3	
JOHN DOE	
11/11/65	

	200	-0.0	0.1	£°\$	0-0-	30.0	-0-1	•	-0-	•	Ģ	-0-	o o	0.0-	-1.2	-50.0	Ģ	•	•
	NOA	0.0-	-2.7	1.0	25.3	4.0	16.2	•	•	•	ċ	•	ċ	42.1	26.9	-0-	ċ	ċ	ċ
	<b>DOX</b>	0.0-	-4.5	0.1	-16.2	9.0	25.3	•	ė,	• •	ó	•	•	-27.0	42.1	-1.0	•	•	•
	7/0	-0.02	-0.33	-0.00	3.01	-0.03	-0.80	-0.01	-0.07	-1.29	-0-01	-0.11	0.0	2.73	-0.09	-0.00	-0.02	4.83	-0-03
	DVV	14.19	0.31	-0.57	90.0	18.49	-0.33	16.1	29.30	-0.62	4.67	46.23	0.02	0.23	-0.06	-5.33	4.53	0.18	18.73
SYSTEM LH	DVX	-0.21	0.01	-0.00	-0.02	2.61	-0.05	-0.83	1.18	-0.02	-0.44	1.88	00.0	-0-01	-0.03	-1.71	-1.24	-0.02	1.00
OORDINATE S	240	27.	434.	-21.	1553.	•	-697.	.6	41.	-669-	11.	.99	23.	1188	-160.	;	27.	1101.	33.
Ū	DPY	733.	S.	•9	23.	-1239。	20.	696.	225.	-15.	513.	333.	•	21.	19.	1053.	988.	32.	-51.
000*000	DPX	-11325.	-240	483.	-57.	-16952.	311.	-457.	-23275.	498.	-3265.	-36764.	-16.	-188	81.	6394.	245.	-149.	-15339.
TIME=		0111-01	0112-01	0113-01	10-1610	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	2001-01	6002-01	6003-01	T021-02	1022-02	1023-02

C-3. Test Case 2 (Continued)

Ü

TIME		000.0009	0	2	ORBIT (	SYS	ORBIT DISPERSIONS EVALU 2 COORDINATE SYSTEM LH	VAL		ZA Z	TRAJECTORY TAPE 562	APE	295			
COVAR	COVARIANCE MATRIX	XIX														
X 40	OPV		0P2		DVX		DVY		DVZ		MOG		00A		700	
0.3454E 1	0.3454E 10 -0.8258E 07 -0.7059E 07 -0.2052E 06 -0.4274E 07	5 07	-0.7059E	01	-0.2052E	8	-0.4274E	20	0.6960E 04	\$	0.2045E	ð	0.2045E 04 -0.1247E 05 -0.8260E	9	-0.826	<b>9</b>
-0.0599	0.5504E 07	5 07		90	0.1910E 06 -0.6335E 04	5	0.2329E 05	9	0.1870£	03	0.1870E 03 -0.1402E 04	6	0.1079E 04 -0.8980E	Š	-0.898	90
-0.0482	0.0327		0.6220E 07	01	0.2459E 03	03	0.8926E 04	8	0.1452E	00	0.1452E 05 -0.8328E 05	0.5	0.7254E 05	9	0.6553E 0	36
-0.7677	-0.5936		0.0217		0.2069E 02	05	0.2377E	03	-0, 5476E	8	0.11476	70	0.2377E 03 -0,5476E 00 0.1147E 01 -0.5094E-01	-01	0.1636E 0	9
-0.9962	0.1360		0.0490		0.7159		0.5328E	Š	0.5328E 04 -0.8939E 01 -0.3235E 01	01	-0.3235E	10	0.1438E 02	05	0.8185E 0	2E
0.0182	0.0123		0.8961		-0.0185		-0.0188		0.4222E	05	0.4222E 02 -0.1448E 03	03		03	0.1766E 03 -0.3459E 0	96
900000	-0.0102		-0.5712		0.0043		-0.0008		-0.3812		0.3417E 04	ð		05	0.1105E 02 -0.8049E-0	<b>36</b>
-0.0036	0.0079		0.4983		-0.000-		0.0034		0.4657		0.0032		0.3407E 04	Š	0.1257E-0	7
-0.2402	-0.6541		0.0045		0.6145		0.1916		-0.0009		-0.0000		0.0000		0.3424£	¥
SIGNA 58769.9321	1 2346.0510	1510	2493.9410	011	4.5486	9	72.9947	;	6.4980	9	58.4574	¥2.	58.3702	702		58.517
TRAJEC TE	TRAJECTORY VARIABLES. TIME X 6000.000 14064	I 40	BLES. X 14064065. LAT 23.012	7	Y -13934491. LONG -69.803		2 8+0@797. ALT 97.92	. 2	X007 1930 VĒI 2558	XDOT 19303.54 VEL 25543.39	\$ <b>\$</b>	Y00T 1524 FP -0	YDOT 15244.45 FPA -0.010		2007 -7034.90 A2 107.378	2 2

C-3. Test Case 2 (Continued)

TAPE 562	RANGE	· >	731.	٠.		23.	-1242.	20.	.969	221.	-15.	_	326.	ċ	21.	19.	1054.	988.	32.	-54.
TRAJECTORY TAPE 562	CRITERION	- DE	228.	439.	-30.	1554.	311.	-702.	17.	456.	-108.	.69	721.	24.	1191.	-161-	-110.	23.	1103.	306.
DISPERSIONS EVALU 2	000*0009	I	0.468	010.0	-0.020	0.001	0.100	-0.612	0.019	0.961	-0.020	0.135	1.518	0.001	0.007	-0.003	•	-0.010	0.005	0.633
ORBIT	T IME =		0111-01	0112-01	0113-01	0131-01	0132 1	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	6001-01	C002-01	6003-01	1021-02	1022-02	1023-02

C-3. Test Case 2 (Continued)

COVARIANCE MATRIX

0.315615E 03 0.325949E 06 0.282758E U4 0.7554976 07 Ä 0.05053 0.5493776 01 0.42357 0.05544 ¥ **}** 

0.550114E 07

SIGMAS

2750. 2.427

2345.

MOMINAL TERMINAL CONDITIONS

24209.426 VEL/A 97.92 ALT -69.603 LONG 23.012 LAT

C-3. Test Case 2 (Concluded)

108.399 AE/A

-0.030 FPA/R

11/11/65 JOHN DOE BLOGN 64 RM 2 TEST CASE 3
PHASE LUGIC SYN EQ MISSION

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11ME=

Ö X

COURDINATE SYSTEM LH

DP.Z DVX DVV DVZ DOX

-0. 0.03 -0.03 -0.052 -0.0

-500. -0.02 0. -0.00 4.9

-0. 0. 0. 0. 0. 0.0

-0. 0. 0. 0. 0. 0.0

-0. 0. 0. 0. 0. 0.0

-0. 0. 0. 0. 0. 0.0

-0. 0. 0. 0. 0. 0.0

-0. 0. 0. 0. 0. 0.0

500. 500. - 6. - 0.

300.000

0111-01 0112-01 0113-01 0131-01 0132-01

0.0

00000

C-4. Test Case 3

	200 ¥00	526E-04 0.2467E 04	0.4470[-07 -0.1474E-04 -0.1583E-05 -0.6254E-05	0.7451E-08 -0.2467E 04 -0.4625E-05 -C.4189E-06	-0.8599E-01 -0.1318E-09 -0.9046E-09	0.30872-09 -0.9313E-09 -U.1580G 00	0.9949E-10 0.4657E-09 -0.8599E-01	0.9243E 03 -0.1703E-05 -0.1329E-05	0.90006 03 -0.75296-05	000 0.9243E 03	30.0000 30.4030	7.01.7 0.04 0.000
	ă	35 -0-1!	1-0- +0	)+ -0 - +C	1.0- 10	6-0- 50	10 0.40	3 -0-11	0.9	-0°000		YUUF 213-17 FPA -0.000
	DOX	-0.3092E-(	-0-14746-	-0.2467E	-0.8599£-(	0.30876-0	0.9949E-	0.9243E	-0.0000	00000-0-	30.4030	
-	DVZ	0.2500E 06 -0.4230E-03 -0.3642E-03 -0.2980E-07 -0.1601E 02 -0.8714E 01 -0.3692E-05 -0.1526E-04	0.44706-07	0.74516-08	•	0.5581E-03	0.3037E-03	0.000.0	0000*0	-0.1623	0.0174	XDUT 1320.79 VEL 1338.85
	DVV	-0.1601E 02	0.5960E-07	-0-	-0.18136-11	0.1026E-02	1.0000	0.000.0	-0.000-	-0.1623	0.0320	4 9091646. ALT -1.10
	DVX	-0.2980E-07	0.1601E 02	0.8714E 01 -0.	0.13296-02 -0.18196-11	-0.0000	•	-0.0176	0000.0.	00000-0-	5960.0	Y -18112597. LONG -80.578
	240	-0.3642E-03	0.2500E 06 -0.9766E-03	0.2500E 06	0974.5	-0,	00000.0	-0.1è23	-c.oco-a-	3000°5-	\$00.000	559. T •555
COVARIANCE MATRIX	DPY	0.4230E-03	0,2500E 06	00000-0-	0.8784	000000	00000*0	00000-0-	0000.0-	0000.	2000 0000	TRAJECTORY VARIABLES. TIME 3005 0. LA
COVARIAN	DPK	0.2500£ 06 -	-0.000	-0.000.	-0.0000	-1.0000	-1.0000	-0.0000-	- 00000-0-	0.1623	0000°005	TRAJECTOR TIME 0.

C-4. Test Case 3 (Continued)

464.664 COORDINATE SYSTEM LH

464.664 COORDINATE SYSTEM LH

-148. 653. -1. -0.07 0.75 -0.00

514. 0. -2. -17. 0.00 0.00

-17. -2. -497. -0.01 0.01

-13. 15. -461. -0.04 0.07 -1.03

-13. 616. 9. -1.90 0.07 -1.03

-223. 219. -5. 1.14 0.71 -0.02

-203. 243. -0.03 1.30 0.00

-203. 224. -10. 2.15 1.37 -0.05

-203. 224. -10. 2.15 1.37 -0.05

-203. 224. -10. 2.15 1.37 -0.05

-203. -22. -360. 0.00 0.00 0.00

-241. 5. -420. -0.01 0.00 0.00

-241. 5. -420. -0.02 -2.59

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

-241. 5. -420. -0.04 0.01

0111-01 0112-01 0113-01 0131-01 0132-01 00132-01 0002-01 0001-01 0001-01 0002-01 0002-01

0.04 C.00.00 C

ŽQ^

TREJECTORY TAPE 562

PHASE LUGIC SYN EQ MISSION

TEST CASE

RH 2

3

BLDG N

JOHN DOE

11/11/65

C-4. Test Case 3 (Continued)

TIME

TRAJECTORY TAPE 562 PHASE LOGIC SYN EG MISSION COORDINATE SYSTEM LH 1,04.664 TIME=

		Ş	9	03	03	03	8	20	70	8	156	
	700	0.4873E	-0.5972E	-0.3810E	0.1555E 03	-C.3791E	-0.9603E	0.3606E 02	0.1068E 02	0.46076 04	67.8756	1007
	A00	0.63.56E 02	-0.2912E 03	0.3519E 05 -0.3810E 03	0.8325E 00	-0.1478E 01	0.2080E 03 -0.9603E 00	0.6239E 01	0.2653E 04	0.0031	51.5045	51.6
	DOX	0.2654E 03	.0.3401E 03	-0.2355E 05	0.1005E 01	-0.3043E 01	-0.6374E 02	0.2674E 04	6,000°0	0.0103	51.1152	•
	DVZ	-0.4805E 02	0.7194E 04 -0.3914E 02 -0.3401E 03 -0.2912E 03 -0.5972E 05	0.4545E 04 -0.2355E 05		0.3878E 02 -0.7253E-01 -0.3043E 01 -0.1498E 01 -C.3791E 03	0.2241E 02 -0.6374E 02	-0.2404	0.8529	-0.0030	4.7338	XDGT
	DVV	0.3829E 04 -0.3973E 04 -0.4805E 02	0.7194E 04 -	0.5294E 01	0.1524E 02 -0.9783E 01 -0.1410E 00	0.3878E 02 -	-0.0025	- \$600*0-	-0.0047	- 0.8970	6.2274	7
	DVX	0.3829E 04 ·	-0.9387E 03	0.1284E 07 -0.3054E 02	0.1524E 02 -	-0.4024	. 920000-	0.0050	0.0041	0.5868	3.9043	<b>→</b>
	240	-0-1037E 05	E 04	0.1284E 07	6900*0-	8000.0	0.8472	-0.4019	0.6028	-0.0050	1133.2448	
COVARIANCE MATRIX	DPY	0.1298E 07 -0.5535E 05 -0.1037	0.1689E 07 -0.5511	-0.0037	-0.1850	0688*0	-0.0064	-0.0051	-0.0044	-0.6770	1239.4974	VAK I AB
COVARIA	DPX	0.1298E 07	-0.3738	-0.0080	0.8608	-0.5599	-0.0089	0.0045	0.0011	0.6302	S1GMA 1139.2668	TRAJECTORY TIME

C-4. Test Case 3 (Continued)

2491.38 -3491.38 AZ AZ

Y60T 9347.12 FPA 0.077

xDG7 23153.78 VEL 25212.21

2 9832988. ALI 98.58

> -17166351. LONG -65.748

8444418. LAT 27.202

464.664

O

PHASE LUGIC SYN EQ MISSION TRAJECTORY TAPE 562
PARTIALS AT I= 477.664 WITH RESPECT TU I= 464.664 TRANSITION MATRIX. COORDINATE SYSTEM

PARTIALS OF X, Y, Z, XDOT, YDOT, ZDOT, PHIX, PHIY, PHIZ WITH RESPECT TO

•								
×	>	7	XDOT	YDOT	1007	* He	PHIV	PHil
0.9998E 00	0.9998E 00 -0.1524E-01 -0.2049E-07	-0.2049E-97	0.1300E 02	0.1300E 02 -0.1981E 00 -0.2682E-06 -0.	-0.2682E-06	-0.	•	°°
0.15246-01	0.1000E 01	•	0.19818 00		0.1300E 02 -0.1192E-06 -0.	•0•	•	-0-
0.8382E-08	0.6382E-08 -0.1490E-37	0.9999E 00		0.1192E-06 -0.2384E-06 0.1300E 02 -0.	0.1300E 02	•0-	.0	•
-0-1839E-04	-0.1839E-04 -0.1401E-06	0.5400E-12	0.9998E 00	0.9998E 00 -0.1524E-01 -0.2421E-07 -0.	-0.2421E-07	• 0-	•	0-
0.1401E-06	0.3677E-04	0.6821E-12	0.1524E-01	0.1524E-01 0.1000E 01	0.37256-08 -0.	-0-	•	.0-
-0.3979E-12	C.3979E-12	C.3379E-12 -0.1839E-04		0.6519E-08 -C.1118E-07	0.9999E 00 -0.	-0-		•
-0-	-0-	-0-	-0-	•0,	-0-	0.9999E 00	0.9999E 00 -0.1524E-01 -0.2235E-01	-0.2235E-U
•	•	•	•	•	•	0.15246-01	0.99596 00	0.3725E-0
•0•	-0-	-0-	•	-0-	-0-	0.65196-06	0.65196-08 -0.11186-07	0.1000E 0
18AJECTUR 11ME 464-664 477-664 477-664	Y VARIABL	18. 96. 202 063	V -17166351. -17042791. LONG -65.748	2 9632986. 9786427. ALT 96.58	XDOT. 23153-76 22995-75 26212-21 25212-21	•	007 9347.12 9641.63 FPA 0.077 0.052	2007 -3493.38 -3671.75 A2 A2 96.998

C-4. Test Case 3 (Continued)

m
CASE
TEST
R# 2
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		<b>700</b>	-0-	÷	•	ġ	ė	-30.	•	<u>.</u>	•	ċ	ė	• •	ė	ċ	-47.	-39.
		D0Y	0.0-	0.0	1.3	28.9	8.1	-0.5	•	•	•	•	•	•	19.7	-38.5	-0-3	-0.5
DRY TAPE 562		DOX	0.0	7-0	4.7	-8-1	28.9	9.0-	•	• •	•	•	•	•	38.2	19.1	-0.9	<b>1.</b> 0-
TRAJECTORY		2/0	-0.00	-0.01	91.0	3.37	-1.02	0.02	-0.02	-1.41	0.00	-0.05	0.05	00.0	1.10	-2.59	0.0	0.01
EQ MISSION		DVY	0.17	-0.60	0.01	00.0	0.07	3.38	0.74	-0-01	1.30	1.42	00.0	0.22	0.04	0.02	3.01	3.46
PHASE LOGIC SYN EQ	SYSTEM LH	DVX	-0.08	00.0	-0.01	00.0-	-0.04	-1.94	1.12	-0.03	-0.60	2.12	00.0	-0-12	-0.01	-0.02	-C-98	-1.45
PHAS	COORDINATE S	DP.2	-	-17.	-495.	760.	-474-	•6	-9-	-357.	3.	-11-	13.	-	169.	-454	2.	5.
	J	OPY	661.	•	-2.		16.	650.	232.	-2.	256.	448.	•	50.	7.	5.	447.	<b>605</b>
	417.664	DPX	-157.	514.	-18.	-3.	-14.	-670.	235.	-7.	-214.	452.	•	-45.	-4-	-3.	-260.	-436.
	TIME=		0111-01	0112-01	0113-01	0131-01	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	C001-01	6002-01	6003-01	6063-01

C-4. Test Case 3 (Continued)

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411.664	Ü	PHASE LOG DORDINATE SY	PHASE LOGIC SYN ED MISSION COORDINATE SYSTEM LH		TRAJECTORY TAPE 562	562	
740		DVX	DVY	7,00	xna	<b>A</b> 00	700
0.1419E 07 -0.6261E 06 -0.1132E	0.5		0.4081E 04 -0.4177E 04 -0.4906E 02	-0.4906E 02	0.2870E 03	0.9043E 02	0.5224E 05
0.1864E 07 -0.6137E	40	E 04 -0.1110E 04		-0.4074E 02	0.7687E 04 -0.4074E 02 -0.3773E 03 -0.3274E 03 -0.5470E 05	-0.3274E 03	-0.5470E 09
0.1406E	C7	0.1406E C7 -0.3223E 02		0.4411E 04	0.3634E 01 0.4811E 04 -0.2470E 05	0.3809E 05 -0.4063E	-0.4063E 03
6900*0-		0.1540E 02	0.1540E 02 -0.1011E 02 -0.1384E 00	-0.1384E 00	0.10536 01	0.9029E 00	0.1622E 03
\$1.00.0		-0.4122	0.3902E 02	-0.7621E-01	0.3902E 02 -0.7621E-01 -0.3063E 01 -0.1604E 01 -0.3843E	-0.1604E 01	-0.3843E 03
0.8674		-0.0075	-0.0026	0.2224E 02	0.2224E 02 -0.6483E 02	0.2096E 03 -0.1008E	-0-1008E 01
-0.3959		0.0051	-0.0093	-0.2613	0.2769E 04	0.6574E 01	0.3699E 02
0.6128		0.0044	-0.0049	0.8479	0.0024	0.2747E 04	0.1157E 02
-0-0050		0.5990	-0.8915	-0.0031	0.0102	0.0032	0.4761E 04
1185.6961	~	3.9244	6.2469	4.7156	52.6194	52.4159	69.0002
TRAJECTORY VARIABLES.  TIME X 477.664 8744396: LAT 27.063		V -17042791. LONG -64.834	2 9786427. ALT 98.62	XDUT 22995.75 VEL 25211.77	•	DDT 9661.63 FPA 0.052	2001 -3671.75 A2 99.439

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C-4. Test Case 3 (Continued)

	IRY TAPE
	TRAJECTORY TAPE
IN DOE BLDG N 64 RM 2 TEST CASE 3	NOISSIM OF Man Property
CASE	2
EST	,
)e=	
RM 2	
99	
HLDG N	
DOE	
JUHN DOE	
11/11/65	

	700	0.0-		•••	-0-	0.0.		9.0-	-30.0		5	0-	-	;	•	-0-	•	•	6.0-	•	1:0-	8.64-		1.04-		
	DUY	0-0-		0	1.5	28.7		<b>.</b>	-0.2	,	• •	•	ć	•	•	c	•	•	20.5		-34.6	-0-		-0-3		
	30X	0.0	,	0.1	7.4	9 9	0.0	28.7	C 1	` (	01	Ģ	6	•	•0-	(	•	•	4.05		20.5	0.		-0-		
	200			10.0-	8		20.00	-0.99		30.0 30.0	-0.03	-1.47		00.0	50.0-		0.00	00.0	7	7 . 7	-2.64	0	•	0.0		
	^^		18.0	-0-61		10.0	00.0	£0.0		3.45	0.78		1000	1.37	08.1		00.0	0.23	100	*0.0	0.02		2.10	4,54		
SYSTEM LH	***	YA0	60.0-			10.0-	00-0-	100	•	-2.00	1,16		-0.03	-0.62	2 11	1707	00.0	41.0 <del>-</del>		-0.01	-0-02		*0.1-	-1.52	76.1	
COORDINATE SYSTE	6	د			•07,																					
	;	740	673.		•	-3.	7	•		703.	252	•667	<u>۔</u>	279.		• 06.4	Ċ	ָ ֖֓֞	.00	*	•	•	503		• 000	
498.375		しアス	-177.		>14.	-18.	71	•	-15.	-127.	• : : : : : : : : : : : : : : : : : : :	.262	-/-		• ( ( )	484.	<	• •	- 24-	.5.	, ,	-5-	.292.		-482.	
TIME			10-11	70-11	12-01	13-01		10-16	32-01	23-03	10-00	10-100	002-01	20-600	10160	10-110	10 010	10-216	10-610	101-01		10-20	10760	10100	33-01	

C-4. Test Case 3 (Continued)

			E 05	E 05	E 03	E 03	E 03	E 01	E 02	E 02	\$ U	1981.01	<b>.</b> • • •
		700	0.5824E	-0.7286E	0.4284E 05 -0.4447E	0.17296	-0.4314E	0.2171E 03 -0.1044E	0.3815E	0.1307E	0.5012E C4	70.	2007 -4016.04 A2 100.132
			03	03	0	10	10	03	10	4		96.	
295		DOY	0.1327E	02 -0.4260E 03 -0.3902E 03	0.4284E	0.1042E	-0.1800E	0.21716	0.7397E	0.2903E 04	0.0034	53.8798	YDDT 10315.87 FPA 0.000
A P E			03	03	0.5	10		05	4			718	Y007 10319 FP/
TRAJECTORY TAPE 562		DOX	0.3185E	-0.4260E	-0.2660E	0.1110E	-0.3151E	-0.6640E	0.2924E 04	0.0024	0.0100	54.0718	0 6
RAJ			05	02	*	00	. 10	. 20				38	XDUT 23061.90 VEL 25581.19
		240	-0.5078E	0.8636E 04 -0.4525E	0.5329E 04 -0.2660E	-0.1351E 00	-0.8578E-01 -0.3151E 01	0.2288E 02 -0.6640E 02	-0.2567	0.8422	-0.0031	4. 78 38	XDUT 2306 2506 2558
MIS			40	40	10	05	02					69	2 6828. LT 98.62
PHASE LUGIC SYN EQ MISSION CO'JRDINATE SYSTEM LH		DVY	0.4549E 04 -0.4647E 04 -0.5078E	0.8636E	0.1742E	-0.1080E 02	0.4105E 02	-0.0028	-0.0091	-0.0052	-0.8851	6904.9	2 9706828. ALT 98.62
.061 SYS			40	4	02	05						25	
PHASE I		DVX	0.4549E	-0.1341E	07 -0.3494E	0.1612E 02	-0.4200	-0.0070	0.0051	0.0048	0.6081	4.0152	Y -16835937. LONG -63-372
3			90	0,4	0 7							0	7
10		740	0.1631E 07 ~U.7548E 06 -U.1283E	0.2168E 07 -0.7372E 04 -0.1341E	0.1616E	-0.0068	0.0002	0.8763	-0.3871	9.6255	-0.0049	1271-1400	3LES. X 9221363. LAT 26.824
498.375	×		90	07								192	81ES
864	COVARIANCE MATRIX	DPY	-U.7548E	0.2168E	-0.0039	-0.2268	0.9153	-0.0064	-0.0054	-0.0049	-0.6989	1472.5261	FRAJECTORY VARIABLES. TIME X 498.375 9221 LA
H	AR IA		07									#, 241	JECTORY TIME 498.375
TIME	'A02	X dQ	0.16316	-0.4013	-0.0019	0.8871	-0.5679	-0.0083	9,00.0	0.0019	0.6441	SIGH, 1277-1241	A A A

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C-4. Test Case 3 (Continued)

PARTIALS AT T= 1380.724 WITH RESPECT TO T= 498.375 TRANSITION MATRIX. COORDINATE SYSTEM

	21Hd	•	•	•	•	•		,8941E-07	0.2701E-07	0.1000E 01	2007 -4016.04 -12099.99 A2 100.132
	PHIY	.0-	.0-	.0-	.0-	G0.	.0-	0.4982E 30 -3.8671E 00 -0.8941E-07	D.4982E 00 0.		717
	РНІХ				-0-			0.4982E 30 -3	0.8671E 00 0	0.7451E-08 -0.8941E-07	YDD 103 224 F
SPECT TO	1007	0.2694E 03 -0.8440E 03 -0./866E-04 -0.	0.2861E-04 -0.	0.7291E 03 -0.	-0.5960E-07 -	0.5588E-07 -0.	0.4982E 00 -0.	-0-	0.	-0-	XDUT 23061.90 1979.81 VEL VEL 25581.19
PHIZ WITH RE	YDOY	-0.8440E 03 ·	0.7291E 03	0.95376-06 -0.83926-04	-0.8671E 00 -	0.1502E 01	-0.6519E-07	0-	.0	. •0-	2 970 <sup>k</sup> 828. 1907 <sup>k</sup> 25. ALT 98.62
T.PHIX.PHIY.	XDOT	0.2694E 03 -	C.8440E C3	0.953 /E-06 -	-0.367cE-02 .	0.1414E 01	-0.1211E-07	-0-	ċ.	0-	Y -16835937. -865589. LONG -63.372
PARTIALS OF X,Y,Z,XOOT,YOOT,ZOOT,PHIX,PHIY,PHIZ WITH RESPECT TO	7	-0.5215E-07	0.1863E-07	0.4982E 00	0.7458E-10 -0.3676E-02 -0.8671E 00 -0.5960E-07	C.5968E-03 0.2712E-02 0.2910E-10 0.1414E 01	-0.3638E-10 -0.2183E-10 -0.1031E-02 -0.1211E-07 -0.6519E-07	, -0-	••	-0-	631 16. 824
. OF X.Y.Z.X	>	-0.3676E-02 -0.1414E 01 -0.5215E-07	0.1502E C1 0.1863E-07	-0.1490E-07 -0.1304E-06 0.4982E 00		0.27126-02	-0.2183E-10 -	٠.	0,	•0-	7 VARIABL 92 214
PARTIALS	×	0.3676E-02 -	0.8671E 00	0.1490E-07 -	-0.1031E-02 -0.5958E-03	C.5968E-03	0.36386-10 -	-0-	0.	-0-	TRAJECTUR 11ME 498-375 1380-724 498-375

C-4. Test Case 3 (Continued)

	THAJECTORY TAPE 562
BLDG N 64 RM 2 TEST CASE 3	PHASE LUGIC SYN EQ MISSION
JOHN DOE 8	
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# JM I L	1380.724		COORDINATE S	SYSTEM LH					
	DPX	DPY	240	DVX	DVY	DVZ	XOO	AOO	700
0111-01	-1659.	1370.		-0.92	2.31	00.0	-0.0	-0.0	-0-
0112-01	514.	• •		-0.00	-0.61	0.01	0.0	1.0	5 <b>*</b>
0113-01	-5.	-26.		0.01	-0.13	09.0	1.1	8.4	-0-
0131-01	-1.	-6-	2887.	00.0	-0-01	0.83	-29.3	9.9	-0-0
0132-01	-95.	31.		-0.06	0.09	0.02	9.9	29.3	9.0-
0133-01	-4418.	1232.		-2.63	3.78	00.0-	-0-1	9.0-	-30.0
A001-01	-707-	2147.		-1.09	3.65	-0.01	0-	•	ò
A002-01	5.	-40.		0.02	-0.06	-0.33	•	•	-0-
A003-01	-1715.	694.		-1.11	1.80	-0.00	•0-	•	••
A011-01	-1392.	4025.		-2.10	6.85	-0.01	••	•	o-
A012-01	o o	<b>.</b>		-0.00	00.0	0.01	o-	•	0-
A013-01	299.	96		-0.18	0.28	-0.00	•	ċ	0-
C001-C1	-51.	27.		-0.04	90.0	0.37	78.0	83.5	-1.9
6002-01	-30.	•		-0.02	0.02	-0.19	83.6	-78.0	1.2
6003-01	-3605.	1882.		-2.68	4.37	-0.00	-0.5	-2.6	-138.0
6063-01	-4330.	1872.		-2.96	4.67	00.0-	-0.5	-1.1	-58.9

C-4. Test Case 3 (Continued)

			90	90	8	03	ŧ0	-; O	05	03	90
		700	0.8860E 06	0.1511E 04 -0.5151E 04 -0.4063E 06	0.23736 06 -0.50436	0.6218E 03	-0.9930€	.0.1268E	0.3469E 02	0.1787E 03	0.2341E 05
			90	*	90	10	92 -	03	10	90	
		<u></u>	0.12126 05	.51E	173E	0.8583E 01	36 7E	341	0.5891E 01	0.1399E 05	660
295		<b>D0</b>	0.12	-0.51	0.23	0.8	-0-12	0.10	0.56	0.13	0.0099
APE			6	•	90	0.6003E-01 -0.2519E 01	0.1524E 03 -0.1588E 00 0.3739E 01 -0.1267E 02 -0.9930E 03	0.1923E 01 -0.6108E 32 0.1014E 03 -0.1268E 0.	-0.3728 0.1396E 05	0.6184 0.0004	
TRAJECTORY TAPE 562		DOX	0.5033E 02 -0.3811E 04	0.15116	0.4798E 04 -0.2008E 06						-0.0060 0.0019
Z Y			05	05	*						
		7.00	0.5033E	0.4045 08 -0.2355E 06 -0.3121E 05 0.7701E 05 -0.9171E 02							
SIE			90	90	03	05	03				
PHASE LOGIC SYN EQ MISSION DINATE SYSTEM LH		DVV	0.4307E 05 -0.7837E 05	0.7701E	0.1206F 03 -0.3819E 03	0.3303E 02 -0.6632E 02	0.1524E	-0.0093	0.0026	-0.0087	-0.5257
.061 SYS			90	90	60	05					
COOR		DVX		-0.3121E	0.1206F	0.3303E	-0.9346	0.0075	-0.0037	0.0126	0.7073
			0.5	90	80						
		740	0.7283E	-0.2355E	0.1644E	0. 3052	-0.0076	0.8535	-0.4192	0.4950	-0.0081
1380.724	ž		90	90							
	COVARIANCE MATRIX	DP Y	0.6124E 08 -0.3403E 08	0.4045	-0.0001	-0.8540	2.9807	-0.0104	0700°C	-0.0068	-0.4175
<b>#</b>	AR IA		80								
TIME =	<b>COV</b>	Xdo	0.61246	16831	0.0023	1136.0	-0-8112	9,00.0	0.0041	0.0131	0.7400

118.1592 118.2660 152.9893

1.3866

12.3467

5.7470

SIGMA 7825.5453 6360.4144 4054.2928

2001 -12009.99 A2 118.122

YDUT 22499.63 FPA 0.000

XDUF 1979.81 VEL 25581.10

2 1907424. ALT 96.36

Y -865589. LONG -8.084

21408417. LAT 5.087

TRAJECTORY VARIABLES. TIME X 1380.724 21408

C-4. Test Case 3 (Continued)

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BLDG
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JOHN
11/11/65

TIME	1685.897		COORDINATE SYSTEM	SYSTEM LH					
	0P.X	λdO	740	DVX	DVY	700	DOX	AOO	700
0111-01	-2591.	1483.	5.	-1.35	3.59	00.0	0-0	0-0-	0-0-
0112-01	521.	-0-	-12.	0.07	-0.80	0.02	0-0-	0.0	6.4
0113-01	14.	.35.	98.	0.03	-0.04	08.0	6-0-	<b>6</b>	-0-
0131-01	11.	<b>6</b>	2963.	0.0	-0.02	-0.39	-29.5	-5.6	0.1
0132-31	-124.	16.	-1.1.	-0.06	0.11	1.57	-5.6	29.	-0-
0133-01	-5520.	472.	. <u>.</u> 5.	-2.29	4.75	-0.03	0	9.0-	-30.0
A001-01	-2128.	2965	-13.	-1.43	40.M	00.00	-0-	9	-0-
A002-01	31.	60	-1429.	0.05	-0.11	-0.74	o	0-	-0-
A003-01	-2347.	574.	• 9	-1.41	2.82	-0.02	0-	-0-	, o -
A011-01	-4227.	5448.	-34.	-3.63	9.93	0.0	0-	-0-	0-
A012-01	-1:	2.	42.	-0.00	00.00	00.0-	•	•	0
A013-01	-372.	26.	2.	-0.09	0.14	00.0	-0-	-0-	-0-
6001-01	- 78.	36.	1464.	-0.09	0.17	3.84	66.1	119.9	-2.2
6002-01	-37.	**	-2672.	.0	00.00	-2.82	119.9	-66.1	1.5
6003-01	-5361.	2246.	-2.	-4.03	10.30	-0.13	0.3	-3.3	-168.6
6063-01	- 5959-	1546.	14.	-3.28	7.29	<b>90.0-</b>	0.1	-1.2	-61.6

C-4. Test Case 3 (Continued)

			20	δ	<b>†</b>	<b>6</b>	40	20	~	<b>M</b>	8	<b>9</b>	
		700	0.1439E	-0.4881E	-0.7907€	0.9501E 03	-0.2434E	0.91366 01	-0.2538E	0.26038 63	0.33146 05	132.0343	2007 -15889.56 A2 118.073
295		۵۵.۰	3.1732E 05	-0.4513E 04	0.3140€ 06 -0.7907€ 04	0.4965E 01	0.1610E 02 -0.2349E 02 -0.2434E	0.69948 03	0.1965E 06 -0.4959E 01 -0.2538E	0.1968E 05	0-0105	140.2863	A A •∈00
TRAJECTORY TAPE 562		DOX	-0-1199E 05	0.29446 04	C.1194E 05 -0.3069E 06	0.1582E 00 -0.5871E 01		0.2550E 02 -0.3238E 02	0.1965E 08	-0.0003	-0.0010	1.0.1878	
		2,40	6.6226E 53	-0.8878E 02		0.1582E 00	0.4008E 03 -0.7565E 00	0.2550E 02	-0.1137	0.9684	1600.0	5.1483	XDDT -7978,25 VEL 33407,06
C SYN E) MISS		DVY	0.8631F 05 -0.2213E 06 6.6226E 63 -0.1199E 05	0.1454E 06	-0-1352E 03	0.3% /c 02 -0.1489E 03	0.4008E 03	-0.0073	0.0057	-0.0084	-0.6578	20.0191	2 -2315187. ALT :41.70
FHASE LOGIC SYN E) MISSION COORDINATE SYSTEM LH		XAG		0.6463E 08 -0.1966E 36 -0.5135E 05 0.1454E 06 -0.8878E 02 0.2944E 04 -0.4513E 04 -0.4881E 04	0.2062E 08 -0.65775 02 -0.1352E 03	0.5% AC 02	-0.9890	0.0041	-0.0056	0.0047	0.6938	7.5227	Y 6830437. LONG 11.336
		240	0.8490E 05	-0.19668 36	0.2062E 08	-0.0019	-0.0015	0.5109	-0.4821	0.4930	9500*0-	4540.8724	451. I .100
1685.897	COVARIANCE MATRIX	DPY	0.1397E 09 -0.7061E 08	0.6463E 08	-0,0054	-0.84	0.9016	-0.0021	0.0026	- 0*00*0	-0-3330	8051,9474	VARI
31 124 124 124 124 124 124 124 124 124 12	COVARIA	SPX	0.1397E 09	-0.7421	910000	6.9703	-0.9353	6.6102	-0.0072	5-0104	6999*0	S'GHA 11817-7649	33AJECTORY TIME 1695.897

C-4. Test Case 3 (Continued)

PHASE LOGIC SYN EQ MISSION TRAJECTORY TAPE 562 PARTIALS AT T# 7200.000 MITH RESPECT TO T# 1685.897 TRANSITION MATRIX. COORDINATE SYSTEM

(

10
RESPECT
HITH
PARTIALS OF X,Y,7,X00T,Y00T,200T,PHIX,PHIY,PHIZ WITH RESPECT
250T,PH
T, YD01,
7 x x 00
OF X,Y,7,X00T
96
PARTIALS

×	<b>&gt;</b>	7	XDOX	YDGT	2,007	PHIX	<b>PHIY</b>	21H4
4321E 01	-0.9992E 01	-0,4321E 01 -0,9992E 01 -0,5960E-07 -0,8308E 04 -0,6153E 04	-0.8308E 04	-0.6153E 04	0.26558-02 -0.	-0-	-0-	-0-
0.7864E 00		0.7820E 01 -0.7749E-06 0.9465E 04	0.9465E 04		0.1376E 04 -0.2045E-02 -0.	-0-	-0-	٠٥.
0.4470E-07		0.7711E-06 -0.2703E 01 0.4730E-03	0.4730E-03	0.1043E-02	0.2019E 04 -0.	-0-	-0-	-0.
.5697E-03	-0,1442E-02	-0.5697E-03 -0.1442E-02 -0.4366E-10 -0.1562E 01 -0.7863E 00	-0.1562E 01	.0. 7863E 00	0.4396E-06 -0.	-0-	-0,	-0.
0.36786-03		0.2973E-02 -0.2510E-09 0.3134E 01	0.3134E 01	0.7811E 00	0.7811E 00 -0.7451E-06 -0.	-0-	-0-	-0-
.8549E-10	-0.1005E-09	-0.8549E-10 -0.1005E-09 -0.5597E-03 -0.5984E-07	-0.5984E-07	0.3667E-07	0.5561E-01 -0.	-0-	-0-	-0-
••	•0	•0	ç	•0	•	-0.6178E 00 -0.7863E	-0.7863E 30	0.3949E-06
-0-	-0-	-0-	-0-	-0-	-0-	0-7863E 00	0.7863E 00 -0.6178E 00	0.1863E-07
-0-	-0-	• 0-	-0-	-0-	-0-	0.2198E-06	0.2198E-06 0.3101E-06	0.1000E 01
18AJECTURY 1 E 1685-897 7200-000 1685-897 7200-000	20 20 - 71	51. 71. 100 595	Y 6830437. 38640352. LONG 11.336	2 -2315187. -23623653. ALT 141.70	XDUT -7976.25 -12155.85 VEL 33407.06 12382.68		2.52 8.76 8.76 749	2007 -15889.56 435.44 A2 118.073

C-4. Test Care 3 (Continued)

11/11/65 JUHA DUE BLDG N 64 RM 2 TEST CASE 3

PHASE LUCIC SYN EU MISSIUN

TRAJECTORY TAPE 562

	700	-0.0	4.9	-0-1	0.1	-0.6	-30.0	-0-	-0-	-0-	•	•	-0-	3.4	9.3	-719.9	-98.5
	DOY	0.0	-0-1	-3.7	-19.7	-22.6	<b>*•</b> 0	•	•	-0-	•	o o	•	465.1	204.6	9.7	1.3
	XOO	0.0	-0-1	-3.2	22.6	-19.1	••0	ď	•	•	ċ	·°	•	-204.7	465.1	10.1	3.3
	200	-0.00	0.0	-0.01	-1.71	0.51	-0.02	0.01	0.17	-0.00	0.02	-0.02	-0.00	-0.62	1.37	-0.00	-0.01
	DVY	2.03	-0.20	-0.05	-0.01	-0.10	60.4-	7.88	-0-11	-1.37	11.02	υ°00	-0.24	-0.07	0.02	09.0	-2.19
YSTEM LH	DVX	-1.37	0.22	0.03	10.0	0.05	2.30	-5.19	60.0	0.49	-7.59	-0.00	0.21	-0.00	0.63	-2.47	0.56
OURDINATE SYSTEM	240	89-	79.	1341.	-8797.	5193.	-122.	53.	2361.	-53.	108.	-115.	-1-	3794.	1535.	-222•	-128.
J	DPY	1713.	-2.	-64.	-13.	-381.	-15780.	15602.	-173.	-6814.	18598.	5.	-761.	-305-	78.	-9753.	-13629.
TIME = 7200.000	DPX	-14478.	2047.	321.	103.	196.	я913.	-42545.	785,	-1231.	-61109.	-22.	1260.	-329.	76.	-32908.	-1298.
11ME=		0113-01	J112-01	0113-01	0131-01	0132-01	C133-01	A001-01	A002-01	A003-01	4011-01	A012-01	A013-01	CC01-01	C005-01	6003-01	C063-01

C-4. Test Case 3 (Continued)

2007 435.44 A2 66.987	8.76 4.76	4D	XDOT -12155.85 VEL 12362,68	25823653. ALT 10616.61	Y 38640352. LONG 121.590	ABLES. X X -71678571. LAT -17.595	TRAJECTORY VARIABLES. X
726.8398	509.1016	509.1027	2.4532	17.2822	6 11.7403	SIGMA 103033.5176 38273.9966 11328.3386	273.9966
0.5283E 06	-0-0008	-0.0102	0.0085	-0.0082	0.1939	0.0243	0.3162
-0.3615E 04	0.2592E 06 -0.3615E 04	0.6002	0.0103	-0.0028	-0.0040	0.3689	-0.0142
-0.3779E 04	0.6282E 02 -0.3779E 04	0.2592E 06	0.5712	0.0031	-0.0037	-0.0643	0.0001
0.1522E 02	0.1287E 02	0.7134E 03	0.6018E 01	0.0115	-0.0086	1069.0	0.0140
-0.1026E 03	0.2704E 02 -0.2428E 02 -0.1026E 03	0.2704E 02	0.4456E 00	0.2987E 03	-0.9800	0.0106	0.8920
0.1655E 04	-0.2379E 02	.0.2214E 02	0.2464E 00 -	0.1378E 03 -0.1988E 03 -0.2464E 00 -0.2214E 02 -0.2379E 02	0.1378E 03	-0.0072	-0.7925
0.1998E 06	0.2127E 07	.0.3708E 06	0.1,20E 05 -0.3708E 06	0.2076E 04	0.1283E 09 -0.9567E 03	0.1283E 0	0.6154
0.8795E 07	0.1059E 04 -0.2770E 06	0.1059E 04	0.1313E 04	0.5900E 06	07 -0.3561E 06	0.1465E 10 0.6670E 0	0.1465E 10
0.2413E 08	-0.4691E 06	·0.2389E 36	0.1610E 04 -	0.1184E 07 -0.1644E 07 -0.1613E 04 -0.2389E 36 -0.4691E 06		0.1062E 11 -0.2575E 10 -0.4943E 07	0.2575E 10
700	Ang	DOX	7.00	DVY	DYX	2 d Q	DPY
							COVARIANCE MATRIX
	796	TRAJECIURT TAPE 562		PHASE LUGIC SYN EG MISSIUN DINATE SYSTEM LH	COORDINATE SYSTEM		7200.000

C-4. Test Case 3 (Continued)

PARTIALS AT T\* 14400.000 WITH RESPECT TU T\* 7200.009 TRANSITION MATRIX.

	21H4	-0-	•0-	••	•0-	-0-	•0•	0.9013E 00 -0.4333E 00 -0.2608E-07	0.9013E 00 -0.5122E-07	0.1000E 01	2001 435-44 2264-49 A 4 66-987 61-983
	PHIV	•0-	-0-	-0-	-0-	-0-	-0-	-0.4333E 00		0.3725E-07	YDOI -2318.76 -4678.79 FPA 46.749 30.934
	PHIX	•	••	••	•	••	0.	0.9013E 00	0.4333E 00	0.5960E-07	4 T
PECT TO	Z00T	·0.2136E-03	.0.3510E-03	0.6543E 04	·0.1863E-07	.0.5588E-07	0.7740E 00	•0	-0-	-0-	XDDT -12155.85 -4058.41 VEL 12382.68 6594.67
COORDINATE SYSTEM LH Partials of X,Y,2,XDOT,YDOT,2DDF,PHIX,PHIY,PH12 with respict to	YDOT	0.5819E 04 -0.3256E 04 -0.2136E-03	0.7863E 04 -0.3510E-03	0.3357E-03	0.6752E 00 -0.4333E 00 -0.1863E-07	0.1395E 01 -0.5588E-07	0.4057E-07	•0	. 0-		2-25823653. -14220141. ALT 10616.61* 17644.42
',PHIX,PHIY,	XDOT	0.5819E 04 -	0.3293E 04	0.3967E-03	0.6752E 00 -	0.5431E 00	0.5215E-07	•	-0-	-0-	Y 38640352. 10368633. LUNG 121.590 115.165
LH 301,YD01,2D0?	7	-0.2235E-07	-0.2608E-07	0.6610E 00	0.1137E-11	0.3638E-11	-0.7464E-04	•	-0-	• o-	71. 30. 372
COORDINATE SYSTEM PARTIALS OF X,Y,Z,XI	>	. 5980E 00	0.1650E 01	0.7823E-07	.0.2245E-04	0.1891E-03	0.6366E-11 -0.7464E-04	°.	-0-	-0-	7 VARIABL -716 -1269
COORDINA	×	0.5623E 00 - J.5980E 00 -0.2235E-07	0.4333E 00 0.1650E 01 -0.2608E-07	0.46576-07	-0.7464E-04 -0.2245E-04	0.1497E-04 0.1891E-03	-0.31836-11	•			TRAJECTUR TIME 7200.000 14400.000 7200.000

C-4. Test Case 3 (Continued)

11/11/65 JOHN DOE BLOGN 64 RM 2 TEST CASE 3

		700	-0.0	4.9	-0-1	0.1	<b>9.0</b> -	-30.0	•	•	-0-	•	°	•	3.4	9.3	6.6.1-	6.07	11.3		-719.9
		DOV	0°0	9	9.4.	0.9-	-28.9	0.5	•	ė	•	•	ģ	ģ	330.5	385.9	13.1	2.2	428.5	-520.3	13.1
TRAJECTORY TAPE 562		00 x	0.0	0.0-	-1.3	28.9	-8-0	2.0	•	•	•	•	•	•	-386.0	330.5	6.4	<b>9.</b> 0	520.3	428.6	6.4
TRAJECT		7/0	-0.00	0.00	-0-11	-0.67	0.0	-0.00	0.00	0.45	00.0	0.01	-0.01	-0.00	-0.76	<b>*</b> • • •	0.01	0.00	-0-	•	•
EQ MISSION		٥٨٨	2.19	-0-14	-0.05	-0.01	-0.18	-7.31	10.48	-0.13	-2.95	13.77	0.00	-0.34	-0-18	0.05	-2.84	-5.43	ė	ė,	-0-
PHASE LUGIC SYN ED MISSION	SYSTEM LH	DVX	-0.76	0.08	0.02	0.01	0.07	3.02	-4.08	0.05	1.17	-5.31	-0.00	0.17	90.0	-0.01	0.75	2.18	ċ	ċ	ö
PHAS	COORDINATES	740	-21.	106.	812.	-17004.	6788.	-184.	107.	6616.	-63.	200.	-233.	-8-	-1553.	9952.	-179.	-153.	ġ	•0-	-0-
		DPY	7956.		-224.	-45.	-1136.	-46755.	52124.	-551.	-20930.	63298.	15.	-1890.	-1349.	334.	-33758.	-41013.	÷	-0-	-0-
	= 14400.000	DPX	-23752.	3073.	562.	170.	972.	41171.	-89132.	1422.	10723.	-128880-	-39.	3152.	270.	-20•	-28980-	14427.	ċ	•	•
			0111-01	0112-01	0113-61	0131-01	0132-01	0133-01	A001-01	A002-01	A003-01	A011-01	A012-01	A013-01	6001-01	0002-01	6003-01	6063-01	70-7009	20-2009	6003-02

C-4. Test Case 3 (Continued)

		~	68E 08	93E 08	65E 06	53E 04	88E 04	28E 02	00E 04	23E 05	0.1747E 07	1321.5800	6.8%
		700	0.3188E	0.4693E	0.2665E	-0.1253E	0.428BE	-0-19	-0.7600E	-0.20	0.174	1321	2001 2264.49 A2 61.983
			8	0.	0	05	03	03	03	90		382	
295		DOY	-0.44726	0.1819E 04 -0.5590E 35 -0.1640E 07	0.5656E 07 -0.6568E 06	0.5868E 02	0.7080E 01 -0.1808E	0.5916E 03 -0.4305E 03 -0.1928E	0.1445E	0.6346E 06 -0.2023E	-0-0192	796.6382	Y001 -4678.79 FPA 17.934
APE			90	25	07	0	10	03	90			267	Y00Y -467 FP
TRAJECTORY TAPE 562		<b>X00</b>	-0.2621E	-0.5590E	0.5656	-0.2747E	0.70805	0.5916E	0.6343E 06	0.0002	-0.0072	795.4267	7 7
RAS			. 40	. 40	90	ဗွ	00	10			•	66	XDOT -4058.41 VEL 6594.67
		200	0.1716E 07 -0.4386E 07 -0.2216E 04 -0.2621E 06 -0.4472E 06	0.1819E	0.2459E 05	0.8309E 02 -0.2134E 03 -0.1224E 00 -0.2747E 01	0.32818 00	0.2102E 01	5123	3728	-0.0101	1,4499	XD0T -405 VE 059
MIS			10	7.0	40	03	03					88	1.
C SYN EQ		DVY	-0.4386E	0.2855E 07	0.7378E 04	-0.2134E	0.5494E	0.0097	\$1.00 O	-0.0097	0.1384	23.4388	1 -14220141. ALT 17644.42
SYS			20	07	90	05						52	
PHASE LOGIC SYN EQ MISSION COORDINATE SYSTEM LH		XAQ		0.4385E 08 -0.1106E 07	0.4798E 09 -0.2748E 04	0.8309E	0666*0-	-0.0093	-0.0004	0.0081	-0-1040	9.1152	7 10368633. LOPG 115.165
00			90	90	60							132	-
		7 d C	-0.4341E		0.4798E	-7.0138	0.0144	0.7743	0.3242	-0.0376	0.0092	21904.0132	., <sup>c</sup> 5. x 1269,9830. LAT -6.372
• 000	×		1	11								5.4.5	2691 -
14400.000	COVARIANCE MATRIX	<b>V 4</b> 0	0.3952E 11 -0.2099E 11 -0.4341E 08	0.1558E 11	0.0160	-6.9718	0.9760	0.0100	-0.0006	-0.0165	0.2845	SIGMA 198798.2383 124814.354!	VAR
*	AR I A		11									11A 383	RAJECTORY TIME 14400.000
TIME	000	0PX	0.3952E	-0.8458	-0.0100	0.9468	-0.9414	-0.0077	-0.0017	-0.0028	0.1213	S16 198798.2	TRAJ.

C-4. Test Case 3 (Continued)

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PHASE LUGIC SYN EQ MISSION THAJECTOR/ TAPE 562 PARTIALS AT 1= 20177.531 AITH RESPECT TO T= 14400.000 TRANS TION MATRIX. COURDINATE SYSTEM

<u>(</u>

	<b>&gt;</b>	7	XDUT	YDUT	1007	X1H4	PHIY	71Hd
	-0.2525E 00	0.87505 0C -0.2525E 0C -0.3353E-07		0.5441E 04 -0.1345E 04 -0.1831E-03	-0.1831E-03	°.	-0-	٠٥.
_	0.2291E 00 0.1177E 91	0.78466-07	0.1345E 04	0.5995E 04	0.4778E-03	••	-0-	-0-
-	0.2235E-07 -0.9872F-07	0.9016E 00		9.2441E-03 -0.5112E-03	0.5595E 04	•0	.0.	-0-
٠	0.3230E-04 -0.4030E-05	0.11376-11	0.8821E 00	0.8821E 00 -0.2291E 00 -0.3353E-07	-0.3353E-07	•	-0-	•0-
9	U.7022E-04	0.3738E-05 0.7022E-04 0.2103E-11	0.2508E 00	0.1!62E 01	0.9430E-07	•	-0.	-0-
-	-0.39796-12	-0.1137E-11 -0.3979E-12 -0.3230E-04	0.2608E-07	0.2608E-07 -0.8009E-07	0.9087E 00	•	-0-	-0-
	0.	°.	٥.	0.	٥.	0.9734E 00 -0.2291E	-0.2291E 00	00 -0.33536-07
	-0-	-0-	-0-	• •	-0-	0.2291E 00	0.9734E 00	0.7979E-07
	-0-	-0-	-0-	-0-	•0-	0.3353E-07	0.3353E-07 -0.8754E-07	0.10006 01
JECT 11ME 000.00 77.5	Y VARIABL	30. 76. 372	Y 10368633. -16830542. LUNG 115-165	2 -14220141. -150172. ALT 17644.42	XDGT -4058.41 .12.26 VEL 6594.67		YDOT ^4678°79 -4586°59 FPA 30°934	2007 2264-49 2517-13 A2 61-983
20177.531		-0.062	-257.306	19294.65	5248.12	12	1.603	41.325

C-4. Test Case 3 (Continued)

11/11/65 JOHN DOE BLDG N 64 RM 2 TEST CASE 3

			PHAS	PHASE LUGIC SYN ED	ED MISSION	TRAJECT	TRAJECTORY TAPE 562	~	
TIME	= 20177.532		COORDINATE SYSTEM	SYSTEM LH					
	DP.X	DPY	7 40	UVX	AAQ	740	DOX	AO0	700
0111-01	-29881.	007.		-0.44	28.2	-0.00	0.0	0.0	0.0-
0112-01	3316.	-6-		00.00	-0-13	-0.00	0.0-	-0-1	6.4
0113-01	729.	-433.		10.0	-0.07	-0.13	-0-2	6.4-	1-0-
0131-01	208.	-88-		0.0	-0.02	-0.06	30.0	-1.1	0.1
0132-01	1771.	-2074.		0.08	-0.26	-0.21	-1.1	-30.0	9.0-
0133-01	14366.	-85355.		3.19	-10.86	0.00	1.0	9.0	-30.0
A001-02	-127453.	98300.		-3.33	14.49	00.0	•	-0-	-0-
A002-01	1851.	-1043.		0.03	-0-17	0.17	•	• •	-0-
A003-01	25016.	-38301.		1.45	-4.57	00.00	•	÷	0-
A011-01	-176129.	120394.		-3.93	18.63	00.0	· 0	• •	-0-
A012-01	-51.	29.		-0.00	00.0	00.0-	•	•	0,
A013-01	*409*	-3335.		0.13	-0.48	-0.00	•	•	-0-
G001-01	1156.	-2510.	-5672.	60.0	-0.28	-0.64	-451.4	233.3	3.4
6002-01	-592-	642.		-0.92	0.07	0.54	233.3	451.3	9.3
6003-01	-8940.	-62402.		2.38	-5.59	0.02	1.8	13.9	-719.9
0063-01	42127.	-74038.		2,86	-8.60	0.01	0.3	5.4	-126.5
C001-05	Ö	-0-		•	-0-	•	408.3	536.2	11.3
C005-02	•	9		•	-0-	-0-	536.4	-408.3	-6.5
6003-02	•	9		•	-0-	• •	1.8	13.9	-719.9
6001-03	ပ်	9		•	• 0-	-0-	564.8	111.9	3.6
6002-03	•	-0-		ċ	-0-	<b>°</b> 0;	111.9	-564.7	-10.6
6003-03	•0	•0-		·.	-0-	-0-	1.4	11.1	-517.6

C-4. Test Case 3 (Continued)

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TRAJECTORY TAPE 562

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0.9334E 08 -0.1497F 37 C.7613E 07 3.4659E 03 -0.8447E 35 -0.3633E 37 0.1C44E C9 C.8095E 07 -0.5196E 07 0.7531E 05 0.4172E 01 0.1366E 03 -C.3988E 04 0.7815E-01 -0.7816E JI -0.3700E D3 0.9695E 04 0.7928E 00 0.2832E 03 -0.4599E 03 -0.3489E 02 0.1163E 37 3.9286E C2 -0.4771E 04 0.1164E 07 -C.3701E 05 0.5726E UT 0.7873E 11 -6.6056E 11 -0.8625E 08 0.2051E 07 -0.8927E 07 -0.7969E 03 -0.7117E 35 3.6063E 06 DOY 0.0001 Š 0.1242E 05 0.6620E 02 -0.2522E 03 -0.1467E-01 0.2950 -0.4788 7 A Q 0.1237E 05 0.1032E 04 0.0027 -0.00ci -0.0104 ۸ 0 0.7039E 09 -0.3269E 04 -0.9798 -0.0020 0.0005 0.0156 -0.0151 0.0142 0.5256 0.2823 -0.1016 **7** d Q 0.5462E 11 COVARIANCE MATRIX 0.0151 -0.9378 3066.0 0.0022 -0.00e 0.0144 7 0.9236 9110-0-3.8984 9196.0. .0.0u 32 -0.0002

0.8404 1078.3660 1078.7023 1755.8879 2517.13 61.325 2001 -4565.59 1.603 FrA vel 5248.12 412.26 ALT 19234.65 -150172. 32.8489 8.1365 LUNG -257.306 -16430543. 280585.7891 233703.2031 26530.8992 -68566478. -0.062 TRAJELTORY VARIABLES. 20111.532

0.3083E 07

-0°0195

-0.0325

-0.0223

0.1679

-0.2772

0.0016

0.2545

0.0116

0.0020

C-4. Test Case 3 (Continued)

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7144	-0.25396	-0.1808E	0.17506	-0.8656E	-0.3610E	0.5456E	0.4798t 00	0.1755E-	0.8774E 00	2507 2517.13 0.30 A2 61.325 69.998
A I Wa	0.5538E 02 0.5703@ 03 -0.1261E 06 -0.2539E 04	-0-1324E 04	0.3839E 04 0.2750E 06 0.1750E 04	0.3100E 02 -0.2517E 04 -0.8656E 02	-0.2046E 02	0.1125E 03 0.5491E 04 0.5456E 02	0.8774E 00 -0.5696E-02	0.5532E-02 0.1000E 01 G.1755E-02	-0.4798E 00 0.1114E-02	YDOF -4586.59 -10011.07 FPA 1.603 0.001
хІнд	0.57032 03	0.2425E 06	0.38396 04	0.3100E 02	0.4843E 04	0.1125E 03	0.87746 00	0.5532E-02	-0.4798E 00	
7007	0.5338E 02	0.19538 00	0.9761E 02	0.47 18E 0C	C.1755E-02	0.6773E 00	• 0	•0	-0-	XDUT 412.26 1286.42 VEL 5248.12 10093.40
rbor	3.8773E 00 -0.5596E-02 0.4798E 00 0.9761E 02 -0.6337E 00	0.1755E-02 0.6155E 00 0.1113E 03 0.1953E 00 0.2425E 06 -0.1324E 04 -0.1808E 06	0.1240E 00	-3.5209E-06 -3.2337E-08 -0.2847E-06 0.8773E 00 -0.5696E-02	0.1216F-08 0.1187E-05 -0.5084E-10 0.5532E-02 0.1000E 01 0.1755E-02 0.4843E 04 -0.2046E 02 -0.3610E 04	0.1114E-02 0.6773E 00	•0	•0		2 -150172. 3822. ALT 192945 19296.30
XDOT	0.9761E 02	0.6155E 00	0.8773E 00 -0.5338E 02 0.1240E 07	0.8773€ 00	0.5532E-02	0.3361E-10 -0.5209E-06 -0.479HE 00	•0	•	-0-	Y -16830543. -17612547. LONG -257.306
7	0.47986 00	0.17556-02		-0.2847E-06	-0.5084E-10	-0.5209E-06	٥.	•0	-0-	78. 46. 062
<b>&gt;</b> -	-0.5596E-02	0.10006 01	0.11146-02	-0.21396-08	0.11875-05	0.3361E-10	o•	٥.	• 0 -	Y VARIABL -685 -685
×	3.8773£ 00	0.5532E-02	-0.4798E 00	-0.5209E-06	0.1216E-08	3.28498-06	•	٠.	.0-	TRAJECTUR 11ME 2017:532 20288.784 201:7.532 20288.784

C-4. Test Case 3 (Continued)

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C-4. Test Case 3 (Continued)

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7	-70364.	16156.	14355.	-0.33	2.04	0.20	0.0-	0-0	-0-0
01:2-01	2151.	.6-	-1505.	-0.00	17.0-	-0.00	7.7	1-0-	
0113-01	699.	-437.	-262.	0.01	10°C-	-0.25	200	7.4	
-	-4465	-87.	-16830.	-0.00	69.0	-0.05	26.3		~ 1 6 . 3
0132-01	4542.	-2C84.	4498.	0.33	. D. 20	-1.02	-1-1-	0.06-	0
10-6610	u5696.	-96130-	-35764.	2.83	-10,42	-1.51	-14.3	2.5	-26.4
10-1004	-112653.	93210.	61548.	- 54.46	65.41	1.54	3		
10-2004	7636.	-1038.	642).	0.11	i	0.13	0		, c
10- £00v	17284.	-38672.	-12169.	1.23	09-4-	-0.64	o	•	0
A011-01	-155481.	121499.	85036.	-3.15	08. × 1	1.68	0	• •	0-
4012-01	-162.	. 59.	-188.	0.23	-0.00	0.42	<b>.</b>	ံ	0-
A013-01	*990*	-3365.	-2230.	0.12	-0.52	-0.07	ô	0	•
10-1000	-1991-	-3080°	-5299.	-3.14	10.01	5.36	-305.8	230.B	217.8
0005-01	6350°	937.	13246.	-5.24	5.35	12.62	206.6	452.6	-103.3
5003-01	-1293.	-62442.	4027.	2.27	64.49	96-0-	-345.9	12.6	-632.4
6063-01	37607.	-75253.	-20561.	2.57	-6.45	-1.33	4°0°-	7.7	-1111-1
20-1000	-327,	468.	723.	-6.43	9.34	14.50	360.6	538.5	-185.4
C005-02	.152	638.	-534.	5.03	12.75	-10.58	469.8	-405-3	-263.5
20-8005	Ċ	633.	12.	0.13	12.64	0.18	-365.9	12.5	-632.4
A001-03	55.		-38.	96.0	0.13	-3.51	·	3	0-
A002-03	-2).	-	-55-	-0.51	0.02	-0.04	• 0	· ^	-0-
A303-03	• <b>9-</b>	54.	*	-01.0	1.07	90.0	· 0	Ċ	-0-
c001-03	91.	665.	160.	-1.24	13.33	3.31	506.3	110.3	-273.0
6002-03	348.	144.	-756.	60.9	64.7	-15.14	11.4	-575-2	
1	*3	512.	10.	0.11	10.25	0.15	-261.3	500	
	•\$	ċ	•0-	-0.00	01.0		ဂ	0	-0-
•	°.	<b>.</b>		0.00	00.0	0.10		ó	
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0.3131	.E 21	C-1572F 3	3.6165E 11 -0.5408E 11 -0.3131E 11 0.1570E 07 -0.7740E 07 -0.8455E 06	-3.80556		3-53411 3	0.5341L D7 -0.2678E 07	01 0.17471 07
0.245	8F 11	-C-1614E U	0.2958E 11 -C.1634E 07 G.53r7E 07 G.4104E 06	15018.0		1.5056E 0	0.5056E 08 -0.348IF UT	// C.4948E U8
0.189	)E 11	-0.7707E C	0.1890E il -0.7702E 06 0.4561E 07 0.37415 36 0.5156E 07 -0.3176E 07 -C.5549E 07	914/6-0	90	2.5156E D	7 -0.3176E	37 -C.5549E
-0.3787		0.23031 0	0.2303E 03 -0.1385E 03 -0.444E 73 -0.1830E 34 -0.1444E 35 -0.4045E 04	-0.4.48	)- (0	0.1830E U	4 -0.14446	34 -0.4045E
0.6835		-6.1340	0.23516 04	0.10116 03	33 (	).2835E 0	0.2835£ 04 0.1738 03 -0.5248E 05	33 -0.5248E
6.0343		9676*0-	0.0726	0.8232E 03		90 31651.0		0.3083E 05 0.1095E 04
0.0295		-0.0932	0.0459	P250°C	•	3.1621E 0	0.1621E 07 -0.1622E CS 0.6127F 06	36 0.61236
-0.0226		09/8-0-	0.0053	26.00	ĭ	-0.0117	0.11796	0.1179E 27 -3.2983E 05
-0.0247		-0.1630	-0.6612	0.0233	J	0.3905	-0.0168	U-2673E 07
SIGMA 248340.5996 235512.0918 137476.6055	5055	15.1766	6 48.5454	1169.87	11	1273.0711	1 1085.9502	02 1635.0835
TREJECTURY VARIABLES.  TIME  X0288.704 -68522446.  LAT  0.062	ť	7 -17612647. LOYG -257.445	, 3822. 3LT 19296.30		1286.42 VEL 10093.40		You! -10011-39 FPA 5-001	2.0 05.0 A2.0 89.98

C-4. Test Case 3 (Continued)

226 001 001 001 001 001 001 001 001 001
21 0. 0.4534 0.4554 0.1439 0.01439 0.1439
DIRECTION CUSINES  27  27  27  27  27  27  27  27  27  2
DIRLCTION CUSINES  12  2X  17  18002  151299  151299  153408  153408  173629  173629
DIRLCT 12 0.478002 -0.151299 -0.173408 -0.475256 -0.472669 0.472629
17 -0.429553 0.429553 0.444430 0.444430 0.8175572 0.881396 -0.081356 -0.881245
PHI 0.143746 -0.0464 0.890277 86.4644 0.840395 85.8585 0.840395 85.8585 0.840395 85.8585 0.995668 95.6738 -0.995668 81.1369 -0.275320 83.4671 -0.005332 83.1675 -0.005332
PHI -0. 86.4044 86.1639 85.8785 85.8785 85.8788 81.1369 83.4671 83.1675
PSI 0. 97. 1481 98.3971 99.1109 117.8193 117.8193 117.865 68.8626 62.5356 61.5917
AT THETA 89.345 -3.5615 -4.1259 4.7966 19.6488 54.3153 8.7985 6.4381
11ME 0 464.664 477.664 498.375 1380.724 1685.897 7200.000 14400.000

C-4. Test Case 3 (Concluded)

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# APPENDIX D

# RESETS

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#### APPENDIX D

#### RESETS

### D. 1 INTRODUCTION

"Resets" is the term applied to correction schemes for updating inertial system navigation data as a result of measurements made by sensors other than the inertial elements (gyros and accelerometers). These measurements can be made by ground equipment from which processed navigation data is transmitted to the navigation computer; or airborne sensor data can be used by the computer to update the navigation data. Many sensor configurations and data processing schemes could be used, but only a few are discussed here. It is assumed for this analysis that only a limited number of corrections would be made, although many measurements might be used and pro-filtered to obtain the measured value used for reset.

## D. 2 MEASUREMENTS CONSIDERED

The measurements considered are components of position, velocity, and/or platform orientation as follows:

#### a. Position Measurements

- (1) altitude
- (2) slant range to a ground station
- (3) position vector in the ECI or orbit plane (see Section 2.4.1) coordinate system as derived by a ground station and transmitted to the airborne computer

#### b. Velocity Measurements

- (1) altitude rate
- (2) slant range rate to a ground station
- (3) velocity vector (ECI or orbit plane coordinates) as derived by a ground station

#### c. Angular Measurements

- (1) angular measurements with respect to inertial space, using a stellar sensor
- (2) angular measurements with respect to the local vertical (assumed geocentric), using a horizon sensor
- (3) platform error vector as derived from multiple stellar sensor or horizon sensor measurements.

In developing the appropriate reset equations, it was desired to retain the common notation of Y for measurement vectors and X for state vectors. For this reason, there is some ambiguity between this notation and that of coordinates of the position and velocity vectors (e.g., see Section D.6). It is hoped that this ambiguity will not cause confusion in interpretation.

Three reset methods are considered that use the same form for correcting the state vector. The concept for deriving the form of the reset equations is obtained from the following considerations. A measurement is functionally related to the navigation duta and is corrupted by some noise. This relationship is shown by

$$Y_i = F_i(X) + N_i$$

where

Y; is ith measurement

F<sub>i</sub>(X) is the functional relationship (see Section D. 6 for explicit forms)

X is the true state vector (9 elements)

N<sub>i</sub> is the error (noise plus bias) of the i<sup>th</sup> measurement (a random variable)

Likewise a vector of measurements can be constructed as

$$Y = F(X) + N$$

The measurement state vector can be estimated from the navigation system data as

$$\hat{\mathbf{Y}} = \mathbf{F}(\hat{\mathbf{X}})$$

where  $\hat{X}$  is the navigation system estimate of the state vector X and is in error by  $\Delta X$ , that is

$$\hat{\mathbf{X}} = \mathbf{X} + \Delta \mathbf{X}$$

where  $\Delta X$  is a random variable, which is the sum of the effects up to time (t) of all the error sources (P in number), that is

$$\Delta \mathbf{X} = \sum_{i=1}^{\mathbf{P}} \frac{\partial \mathbf{X}_{i}}{\partial \epsilon_{i}} \epsilon_{i} = \sum_{i=1}^{\mathbf{P}} \delta \mathbf{X}_{i} \epsilon_{i}$$

Then the difference between  $\hat{Y}$  and Y can be calculated and used to estimate  $\Delta X$  and/or  $\epsilon_i$ . That is

$$\Delta Y = \hat{Y} - Y$$
$$= F(X + \Delta X) - F(X) - N$$

 $F(X + \Delta X) - F(X)$  can be expanded into a Taylor Series so that

$$\Delta Y = \frac{\partial F}{\partial X} \Delta X + \cdots - N$$

where  $\partial F/\partial X$  is the matrix formed by taking the partial derivatives of F(X) with respect to X for each measurement. All higher-order terms are assumed to be zero.

Again, for purposes of error analysis, it is desired to obtain the sensitivities of  $\Delta Y$  to each error source. Therefore

$$y = Mx - u$$

where the notation has been adopted that

- y = sensitivity (vector for multiple measurements) of the measurement state with respect to the i<sup>th</sup> error source  $\partial \Delta Y / \delta \epsilon$ ;
- $M = \partial F/\partial X$  is an m x n matrix in which m equals the number of functionally independent measurements at time t and n = 9
- $x = \text{navigation sensitivity state vector } \partial X / \partial \epsilon_{i}$
- u = unit vector (one for each measurement), as described
  in Section 2. 3. 3. (An explicit symbol EKlm is not given
  here.)

The Reset Equation is developed by letting

or

$$\hat{X}_{R} \triangleq \hat{X} - K\Delta Y \text{ (or) } \Delta X_{R} = \Delta X - K\Delta Y$$

where  $\hat{X}_{p}$  is the estimated state vector after the measurement correction(s) and K is an n x m matrix developed in the sequel.

Taking the partial derivatives of this expression with respect to each error source, it is seen that the state vector sensitivity for each error source is changed when a measurement is made, that is

$$\delta \Delta X_{R} = \delta \Delta X - K \delta \Delta Y$$

$$x_{R} = x - Ky$$

$$= x - KMx + Ku$$

$$= (I - KM) x + Ku$$

NOTE: The notation and form of this equation are the same as for Kaunan filtering (Reference 6), except that x and u are consitivity (w. r. s. t. random variable) vectors, rather than vectors of random variables.

It remains to establish the matrix K in the above equation. Three methods are considered here, which are termed: replacement reset, deterministic reset, and linear statistical reset.

The development of each of these methods will now be described.

#### D. 3 REPLACEMENT RESET

In using this technique, it is assumed that the measurement error is much smaller than the state vector error; thus, the measurement difference(s) ( $\Delta Y$ ) is assumed to be dependent on the navigation state vector error only. The constraint of the correction is such as to make  $\Delta Y_R = 0$ , and therefore

$$\Delta Y_{R} = \hat{Y}_{R} - Y = 0 = M\Delta X_{R} - N$$

Taking the partial derivatives of this expression results in

$$y_R = Mx_R - u$$

$$= (I - MK)(Mx - u) \stackrel{\triangle}{=} 0$$

In order for this condition to be satisfied for all x, the first term must equal zero. Therefore

$$MK = I$$

post multipling by [MM<sup>T</sup>]

$$MK[MM^T] = MM^T$$

from which K is determined as

$$K = M^T [MM^T]^{-1}$$

K is sometimes referred to as the pseudo-inverse of M.

Thus, the reset sensitivity state vectors for all error sources active up to time t, based on this constraint, are

$$x_r = [I - KM]x$$

Additionally, new sensitivity state vectors are generated to account for each measurement error by

x<sub>m</sub> = Ku

which are essentially initial condition errors at time t.  $x_r$  and  $x_m$  represent the total set of sensitivity vectors x, which are subsequently operated upon as independent sensitivity vectors. Thus, any operations including additional resets at time t would include  $x_m$  in the set of state vectors.

A few remarks about  $[MM^T]^{-1}$  are in order here. For most measurement types considered (e.g., an individual position measurement, a stellar rensor sighting or a platform reset, or a position and/or velocity correction from the ground),  $[MM^T]^{-1} = I$ .

For individual velocity measurements and nonorthogonal measurements (e.g., simultaneous altitude and slant range measurements),  $[MM^T]^{-1} \neq I$ .

Functionally dependent measurements (such as altitude and slant range when the slant range vector is along the radius vector, and overdetermined measurements when two stellar sightings give four measurements of platform angle errors), result in singular inverses. The pseudo-inverse could be invoked for the altitude and slant range example, which would in effect result in the average of the two measurements. The case of the two stellar sightings should be reformulated by partitioning the state vector into the orientation elements only, from which the least squares solution ([M<sup>T</sup>M]<sup>-1</sup>M<sup>T</sup>) can be used.

The question of sequential (at time t) reset vs simultaneous reset is of interest. The M matrix is formed from row vectors of partials. If the dot product of these vectors is zero, and the cross product is one, then sequential or simultaneous reset is equivalent. However, if both these conditions are not satisfied, the order of sequential reset is important.

An elternate and generally equivalent approach is one in which a transformation matrix is developed, which transforms the state vector in ECI coordinates into a state vector in the measurement coordinate system. The elements that are measured are set to zero, and the resultant state vector is transformed back by the inverse of the transformation matrix. This method suffers in that simultaneous multiple measurements usually cannot be included in the reset technique; therefore, multiple measurements would have to be handled sequentially and sometimes only in a specific order.

#### D. 4 DETERMINISTIC RESET

In this method it is assumed that the measurement differences are solely dependent on an equal number of error sources. A typical example would be the use of a stellar tracker to derive the launch position errors of a mobile missile system, and thus compensate for the error. The technique developed here is not restricted to measurement types or the error sources to be considered. The concept is developed as follows. Let

$$\Delta X_D = D\epsilon_D$$

where

 $\Delta X_D$  = the error in X due to the error source vector  $\epsilon_D$ 

 $D = an n \times m$  matrix formed from the sensitivity vectors of  $\epsilon_D$ 

E = an m vector of error sources to be determined from
the measurement(s)

In using this technique, it is assumed that the measurement error is much smaller than the effect of the state vector error, and that the state vector error due to all other error sources is much smaller than the state vector error due to  $\epsilon_{\rm D}$ . Therefore, the measurement differences ( $\Delta Y$ ) are assumed to be dependent on the error vector only, so that

$$\Delta Y_D = M\Delta X_D = MD\epsilon_D$$

$$\epsilon_{D} = [MD]^{-1} \Delta Y_{D}$$

However,  $\epsilon_D$  can only be estimated from  $\Delta Y$  (the quantity derived from the measurements), so that the estimated value of  $\epsilon_D$ ,  $\hat{\epsilon}_D$  is

$$\hat{\epsilon}_{\mathrm{D}} = [\mathrm{MD}]^{-1} \Delta Y$$

The state vector estimate is corrected by using the estimate of  $\epsilon_{D}$ , as follows

$$\hat{\mathbf{x}}_{\mathbf{R}} = \hat{\mathbf{x}} - \mathbf{D}\hat{\boldsymbol{\epsilon}}_{\mathbf{D}} = \hat{\mathbf{x}} - \mathbf{D}[\mathbf{M}\mathbf{D}]^{-1}\Delta\mathbf{Y}$$

Thus, it is seen that for this correction scheme

$$K = D[MD]^{-1}$$

and

$$x_r = (I - KM)x$$

The sensitivity vector corrections follow the same procedure as for the replacement reset; each sensitivity vector is corrected at time t, and new sensitivity vectors are added to account for the measurement errors. The constraints on [MD]<sup>-1</sup> are that the measurements be functionally independent and that the error sources to be determined do not have equal sensitivities.

It is apparent from the state vector reset equation that the explicit determination of  $\hat{\epsilon}_D$  is not required for corrections of the navigation data. Also, it can be shown that the reset sensitivity state vector for each element of the  $\epsilon_D$  vector is set to zero at the reset time, provided that the sensitivity matrix D, used in the reset equations, is formed from the sensitivity vectors of the error analysis discussed in detail in the next paragraph. Thus, the navigation errors resulting from  $\epsilon_D$  vector errors are zero at reset time,

regardless of the magnitude of the  $\epsilon_{\rm D}$  vector (assuming the elements of  $\epsilon_{\rm D}$  are not large enough to invalidate the linearity assumption). If the  $\epsilon_{\rm D}$  vector were composed of initial condition elements only, the effects would be negleted and new error sources formed by the measurement error vector. On the other hand, if the  $\epsilon_{\rm D}$  vector had elements representing forcing functions (such as accelerometers, drag, etc.), it might be desirable to use the estimate of  $\epsilon_{\rm D}$  to compensate those parameters, thereby reducing the variance of navigation errors following the reset time. For this procedure, it is necessary to determine the variance of the estimate error, which can be calculated, when desired, from the relationship

$$\hat{\epsilon}_{D} = [MD]^{-1} \Delta Y$$

$$= [MD]^{-1} \{M \Delta X_{D} + M \Delta X_{P-D} - N\}$$

$$= \epsilon_{D} + [MD]^{-1} M \sum_{i=1}^{P-D} \delta \chi_{i} \epsilon_{i} - [MD]^{-1} \sum_{j=1}^{M} \epsilon_{j}$$

where

 $\boldsymbol{\varepsilon}_{1}$  are all error sources excluding the set  $\boldsymbol{\varepsilon}_{D}$ 

 $\epsilon_j$  are the measurement errors

Thus, the estimate error is defined as

$$\Delta \epsilon_{\mathbf{D}} = \hat{\epsilon}_{\mathbf{D}} - \epsilon_{\mathbf{D}}$$

and, assuming that the measurement errors are independent of the other error sources, the variance covariance of the estimate error can be calculated as

$$E(\Delta \epsilon_{D} \Delta \epsilon_{D}^{T}) = [MD]^{-1} \left\{ M \sum_{m=1}^{\infty} M^{T} + Q \right\} ([MD]^{-1})^{T}$$

where

is the covariance matrix of navigation state vector errors excluding a parameters at reset time (before the measurement is included)

Ū

Q is the covariance matrix of measurement errors at reset time

In the application of this method, the sensitivity matrix D would be obtained in one of the three following ways:

- a. Input based on a nominal trajectory
- b. Computed by using the normalized integral approach (which excludes the effects of gravity feedback in navigation equations)
- c. Computed in a manner similar to the equations of this program.

Approach (a) should be adequate for most applications for the same reason that a nominal trajectory suffices for error analysis. Approach (b) more closely approximates the true sensitivities for a given trajectory and is not a difficult computation for an airborne computer. An analysis of either of the first two methods requires the generation of the D matrix from alternate runs, which would then be treated as input data. Method (c) is self-contained, but more complex for airborne computations.

### D. 5 LINEAR STATISTICAL RESET

This is equivalent to the Kalman filtering technique (Reference 6), but it is developed differently. Certain assumptions are made to facilitate the development of the problem at hand, but as the technique presented is a general one, assumptions need not be made. The one basic restriction made, on both the Kalman filtering technique and the method here, is that of the best linear estimate of the random variables in the sense of minimizing the mean square error of the estimate. The development uses the conditional expectation function directly. For the scalar case it is well known that

$$\hat{\mathbf{E}}(\mathbf{X} \mid \mathbf{Y}) = \rho_{\mathbf{X}\mathbf{Y}} \frac{\sigma_{\mathbf{X}}}{\sigma_{\mathbf{Y}}} \mathbf{Y}$$

(The notation  $\hat{\mathbf{E}}$  is adopted to distinguish it from the normal operator  $\mathbf{E}$  in the conditional expectation function, because of the restriction of best <u>linear</u> estimate. However, if the stochastic processes are Gaussian, the operators are equivalent. This same notation is used in Reference 6.)

$$\widehat{\mathbb{E}}(X \mid Y) = \frac{\mathbb{E}(XY)\sigma_X}{\sigma_X\sigma_Y} Y = \mathbb{E}(XY)[\mathbb{E}(Y^2)]^{-1} Y$$

For X and Y vectors, it can be shown that the same form holds as

$$\hat{\mathbf{E}}(\mathbf{X} \mid \mathbf{Y}) = \mathbf{E}(\mathbf{X} \mathbf{Y}^{\mathbf{T}}) [\mathbf{F}(\mathbf{Y} \mathbf{Y}^{\mathbf{T}})]^{-1} \mathbf{Y} = \mathbf{K} \mathbf{Y}$$

where the elements of K in this expression (an n x m matrix) are termed regression coefficients (Reference 7, Chapter 23, p 302).

For the problem at hand, it is desired to estimate AX, the error in the state vector estimate, given the measurement difference AY, or

$$\Delta \hat{X} = \hat{E}(\Delta X | \Delta Y) = E(\Delta X \Delta Y^T)[E(\Delta Y \Delta Y^T)]^{-1} \Delta Y$$

and based on this estimate, the state vector estimate would be corrected as follows

$$\hat{X}_{R} = \hat{X} - \Delta \hat{X} = \hat{X} - K \Delta Y$$

where

$$\hat{\mathbf{E}} = \mathbf{E}(\Delta \mathbf{X} \Delta \mathbf{Y}^{\mathbf{T}}) [\mathbf{E}(\Delta \mathbf{Y} \Delta \mathbf{Y}^{\mathbf{T}})]^{-1}$$

As defined previously

$$\Delta Y = M\Delta X - N$$
 ,  $\Delta Y^T = \Delta X^T M^T - N^T$ 

and therefore

$$K = E(\Delta X \Delta X^{T} M^{T} - \Delta X N^{T})[M E(\Delta X \Delta X^{T}) M^{T} - M E(\Delta X N^{T}) - E(N \Delta X^{T}) M^{T} + E(N N^{T})]^{-1}$$

Assuming that the inertial navigation system parameters are independent of measurement errors, this reduces to

$$\mathbf{K} = \left\{ \sum_{\mathbf{m}} \mathbf{M}^{\mathbf{T}} - \mathbf{D}_{\mathbf{n}} \mathbf{R}_{\mathbf{n}}(\mathbf{t}, \tau) \right\} \left[ \mathbf{M} \sum_{\mathbf{m}} \mathbf{M}^{\mathbf{T}} - \mathbf{M} \mathbf{D}_{\mathbf{n}} \mathbf{R}_{\mathbf{n}}(\mathbf{t}, \tau) - \mathbf{R}_{\mathbf{n}}^{\mathbf{T}}(\mathbf{t}, \tau) \mathbf{D}_{\mathbf{n}}^{\mathbf{T}} \mathbf{M}^{\mathbf{T}} + \mathbf{R}_{\mathbf{n}}(\mathbf{t}, t) \right]^{-1}$$

where

is the covariance matrix of navigation errors at reset time

 $R_n(t,\tau)$  is a matrix of time correlation functions (including cross-correlation terms) for the measurement errors

 $D_n$  is a matrix that propagates the effects of measurements made at a previous time (or at the same time but processed sequentia'ly)

 $R_n(t, t)$  represents the covariance matrix of measurement errors at time t.

If it is assumed that the measurements are independent (and time and timecross-correlation functions are zero), the gain expression can be further reduced to

$$K = \sum_{i=1}^{n} M^{T} \left[ M \sum_{i=1}^{n} M^{T} + Q \right]^{-1}$$

The effects of the previous assumptions can be determined, however, since the calculation of  $\sum$  in the program includes the effects of time and time-cross-correlated errors independent of the assumptions for obtaining K. The simplified gain computation represents a more realistic one for airborne use. Finally, the reset state vector sensitivity is

$$x_r = x - Ky$$

$$= [I - KM]x$$

which is in the same form as the previous methods. Additionally, a new vector is formed for each measurement, and the complete set of sensitivity vectors is handled in the same manner as Methods 1 and 2 (in Sections D-3 and D-4).

This reset technique could be extended to include the estimation of the envor sources as follows

$$\hat{\mathbf{E}}(\mathbf{c}|\mathbf{\Delta Y}) = \mathbf{E}(\mathbf{c}\mathbf{\Delta Y}^{\mathrm{T}})[\mathbf{E}(\mathbf{\Delta Y}\mathbf{\Delta Y}^{\mathrm{T}})]^{-1}\mathbf{\Delta Y}$$

where e = the error vector to be estimated, and

where D = the sensitivity matrix of all error sources.

Therefore

$$\hat{\epsilon} = \hat{\mathbf{E}}(\epsilon | \Delta \mathbf{Y}) = \mathbf{E}[\epsilon \epsilon^{\mathrm{T}} \mathbf{H}^{\mathrm{T}} - \epsilon \mathbf{N}^{\mathrm{T}}][\mathbf{E}(\Delta \mathbf{Y} \Delta \mathbf{Y}^{\mathrm{T}})]^{-1} \Delta \mathbf{Y}$$

Making the same assumptions as before, that  $E(\epsilon N^T) = 0$ ,

$$\hat{\epsilon} = \sum_{\epsilon} H^{T} [M \sum_{\epsilon} M^{T} + Q]^{-1} \Delta Y$$

where

 $\sum_{\epsilon} = E(\epsilon \epsilon^{T}) = \text{covariance matrix of all error sources}$   $\sum_{\epsilon} \text{can also be written as } D \sum_{\epsilon} D^{T}$ 

By using the above relationships,  $\hat{\epsilon}$  can also be written

$$\hat{\epsilon} = [D^T D]^{-1} D^T K \Delta y = K_{\epsilon} \Delta y$$

provided that  $\{D^TD\}^{-1}$  exists. If it is singular, then the pseudo-inverse, which always exists, can be developed. However, it is not required, since the original formula does not present this problem.

For purposes of an error analysis, it is necessary to derive the variance of the estimate error  $(\Delta \epsilon = \hat{\epsilon} - \epsilon)$ , which is

$$\mathbb{E}(\Delta \epsilon \Delta \epsilon^{\mathrm{T}}) = \mathbb{E}\{(\hat{\epsilon} - \epsilon)(\hat{\epsilon}^{\mathrm{T}} - \epsilon^{\mathrm{T}})\}$$

and reduces to

$$\sum_{\epsilon R} = (I - K_{\epsilon} H) \sum_{\epsilon}$$

where  $\sum_{\epsilon R}$  is the covariance matrix of the reset error source parameters.

There are several approaches that can be used to compensate the navigation data, given the estimate of the error vector; the most straightforward being to reset the sensor error equation.

It is seen that, in theory, the navigation data and error source parameters can be corrected, given one or more measurements. Thus, from the standpoint of minimum navigation error in the sense of the least-mean-squared-error under the constraint of a linear estimate, an optimum use of the data would incorporate both navigation data and error-source reset.

Practically, the task described would overburden any airborne computer, and in particular the computation of the D matrix. Although the estimate of  $\hat{\epsilon}$  could be partitioned so that only a selected few would need to be estimated, all sensitivities are required (or should be) for the calculation of  $\sum$ . For that reasc it is assumed that calculation of the sensitivities (D matrix elements) would be based on the nominal trajectory; therefore, it would be precomputed and inserted in the airborne computer for flight data processing.

In the special case of free flight (orbit navigation), most forcing functions reduce to zero; and the problem can be reformulated so that  $\sum$  can be updated by using the transition matrix in conjunction with those forcing functions

acting in orbit (drag, gravity model constants, gyro drift, control system impulses, etc.). The capability to perform this last analysis, that is, orbit reset or orbit navigation, is presently under development in a separate program. A report describing it will be published by J. Meditch of Aerospace Corporation.

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#### D. 6 M MATRIX GENERATION

The M matrix is assumed to be computed by the airborne computer and based on the functional relationships of the measured quantities (Y)\* and the navigation data  $(\bar{X}, \bar{X}, M_{EP})$ . Each measurement represents a row of the M matrix and is developed as follows for the measurements considered.

#### D. 6. 1 Altitude

$$Y = h = R - R_e = \sqrt{X^2 + Y^2 + Z^2} - R_e$$

$$\delta \mathbf{Y} = \frac{\partial \mathbf{Y}}{\partial \mathbf{X}} \ \delta \mathbf{X} = \frac{\overline{\mathbf{X}}^{\mathrm{T}}}{\overline{\mathbf{R}}} \ \delta \overline{\mathbf{X}}$$

and

$$\mathbf{m} = \begin{bmatrix} \mathbf{X} & \mathbf{Y} & \mathbf{Z} \\ \mathbf{R} & \mathbf{R} & \mathbf{R} \end{bmatrix} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \quad 0$$

where it has been assumed that  $\partial R_{\mu}/\partial X = 0$ 

#### D. 6. 2 Slant Range to a Ground Station

The slant range vector is defined as

$$\begin{split} \widetilde{S} &= \widetilde{R}_{G} - \widetilde{R} \\ &= (X_{G} - X)\widetilde{X}_{U} + (Y_{G} - Y)\widetilde{Y}_{U} + (Z_{G} - Z)\widetilde{Z}_{U} \\ &= X_{S}\widetilde{X}_{U} + Y_{S}\widetilde{Y}_{U} + Z_{S}\widetilde{Z}_{U} \end{split}$$

<sup>\*</sup>See comment on notation at end of Section D-2.

where

$$X_{G} = R_{e} \cos \lambda_{G} \cos \phi_{G}$$

$$Y_{G} = R_{e} \cos \lambda_{G} \sin \phi_{G}$$

$$Z_{G} = R_{e} \sin \lambda_{G}$$

$$R_{e} = \frac{A(1 - e)}{\sqrt{1 + (e^{2} - 2e) \cos^{2} \lambda_{G}}}$$

and the terms in this equation are as defined in Section 2. 3. 3.

$$Y = S = \sqrt{X_S^2 + Y_S^2 + Z_S^2}$$

$$\delta Y = \frac{\partial Y}{\partial X} \delta X = -\frac{X_S^T}{S} \delta \bar{X}$$

$$m = \left[ -\frac{X_S}{S} - \frac{Y_S}{S} - \frac{Z_S}{S} \quad 0 \quad 0 \quad 0 \quad 0 \quad 0 \right]$$

It is assumed that station locations are perfectly known, and also that timing errors are zero.

- D. 6. 3 Position Vector
- D. 6. 3. 1 ECI Coordinates

$$m = [I_{(3\times3)}^{0}, 0_{(3\times3)}^{0}, 0_{(3\times3)}^{0}]$$

### D. 6. 3. 2 Local Coordinates

$$m = [M_{LE}G_{(3\times3)}O_{(3\times3)}]$$

where  $M_{
m LE}$  is defined as in Section 2.4.1

#### D. 6.4 Altitude Rate

$$Y = \dot{h} = \frac{dR}{dt} = \dot{R} = \frac{\overline{X}^T}{R} \dot{\overline{X}} = \frac{X\dot{X} + Y\dot{Y} + Z\dot{Z}}{R}$$

$$\begin{split} \delta \dot{\hat{\mathbf{h}}} &= \frac{\overline{\mathbf{X}}^{\mathrm{T}} \delta \dot{\overline{\mathbf{X}}}}{R} + \frac{\dot{\overline{\mathbf{X}}}^{\mathrm{T}} \delta \overline{\overline{\mathbf{X}}}}{R} - \frac{\dot{R} \delta R}{R} \\ &= \frac{1}{R^{2}} \big[ \, (R \dot{\overline{\mathbf{X}}}^{\mathrm{T}} - \dot{R} \overline{\mathbf{X}}^{\mathrm{T}}) \delta \overline{\mathbf{X}} + R \overline{\mathbf{X}}^{\mathrm{T}} \delta \dot{\overline{\mathbf{X}}} \big] \end{split}$$

from which

$$\mathbf{m} = \left[ \frac{\mathbf{R}\dot{\mathbf{X}} - \mathbf{X}\dot{\mathbf{R}}}{\mathbf{R}^2} \frac{\mathbf{R}\dot{\mathbf{Y}} - \mathbf{Y}\dot{\mathbf{R}}}{\mathbf{R}^2} \frac{\mathbf{R}\dot{\mathbf{Z}} - \mathbf{Z}\dot{\mathbf{R}}}{\mathbf{R}^2} \frac{\mathbf{X}}{\mathbf{R}} \frac{\mathbf{Y}}{\mathbf{R}} \frac{\mathbf{Z}}{\mathbf{R}}, 0 \ 0 \ 0 \right]$$

## D. 6. 5 Slant Range Rate

$$Y = \frac{dS}{dt} = \frac{\overline{X}_S^T \dot{\overline{X}}_S}{S} = \frac{X_S \dot{X}_S + Y_S \dot{Y}_S + Z_S \dot{Z}_S}{S}$$

where

$$\begin{split} \dot{\bar{\mathbf{X}}}_{S} &= \dot{\mathbf{X}}_{S} \overline{\mathbf{X}}_{U} + \dot{\mathbf{Y}}_{S} \overline{\mathbf{Y}}_{U} + \dot{\mathbf{Z}}_{S} \overline{\mathbf{Z}}_{U} \\ &= (\dot{\mathbf{X}}_{G} - \dot{\mathbf{X}}) \overline{\mathbf{X}}_{U} + (\dot{\mathbf{Y}}_{G} - \dot{\mathbf{Y}}) \overline{\mathbf{Y}}_{U} + (\dot{\mathbf{Z}}_{G} - \dot{\mathbf{Z}}) \overline{\mathbf{Z}}_{U} \\ &= (-\omega_{\mathbf{e}} \mathbf{Y}_{G} - \dot{\mathbf{X}}) \overline{\mathbf{X}}_{U} + (\omega_{\mathbf{e}} \mathbf{X}_{G} - \dot{\mathbf{Y}}) \overline{\mathbf{Y}}_{U} - \dot{\mathbf{Z}} \overline{\mathbf{Z}}_{U} \\ \\ \delta \dot{\mathbf{S}} &= -\frac{1}{S^{2}} \left[ \left( \mathbf{S} \dot{\overline{\mathbf{X}}}_{S}^{T} - \dot{\mathbf{S}} \overline{\mathbf{X}}_{S}^{T} \right) \delta \overline{\mathbf{X}} + \mathbf{S} \overline{\mathbf{X}}_{S}^{T} \delta \overline{\mathbf{X}} \right] \end{split}$$

and the form of m is the same as for altitude rate with the substitutions of  $\overline{X} = \overline{X}_{S'}$ ,  $\overline{X} = \overline{X}_{S'}$ , R = S, and R = S. Station location and timing errors are assumed to be zero.

## D. 6. 6 Velocity Vector

#### D. 6. 6. 1 ECI Coordinates

$$m = [0_{(3\times3)}I_{(3\times3)}0_{(3\times3)}]$$

### D. 6. 6. 2 Local Coordinates

$$m = \left[0_{(3\times3)}M_{LE}0_{(3\times3)}\right]$$

#### D. 6. 7 Stellar Sensor Measurement

It is assumed that the sensor is mounted on the platform and can be slewed in azimuth about the platform 1-axis, and in elevation about the tracker 2-axis to sight on a prescribed star. Figure D-1 shows the tracker axes system with respect to the platform axes. The transformation between a vector in platform

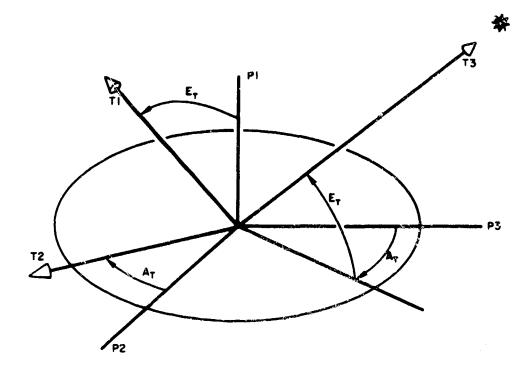


Figure D-1. Stellar Sensor (Tracker) - Coordinate System

coordinates and tracker coordinates is

$$\mathbf{M_{TP}} = \begin{bmatrix} \mathbf{CE_T} & \mathbf{0} & -\mathbf{SE_T} \\ \mathbf{0} & \mathbf{1} & \mathbf{0} \\ \mathbf{SE_T} & \mathbf{0} & \mathbf{CE_T} \end{bmatrix} \begin{bmatrix} \mathbf{1} & \mathbf{0} & \mathbf{0} \\ \mathbf{0} & \mathbf{CA_T} & -\mathbf{SA_T} \\ \mathbf{0} & \mathbf{SA_T} & \mathbf{CA_T} \end{bmatrix}$$

where

A<sub>T</sub> is the azimuth of the star expressed in nominal platform coordinates

E<sub>T</sub> is the elevation of the star expressed in nominal platform coordinates

The tracker is capable of measuring coordinates (small angles) only about its 2-axis (a coordinate along the Tl axis), and about its 1-axis (a coordinate along the T2 axis). Alternately, it can measure the changes in  $A_T$  and  $E_T$ , which make the above coordinates zero. Mathematically either measurement type is equivalent. Since the platform rotation errors are assumed to be small, they can be treated as vectors, so that

$$\begin{bmatrix} \phi_{1T} \\ \phi_{2T} \end{bmatrix} = \begin{bmatrix} CE_T & -SE_TSA_T & -SE_TCA_T \\ 0 & CA_T & -SA_T \end{bmatrix} \begin{bmatrix} \phi_1 \\ \phi_2 \\ \phi_3 \end{bmatrix}$$

where

 $\phi_{1\mathrm{T}}$  is a measurement along the sensor's 2-axis

 $\phi_{2T}$  is a measurement along the sensor's 1-axis

Therefore, for a single stellar fix with a stellar sensor, two angles can be used to correct the effect of platform extors. In this case

$$\mathbf{m} = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & \mathbf{CE_T} & -\mathbf{SE_TSA_T} & -\mathbf{SE_TCA_T} \\ 0 & 0 & 0 & 0 & 0 & 0 & \mathbf{CA_T} & -\mathbf{SA_T} \end{bmatrix}$$

For the case of two independent stellar sightings (two different stars, preferably 90° apart and in the platform's  $^2p_p^3$  plane), the platform orientation errors are overdetermined. In this case, least squares or other techniques could be used to process the four measurements so that the platform error angles were determined explicitly. This is implied in the last measurement category (Section D. 6. 9), Platform Error Vector.

### D. 6.8 Horizon Senso: Measurements

A horizon sensor primarily measures small-angle deviations of its mount with respect to local vertical; the measurements can also be processed to indicate altitude. Conventionally, it is mounted on the vehicle frame and used as a reference for the vehicle control system, while maintaining small-angle deviations of the vehicle axes with respect to local vertical.

In conjunction with platform gimbal-angle readout (direction cosines in the case of strapped-down inertial systems) and the navigation system position data, the angles measured by the sensor can be used to correct the platform angular errors, navigation system position errors, or both. For purposes of a general analysis of the use of the horizon sensor, the local horizontal coordinate system will be used. It is assumed that the sensor measures pitch (rotations about the Z-axis of the local horizontal system) and roll (rotations about the X-axis). Transformed into this system, the state vector error is

$$\overline{\Delta X}_{L} = M_{LE} \overline{\Delta X}$$

where M<sub>LE</sub> is as described in Section 2.4.1.

Under these assumptions, the sensor measures

$$\Delta\theta = -\frac{\Delta X}{R} + \phi_Z - n_{\theta}$$
 pitch measurement

$$\Delta \phi = \frac{\Delta Z}{R} + \phi_X - n_{\phi}$$
 roll measurement

where

ΔX = range error in local coordinates

ΔZ = cross-range error in local coordinates

 $\phi_{Z'}$  = platform error about Z in local coordinates

 $\phi_{X}$  = platform error about X in local coordinates

 $n_{\theta}$  and  $n_{\phi}$  = pitch and roll sensor errors.

Thus

$$\mathbf{m} = \begin{bmatrix} -\frac{1}{R} & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & \frac{1}{R} & 0 & 0 & 0 & 1 & 0 & 0 \end{bmatrix} \underline{\mathbf{M}_{LE}}$$

## D. 6.9 Platform Error Vector

In this case, it is assumed that the platform error angles are derived from multiple stellar sensor measurements and expressed in platform coordinates. Therefore

$$^{\text{m}} = \left[ {}^{0}(3\times3) {}^{0}(3\times3) {}^{\text{M}} \text{PE} \right]$$

The M matrix for any given reset is then constructed, based on any one or more of the m matrices presented above. The combinations, however, must be limited so that elements of the state vector are not overdetermined when the Method 1-type reset is used.

## D. 7 RESET EQUATION SUMMARY

This section summarizes the pertinent equations presented for reset.

Those marked with an asterisk could be conveniently mechanized in the error analysis program.

$$\hat{X} = X + \Delta X$$

navigation system estimate of the state vector

$$\Delta Y = \hat{Y} - Y = M\Delta X - N$$

navigation system processed measurement difference

$$\hat{X}_{R} = \hat{X} - K\Delta Y$$

navigation system reset estimate of the state vector given the measurement(s) Y

$$\Delta X_R = \Delta X - K \Delta Y$$

state vector error following reset

$$* x_r = [I - KM]x$$

reset error-source sensitivity vector(s) for all error sources active prior to current reset time

added sensitivity vector(s) to account for the reset measurement error

\* 
$$M = \frac{\partial F}{\partial X}$$

measurement sensitivity matrix (see Section D. 6)

K is determined by one of the following 3 methods:

a. Replacement

\* 
$$K = M^T [MM^T]^{-1}$$

b. Deterministic

$$* K = D[MD]^{-1}$$

where D is formed from the prescribed state vector sensitivities or is input.

$$\hat{\epsilon}_{D} = [MD]^{-1} \Delta Y$$

navigation system estimate of the prescribed error sources, given the measurement(s) Y.

$$\Delta \epsilon_{\mathbf{D}} = \hat{\epsilon}_{\mathbf{D}} - \epsilon_{\mathbf{D}}$$

error of the estimated error sources

$$\sum_{ED} = [MD]^{-1} M \sum_{ED} M^{T} + Q ([MD]^{-1})^{T}$$

covariance matrix of the estimated error sources

where

is the covariance matrix of the navigation state vector errors due to all error sources excluding of parameters at reset time (before the measurement is included)

Q is the covariance matrix of measurement error(s) at reset time

c. Linear Statistical

$$* K = \sum_{i=1}^{n} M^{T} \left[ M \sum_{i=1}^{n} M^{T} + Q \right]^{-1}$$

where

is the covariance matrix of the navigation state vector error due to all error sources at reset time

Q is the covariance matrix of measurement error(s) at reset time and  $\sum_{i=1}^{n} and Q$  are input.

$$\hat{\epsilon} = \sum_{\epsilon} [MD]^T [M \sum_{i=1}^{T} M^T + Q]^{-1} \Delta Y$$

navigation system estimate of the error sources, given the measurement Y.  $\epsilon$  could be partitioned so that only a selected few need be explicitly derived, e.g.,  $\hat{\epsilon}_D$  as in Method 2

where

D is the sensitivity matrix of all (or partitioned) error sources

 $\sum_{\epsilon}$  is the covariance matrix of all (or partitioned) error sources

$$\sum_{\epsilon R} = [I - K_{\epsilon}MD]\sum_{\epsilon}$$

where

The R = the covariance matrix of error sources after reset

$$K_{\epsilon} = \sum_{i=1}^{n} [MD]^{T} [M\sum_{i=1}^{n} M^{T} + Q]^{-1}$$

APPENDIX E
DRAG ERRORS

#### APPENDIX E

#### DRAG ERRORS

In this appendix is discussed the proposed method for estimating the effects of atmospheric drag errors, when the accelerometers are disconnected during orbital flight phases.

If there were no forces experienced by the vehicle during coast periods (parking orbits, transfer orbits, etc.), the most advantageous way to operate the navigation system would be to disconnect the accelerometers during these periods so that the accelerometer bias error would not be integrated. For low-altitude orbits (in the region of 100 n mi), aerodynamic drag force is not negligible, but is generally of the same order of magnitude as accelerometer bias. Consequently, it must be decided either to measure drag via the accelerometer, or to predict it by an empirical formula. The decision would be contingent on which method would result in the least error, i.e., on the uncertainty of accelerometer bias vs the uncertainty of drag calculations. To fully answer this question, a detailed knowledge of the configuration and flight time (function of time of day, month, and year) is necessary. For purposes of the error analysis, these characteristics are generalized so as to assess the relative importance of drag and thereby determine if more detail is required. Therefore, the configuration's ballistic coefficient and the parameters of the atmospheric density model are treated as random variables, with assumed means and standard deviations.

When utilizing a drag model for calculating the sensed acceleration, the equations of motion become

$$\frac{\ddot{x}}{\ddot{x}} = -\frac{\mu}{R^3} \ddot{x} + \ddot{A}_D$$

where

 $\overline{\mathbf{A}}_{\mathbf{D}}$  = vector of drag accelerations

$$= -\frac{\binom{C_D S}{m}}{V} \stackrel{\cdot}{X}$$
 (assuming that drag acts along the negative inertial velocity vector)

where

C<sub>D</sub> = drag coefficient

S = reference area (ft<sup>2</sup>)

m = system mass (slugs)

q = dynamic pressure  $(lb/ft^2)$ =  $1/2 \rho V^2$ 

where

 $\rho = atmospheric density (slug/ft<sup>3</sup>)$ 

V = magnitude of inertial velocity vector (assuming magnitude of inertial velocity equals magnitude of relative velocity)

$$\overline{A}_D = -(\frac{g_0}{2B} \rho V) \dot{\overline{X}} = -A_D \dot{\overline{X}}$$

where

 $B = \frac{W}{C_D S} = ballistic coefficient$ 

g<sub>o</sub> = reference gravity constant (= 32.174)

W = vehicle weight (lb)

The linearized differential equations are

$$\delta \dot{\overline{X}} = M_G \delta \overline{x} - \delta A_D \dot{\overline{X}} - A_D \delta \dot{\overline{X}}$$

where  $M_G$  is as defined in Section 2.3.2

and

$$\delta A_D = A_D (\frac{\delta V}{V} + \frac{\delta \rho}{\rho} - \frac{\delta B}{B})$$

The first term in  $\delta A_D$  is derived as follows

$$V = (\dot{x}^2 + \dot{\dot{x}}^2 + \dot{z}^2)^{1/2}$$

$$\delta V = \frac{\dot{x}}{V} \delta \dot{x} + \frac{\dot{y}}{V} \delta \dot{y} + \frac{\dot{z}}{V} \delta \dot{z} = \frac{\dot{x}^T \delta \dot{x}}{V}$$

The second term can be approximated at any given altitude as

$$\rho(h) = \rho(h_0) + \frac{\partial \rho}{\partial h} \Big|_{h_0} (h - h_0) = K_1(h_0) + K_2(h_0)h$$

where  $h_0$  is the reference altitude, thus  $\delta \rho = \delta K_1 + \delta K_2 h + K_2 \delta h$ .

In general, density variations are sufficiently homogeneous in a region so that  $\delta K_2 = \partial \rho / \partial h|_{h_O} \stackrel{4}{=} 0$ ; and  $\delta K_1$  can be expressed as a percentage of  $\rho(h_O)$ ; i. e.,  $\delta K_1 = (\delta \rho(h_O)/\rho(h_O))\rho(h_O)$ 

$$\frac{\delta \rho}{\rho} = \frac{\delta \rho(h_0)}{\rho(h_0)} + \frac{1}{\rho} \frac{\partial \rho}{\partial h} \delta h$$

Now h is obtained from

where

$$R_{e} = \frac{A(1 - e)}{(1 + (e^{2} - 2e)\cos^{2}\lambda)^{1/2}}$$

$$\cos^{2}\lambda = \frac{X^{2} + Y^{2}}{R^{2}} \text{ (geocentric latitude)}$$

$$e = \frac{1}{298.3} \text{ (ellipticity)}$$

A = equatorial radius

$$\delta h = \delta R \qquad (\delta R_e \approx 0)$$

$$= \frac{\overline{X}^T \delta \overline{X}}{R}$$

Thus

$$\frac{\delta \rho}{\rho} = \frac{\delta \rho(\mathbf{h}_{o})}{\rho(\mathbf{h}_{o})} + \frac{1}{\rho} \frac{\partial \rho}{\partial \mathbf{h}} (\frac{\overline{\mathbf{X}}^{T} \delta \overline{\mathbf{X}}}{R})$$

The third term is simply

$$B = \frac{w}{C_D S}$$

$$\delta B = -B \frac{\delta C_D}{C_D} \qquad (\delta W = \delta S = 0)$$

Combining these results into the linearized differential equations results in

$$\delta \vec{\overline{X}} = M_G \delta \vec{\overline{X}} - A_D (\frac{\dot{\overline{X}}^T \delta \dot{\overline{X}}}{V^2} + \frac{1}{\rho} \frac{\partial \rho}{\partial h} (\frac{\overline{X}^T \delta \overline{X}}{R}) + \frac{\delta \rho (h_o)}{\rho (h_o)} + \frac{\delta C_D}{C_D}) \dot{\overline{X}} - A_D \delta \dot{\overline{X}}$$

$$= [M_G + M_{xx}] \delta \vec{\overline{X}} + M_{xx} \delta \dot{\overline{X}} + \overline{F}_A$$

where

$$M_{\dot{x}x} = -\frac{1}{\rho} \frac{\partial \rho}{\partial h} A_D V[\frac{\dot{x}x}{\dot{x}x}]$$

$$M_{\dot{x}\dot{x}} = -A_D \left[ \frac{\dot{x}\dot{x}}{v^2} + I \right]$$

$$\overline{F}_A = -(EQOO)A_D^{\dot{X}}$$

In this particular case, EQOO is a scalar and equals 1 when deriving the sensitivity of aerodynamic forces (i.e., due to the rss value of  $\delta\rho(h_0)/\rho(h_0) + \delta C_D/C_D$ ).

When considering relatively short time durations (less than 2 orbits) in a drag environment (a 100-mile orbit), these expressions can be further simplified as

a. the coefficient of  $M_G$  is  $\mu/R^3 \stackrel{!}{=} 1.4 \times 10^{-6}$  and

 $\hat{\mathbf{O}}$ 

$$\mathbf{M}_{iox} = \frac{1}{\rho} \frac{\partial \rho}{\partial h} \mathbf{A}_{D} \mathbf{V} = \frac{8.10^{-8}}{3}$$

for B in the range 10 < B < 100

$$M_G >> M_{xx}$$

$$\mathbf{M}_{\mathbf{x}\mathbf{x}}^{\bullet} = \mathbf{C}$$

b. the coefficient of  $M_{xx} = A_D = 4 \times 10^{-7} / B < 4 \times 10^{-8}$  and

$$\delta \bar{x} > > \delta \bar{x}$$

so that  $M_G \delta \overline{x} >>> M_{\stackrel{\cdot}{x}x} \delta \overline{x}$ 

$$M_{xx} \stackrel{!}{=} 0$$

The validity of these assumptions can always be ascertained by utilizing Reference 9, which includes these effects as well as the first earth oblateness term (J<sub>2</sub>). The intent here is only to assess the relative importance of atmospheric effects, so that when the results indicate that more accuracy is required, Reference 9 will be used for detailed studies. Thus, the equations for drag uncertainty reduce to the same differential equations as those for the other error sources, with the forcing function of

$$\overline{F}_{A} = - (EQOO)A_{D}^{\dot{X}}$$

where

$$A_{D} = (\frac{g_{o}}{2B} \rho V)$$

$$B = \frac{W}{C_D S}$$
 (an input constant)

 $\log \rho = f(h) + K_B$  (an input table plus a scaling constant)

$$\rho = e^{2.30258 \log \rho}$$

It remains to establish methods for specifying the mean values of B and p, and some estimate of their deviations. With the assumptions that the region of interest is in orbital velocities at greater than 80 miles, and the configurations of interest are upper stages with payloads attached, the drag coefficient for zero angle of attack and molecular flow can be approximated by

$$C_D = C_{DF} + 0.256 \frac{L}{D}$$

where  $\mathbf{C}_{\mathbf{DF}}$  is the drag coefficient for the shape of the payload section. Typical values are

flat plate C<sub>DF</sub> = 2.11

20° cone C<sub>DF</sub> = 2.04

15° cone C<sub>DF</sub> = 2.03

L = the length of the cyaindrical section (excluding come sections)

D = the diameter of the cylindrical section

Using this formulation of drag coefficient produces approximately a 20percent uncertainty in its magnitude, provided the assumptions of molecular flow and sero angle of attack are maintained.

The upper atmospheric density is affected by many parameters, by far the most by solar activity. In Reference 10 are discussed the various factors that influence the density and they are summarized as follows:

- Diurnal (Day-Night Effect). The density varies with the time of day, having its minimum at night and maximum at approximately 2:00 P.M. local standard time. The effect is a function of the angle between the earth sun line and the radius vector and, therefore, depends on lattitude as well as longitude. The effect is small (15 percent) at low altitude (100 mmi) and increases with altitude to more than 100 percent at 200 n mi (utilizing Eq. (10) in the Jacchia formula, given in Reference 11).
- b. Solar Activity (11-Year Cycle). There is still a rather large discrepancy in models for this effect, as evidenced by the curves presented in Reference 10: Figure 1 for the Jacchia 1960 model and Figure 2 for the Paetzold 1962 model. However, there is reasonably good agreement in the low-altitude region. The variation between the average densities during active and quiet periods is a factor of 3 and related to the decimetric flux (specifically, the 10.7-cm radiation). Jacchia's model relates density directly, resulting in a factor of 3 for all altitudes. Paetzold's model results in factors greater than 10 at 200 n mi that generally increase with altitude. In addition to the 11-year cycle, there are 27-day cycles and semiannual and annual cycles, which result in approximately 25-percent variations at 100 n mi and also increase with altitude.
- c. Magnetic Storms. These are generally unpredictable, but their effects are relatively short-lived, lasting for only a few days. The effects are proportional to the storm's intensity and can vary as much as 40-percent at 100 n mi and much more at higher altitudes.

Based on the Dove, and on the premise that 100 n mi is the principal altitude for parking orbits, etc., the nominal (mean) atmospheric density model was conservatively chosen as the 1959 ARDC (see Table E-1). It can be

Table E-1. Nominal Atmospheric Density - ARDC 1959 Model

Density (slug/ft <sup>3</sup> )	4.116×10 <sup>-12</sup>	1.020 × 10-12	$2.014 \times 10^{-13}$	4.949 × 10 <sup>-14</sup>	9,028 × 10-15	2.336×10 <sup>-15</sup>
Log Density (slug/ft <sup>3</sup> )	-11.4264	-11.9914	-12.6960	-13,3055	-14.0444	-14,6315
.altitude (ft)	$480 \times 10^3$	608 × 10 <sup>3</sup>	550 × 10 <sup>3</sup>	1.1 × 10 <sup>6</sup>	1.46 × 10 <sup>5</sup>	1.8 × 10 <sup>6</sup>
Altitude (n mi)	,6 <i>t</i>	100+	140-	181	140+	295 <sup>+</sup>

scaled up or down to include the average solar activity effects.\* Combining all the effects of density and drag coefficient uncertainties, so as to estimate a standard deviation for purposes of assessing the relative importance of aerodynamic effects, a conservative value of 0.2 (standard deviation of EQOO) is recommended.

()

Other density models can be easily input, if required, for which Figure E-presents curves.

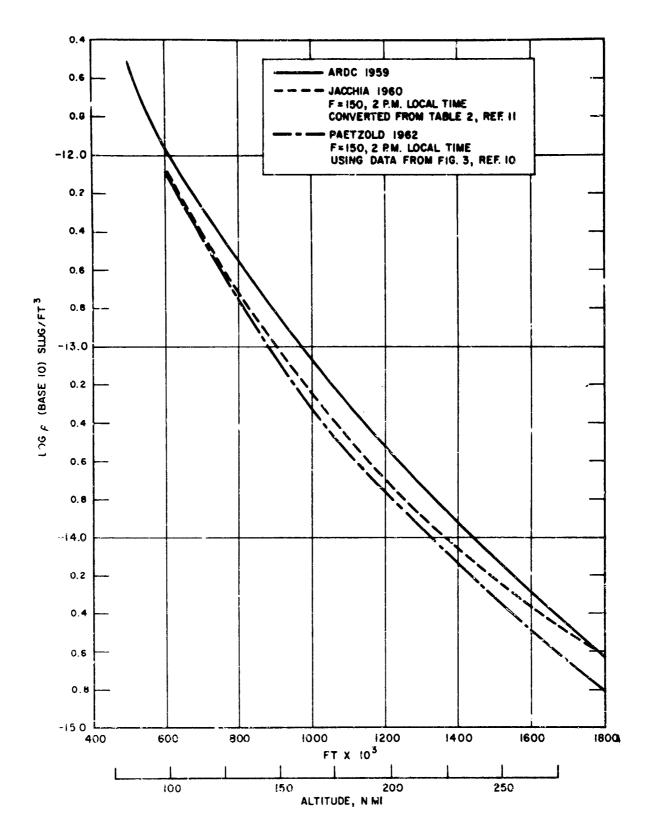


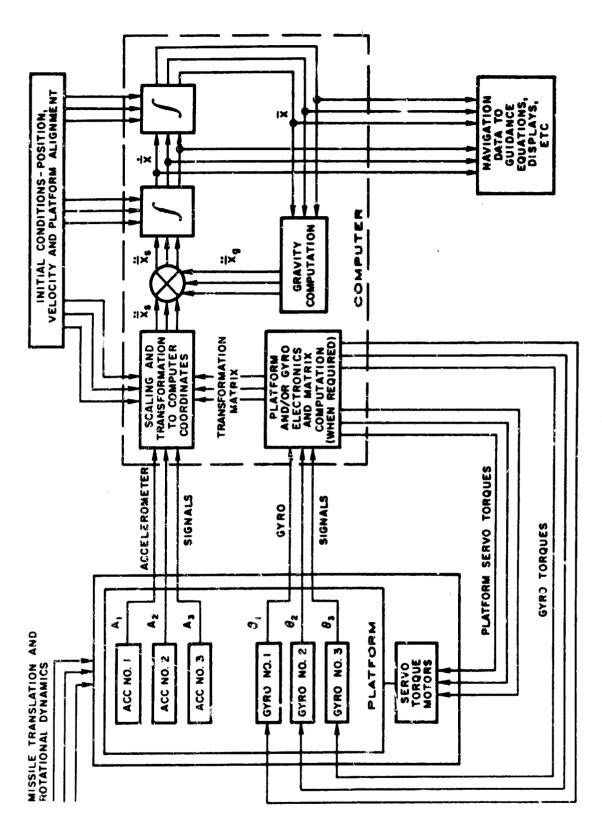
Figure E-1. Log Density vs Altitude Curves

## APPENDIX F

# FIGURES

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Figure 1. Schematic of Navigation System Configuration

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Figure 2. Initial Platform Orientation

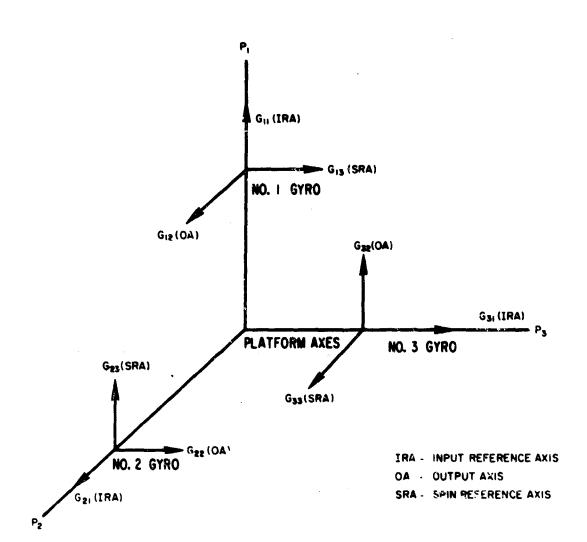


Figure 3. Initial Gyro Orientation

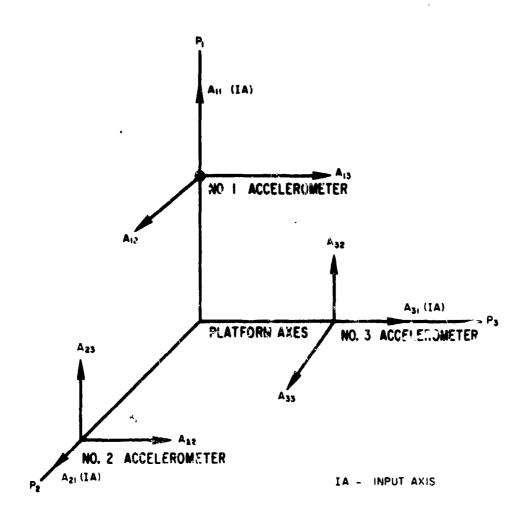
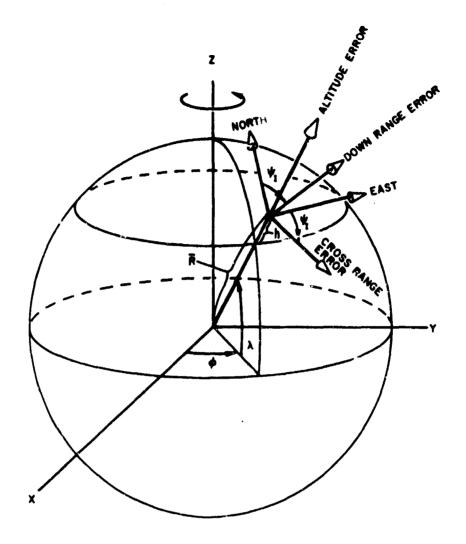


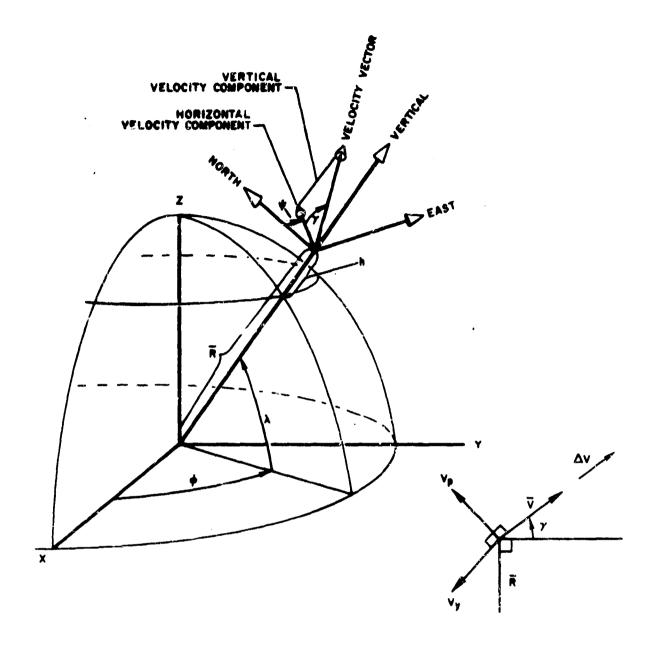
Figure 4. Initial Accelerometer Orientation - Orthogonal Configuration



AS SHOWN, INITIAL CONDITION ORIENTATION OPTION 2

- FINITIAL LONGITUDE
- A INITIAL GEOCENTRIC LATITUDE
- R INITIAL RADIUS VECTOR
- h INITIAL ALTITUDE
- FROM NORTH TOWARDS EAST

Figure 5. Coordinate System for Initial Condition Errors



DOWN RANGE IS DEFINED ALONG THE PROJECTION OF VELOCITY VECTOR ONTO HORIZONTAL PLANE

V. IS PITCH COMPONENT OF VELOCITY ERROR

Vy IS YAW COMPUMENT OF VELOCITY ERROR

AV IS VELOCITY MAGNITUDE ERROR

Figure 6. Coordinate System for Terminal Condition Errors

## APPENDIX G

# PROGRAM DEFINITIONS AND CONSTANTS

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Table G-1. Error Sources

O

Symbol	Description	Units
	Iritial Condition*	
EI11	Initial altitude error	#
EI12	Initial cross_range error	#
EII3	Initial downrange error	#
EI21	Initial altitude rate error	ft/sec
E122	Initial prossurange rate error	ft/sec
E123	Initial downrange rate error	ft/8ec
EI31	Initial platform error about I (aximuth) axis	<b>36</b> C
E132	Initial platform error about 2 (level) axis	(30)
EI33	Initial platform error about 3 (level) axis	\$ <b>0</b> 00
	Accelerometers	
EA00	Accelerometer(s) bias	90
EA01	Accelerometer(s) scale factor	8/8
EA02	Accelerometer(s) second-order nonlinearity	8/8
EA03	Accelerometer(s) third-order nonlinearity	8/8
EA04	Accelerometer(s) cross-axis sensitivity (misalignment, etc)	g/g(rad)
EA05	Accelerometer(s) cross-axis sensitivity (misalignment, etc)	g/g(rad)
EA06	Accelerometer(3) cross-coupling sensitivity	8/8

\*These definitions are consistent with initial condition Option 2 and platform orientation Option 1.

Table G-1, Error Sources (Continued)

Symbol	Description	Units
	Accelerometers (Cont'd)	
EA07	Accelerometer(s) cross-coupling sensitivity	8/8
EA08	Accelerometer(s) sensitivity to normal acceleration	8/8
EA09	Accelerometer(s) cross-coupling sensitivity to normal acceleration	_
EA10	Accelerometer(s) cross-axis squared sensitivity	2/8/2
EAII	Accelerometer(s) cross-axis squared sensitivity	2/8/2
EA12	Accelerometer(s) cross-axis tuct sensitivity	78/3
***************************************	Cyros*	
EGen	Gyro bias	deg/hr
EG91	Sensitivity due to acceleration along input axis	dag/hr/g
EG02	Sensitivity due to acceleration along spin axis	deg/hr/g
EG03	Sensitivity due to accleration along input and spin axes	deg/hr/g2
EG04	Misalignment about gyro output axis	8 CC
EG05	Misalignment about gyro spin axis	( es
EG06	Torquer scale factor error	ę ;
EG07	Sensitivity due to acceleration along output and spin axes	deg/hr/g <sup>2</sup>
EC08	Sensitivity due to acceleration along output axis	deg/hr/g
EG09	Sensitivity due to acceleration squared along input axis	deg/hr/g <sup>2</sup>

\*Descriptive of single-degree.of-freedom gyro.

Table G-1. Error Sources (Concluded)

Units		deg/hr/g	deg/hr/g		sec/g	800/8	sec/g <sup>2</sup>		ft	ft	ft	ft/sec	ft/sec	ft/sec
Description	Gyros* (Cont'd)	Sensitivity due to acceleration squared along spin axis	Sensitivity due to acceleration along input and output axes	Platform	Rotation about platform i axis due to acceleration along j axis	Rotation about platform i axis due to acceleration along k axis	Rotation about platform i axis due to acceleration along j and k axes	Terminal Conditions	Terminal altitude error	Terminal cross-range error	Terminal downrange error	Term and pitch component of velocity error	Terminal yaw component of velocity error	Terminal magnitude of velocity error
Symbol		EG10	EG11		EP01	EF02	EP03		ET11	ET12	ET13	ET21	ET22	ET23

\*Descriptive of single-degree-of-freedom gyro.

Table G-2. Orientation and Control Data

Unite	Sop	deg	ge g	des	deg	deg	deg	deg	deg	deg	\$	9 6 7	<b>8</b> ec	<b>8</b> e C	3ec
Nominal Value	0	0	0	0	0	0	0	0	0	0	0	100	1000	0	8
Description	Eu.er angles used for initial platform	orientation. Generally $\phi_{\rm p}$ is longitude, $\lambda_{\rm p}$	is latitude and $\psi$ is platform azimuth	Azimuth reference for initial position and velocity errors (option 2)	Rotation of No. 1 gyro about its input axis	Rotation of No. 2 gyro about its input axis	Rotetion of No. 3 gyro about its input axis	Rotation of No. 1 accelerometer about its input axis	Rotation of No. 2 accelerometer about its input axis	Rotation of No. 3 accelerometer about its input axis	Option for control of ERAN tape writing density	Power flight tape writing density ( $OUT \neq 0$ )	Free flight tape writing density ( $\phi$ UT $\neq$ 0)	Initial time point to read from trajectory tape	Abort time for reading trajectory tape
Symbol	ψ →PSIP	Ø →PHIP	λ LAMP	ψ <sub>I</sub> →PSII	\phi_1 -PS11	ψ <sub>2</sub> →PSI2	ψ <sub>3</sub> -PSI3	β <sub>1</sub> -BETA 1	β <sub>2</sub> -BETA 2	β <sub>3</sub> -BETA 3	ØUT	PPF	PFF	TSUEO	TSUBA

Table G-2. Orientation and Control Data (Continued)

C

Swarboil	Door	Nominal	
Symbol	Dest ription	Value	Units
TRAJ	Trajectory or file number to be processed	None*	,
ENDC	Location for the equation of metion termination criterion	ı	1
-	Location for the value of terminal control	0	#
DTNP	Powered flight integration step size	4	ပ (၁ (၃)
DINF	Free flight integration step size	32	<b>3</b> e C
BMT	Flag to indicate non-inertial platform	0	ı
BRTAB	Flag to indicate reading the rate table to determine platform orientation	5	1
TGOP	Time to end first phase	8	၁၅
_		8	•
2	NOIE: Ine last phase is always terminated by the	8	•
•		•	•
•	•	. •	•
•	•	•	•
Z	Time to end the N+1 phase (N+1 = $1, 2 12$ )	8	<b>3</b> 60

\*No entry results in taking files in sequence.

\*\*TIME (sec), THETA (deg), or ALTP and ALTM (ft)

Table G-2. Orientation and Control Data (Concluded)

Symbol	Description	Value	Units
GMEGE	Earth rotation rate	7. 2921152 × 10"5	rad/sec
¥	Earth equatorial radius	$2.0925696 \times 10^{7}$	¥
UM	Gravity constant (used in equations of motion)	$1.4076452 \times 10^{16}$	ft <sup>3</sup> /sec <sup>2</sup>
<b>1</b> 3	Earth potential function constant	$1.6234633 \times 10^{-3}$	,
H	Earth potential function constant	0	•
ū	Earth potential function constant	$8.849057 \times 10^{-6}$	ı
MU	Equals GM (used in variational equations)	1.4076452 $\times$ 10 <sup>16</sup>	ft 3/sec 2
END	Indicates end of ERAM data input for this case	•	•
ENDJØB	Indicates end of job, i.e., there are no more ERAN cases to be run	1	ı

Table G-3. Program Constants (Conversion Factors)

From	То	Conversion	From	To	Conversion
8ec	rad	$0.48481368 \times 10^{-5}$	rad	sec )	$2.062648 \times 10^{5}$
deg/hr	sec/sec				
deg/hr	red/sec	$0.48481368 \times 10^{-5}$	rad/sec	deg/l.r	$2.062648 \times 10^{5}$
deg/hr	MERU	66.66667	MERU	deg/hr	0.015
deg/hr/g	rad/sec/ft/sec <sup>2</sup>	$0.15068493 \times 10^{-6}$	rad/sec/ft/sec	deg/hr/g	6.1636364 × 10 <sup>6</sup>
deg/hr/g <sup>2</sup>	rad/sec/(ft/sec <sup>2</sup> ) <sup>2</sup>	$0.46834379 \times 10^{-8}$	rad, sec/(ft/sec <sup>2</sup> )	deg/hr/g <sup>2</sup>	
800	ft/sec <sup>2</sup>	$0.32174 \times 10^2$	ft/sec <sup>2</sup>	<b>60</b> 0	
() 8ec	g/g(rad)	0, 48481368 × 10 <sup>-5</sup>			
8/8	1/ft/sec <sup>2</sup>	$0.31080997 \times 10^{-1}$	1/ft/sec <sup>2</sup>	8/8	3.2174 × 10 <sup>±</sup>
8/8	1/(ft/sec <sup>2</sup> )	$0.96602838 \times 10^{-3}$	1/(ft/sec <sup>2</sup> )	8/8	$1.0351663 \times 10^3$
sec/g	rad/ft/sec 2	$0.15068493 \times 10^{-6}$	rad/ft/sec	sec/g	6. 1636364 × 10 <sup>6</sup>
sec/g <sup>2</sup>	rad/(ft/sec <sup>2</sup> )	$0.46834379 \times 10^{-8}$	rad/(ft/sec <sup>2</sup> )	sec/g <sup>2</sup>	$2.135184 \times 10^{8}$
ft	n mi	$0.16457916 \times 10^{-3}$	n mi	f	$6.0761033 \times 10^3$

NOTE: Underlined numbers only are program constants.

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Security Classification

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13. ABSTRACT The theory and assumptions used in	Space Systems Division Air Force Systems Command Los Angeles, California  developing equations for the error
The theory and assumptions used in analysis of a general class of inertia	Space Systems Division Air Force Systems Command Los Angeles. California  developing equations for the error al navigation systems are described.
The theory and assumptions used in analysis of a general class of inertia. The computer program developed for	Space Systems Division Air Force Systems Command Los Angeles. California  developing equations for the error al navigation systems are described. In their solution is described from a
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KEY WORDS

Digital Computer Program

Error Analysis

Inertial Navigation

Guidance

Acceleromete.

Resets

Abstract (Continued)

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